## Results

## December 12, 2011

## Properties

	plain	simple ind	approx	fixpoint ind	struct ind
$prop_{add_{comm}}$					√ fin
+ x y = + y x					
$prop_{assoc_{mul}}$					
$\star$ x (* y z) = * (* x y) z					
$prop_{assoc_{plus}}$		$\checkmark_{\infty}$	$\sqrt{\infty}$	$\checkmark_{\infty}$	$\checkmark_{\infty}$
+ x (+ y z) = + (+ x y) z					
$prop_{idem_{mul}}$			$\sqrt{\infty}$		
* x x != x					
$prop_{idem_{plus}}$			$\sqrt{\infty}$		
+ x x != x					
$prop_{le_{plus}}$		√ fin			√ fin
<= n (+ n m) = True					
$prop_{le_{plus_{sym}}}$					
<= n (+ m n) = True					
$prop_{le_{succ_{plus}}}$		√ fin			√ fin
< i (S (+ i m)) = True					
$prop_{left_{distrib}}$					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$					
$prop_{left_{identity_{mul}}}$		$\checkmark_{\infty}$			$\checkmark_{\infty}$
$\star$ (S (Z)) x = x					
$prop_{left_{identity}_{plus}}$		$\checkmark_{\infty}$	$\sqrt{\infty}$		$\checkmark_{\infty}$
$+$ (Z) $\times = \times$					
$prop_{lt_{suc}}$					
<pre>&lt; i (S (+ m i)) = True</pre>					
$prop_{lt_{zero}_{eq_{zero}}}$		√ fin			√ fin
<= n (Z) = == n (Z)					
$prop_{max_{absorb}}$					√ fin
$\max x (\min x y) = x$					
$prop_{max_{assoc}}$					$\checkmark_{\infty}$
$\max$ (max a b) c = max a (max b c)					
$prop_{max_{le}}$					√ fin
== (max a b) a = <= b a					
$prop_{max_{le_{sym}}}$					√ fin
== (max a b) b = <= a b					
$prop_{max_{sym}}$					$\checkmark_{\infty}$
max a b = max b a					

$prop_{min_{absorb}}$ min x (max x y) = x		√ fin
$prop_{min_{assoc}}$ min (min a b) c = min a (min b c)		√∞
$prop_{min_{le}}$ == (min a b) a = <= a b		$\checkmark_{ m fin}$
$prop_{min_{le_{sym}}}$ == (min a b) b = <= b a	√ fin	$\checkmark_{ m fin}$
$prop_{min_{sym}}$ min a b = min b a		√ fin
$prop_{minus_{absorbish}}$ - (+ n m) n = m	√ fin	ightharpoons fin
$ prop_{minus_{assocish}} $ $ - (- i j) k = - i (+ j k) $	√ <sub>∞</sub>	$\checkmark_{\infty}$
$prop_{minus_{distribish}}$ - (+ k m) (+ k n) = - m n	√ fin	√ fin
$prop_{minus_{plus}}$ - (+ m n) n = m		
$prop_{minus_{zero}}$ $-$ m m = Z	√ fin	$\checkmark_{ m fin}$
$prop_{minus_{zeroish}}$ - n (+ n m) = Z	√ fin	√ fin
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
<pre>prop<sub>refl</sub> == x x = True</pre>	√ fin	√ fin
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	√ <sub>∞</sub>	√∞
$\begin{array}{ccc} prop_{right_{identity_{plus}}} \\ + & \times & (Z) & = & \times \end{array}$	√ <sub>∞</sub>	√∞
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	√ fin	√ fin
$prop_{zero_{is_{one}}}$ $Z := S (Z)$	$\sqrt{\infty}$	

## Summary

	total	plain	simple ind	approx	fixpoint ind	struct ind	
√ <sub>∞</sub>	12/36	1/12	6/12	6/12	1/12	9/12	
√ fin	17/36		10/17			17/17	