

# CHAPTER 10 : FUNCTIONAL LANGUAGES

# Functional Programming Languages

- Pure Functional languages:
  - ▣ Pure (original) Lisp
  - ▣ Miranda
  - ▣ Haskell
  - ▣ Single Assignment C
- Typed Functional languages:
  - ▣ ML
  - ▣ OCaml
  - ▣ Haskell
  - ▣ F#

# Functional Programming

- Can Programming be liberated from the von Neumann Style?

John Backus

- ▣ Purely functional languages are better than imperative language
  - More readable
  - More reliable
  - More likely to be correct

# Functional Programming



Lisp is the medium of choice for people who enjoy free style and flexibility.

Gerald J. Sussman

A Lisp Programmer knows the value of everything, but the cost of nothing.

Alan Perlis

# Scheme



- Expressions:

- Atomic

- Compound

# Data Types

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- ▣ Atom
  - ▣ Number
  - ▣ Boolean
  - ▣ String
  - ▣ Character
  - ▣ Symbol
- ▣ List

# Data Types

## ▣ numbers:

- `+, -, *, /`
- `zero?`
- `number?`
- `=, <, >=, <=`

## ▣ symbols:

- `quote`
- `symbol?`
- `eq?`

# Scheme - Primitive Functions

## □ Examples:

- `(+ 3 4)`
- `(quote (+ 3 4))`
- `(+ 3 4 5 7)`
- `(/ 40 4 5)`
- `(/ 3)`
- `(- 1.0 0.9)`
- `(- 1000.0 999.9)`
- `((+ 1 2))`



# Scheme – Prefix notation

□ how do we write :

1.  $8 + 9 \times 4$

2.  $(9000 + 900 + 90 + 9) - (5000 + 500 + 50 + 5)$

# Scheme – Predicate Functions

- Boolean values

- #t

- #f

- boolean?, even?, odd?, zero?, negative?,

- or, and, not

# Scheme – Predicate Functions

## Examples:

- ▣ `(not (even? 6) )`
- ▣ `(negative? -8)`
- ▣ `(< 9 87 100)`
- ▣ `(= (/ 1 2) (/ 8 16) )`
- ▣ `(boolean? 'y)`

# Scheme - Lists

- *List* is a recursive structure:
  - Empty list
  - A pair
- *List form*: parenthesized collections of sublists and/or atoms  
e.g., `'(A B (C D) E)`

# Scheme - Lists

- LIST takes any number of parameters; returns a list with the parameters as elements

- CONS takes two parameters

1. either an atom or a list

2. a list

returns a new list that includes the first parameter as its first element and the second parameter as the remainder of its result

# Scheme - Lists

## □ Example:

1. `(cons 'A '(B C))`
2. `(list 'A '(B C) 'd)`
3. `(cons '(a b (c)) '())`
4. `(cons 'A 'B)`
5. `(list 'A 'B)`
6. `(list 'A '(B))`

# Scheme - Lists



- `APPEND` takes two or more lists as parameters  
returns a new list that contains all of the elements of the  
parameter lists in the specified order

# Scheme - Lists

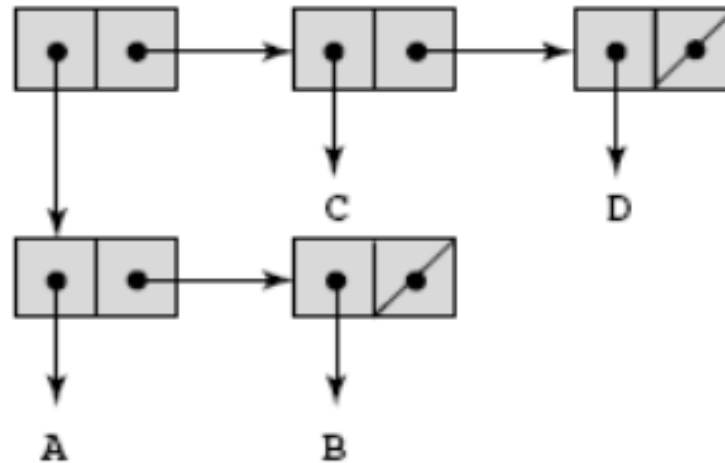
## □ Example:

1. `(append '(A) '(B C))`
2. `(append '(A B) '(B C) '(D))`
3. `(append '(a b (c)) '())`
4. `(append '((a b) (c d))  
          '((e f) (g h)))`
5. `(append '(A) 'B)`
6. `(append 'A '(B))`

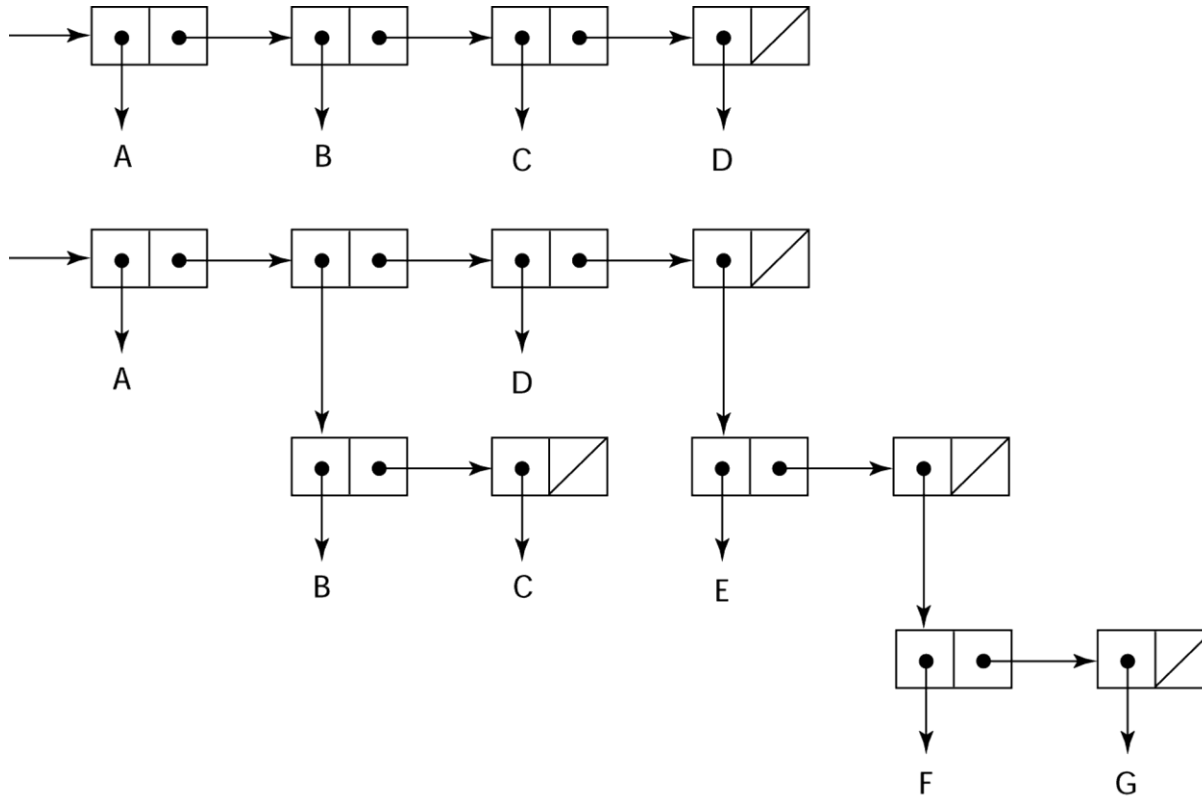


# Scheme - Lists

(CONS '(A B) '(C D))



# Scheme - Lists



# Scheme - Lists

- `car` takes a *pair*; returns the first element of that list

## Examples:

1. `(car '(A B C))`
2. `(car (car '((A B) C D)))`
3. `(car 'A)`
4. `(car '(A))`
5. `(car (car '(A)))`
6. `(car '())`

# Scheme - Lists

- `cdr` takes a pair parameter; returns the list after removing its first element

## Examples:

1. `(cdr '(A B C))`
2. `(cdr '((A B) C D))`
3. `(cdr 'A)`
4. `(cdr '(A))`
5. `(cdr '())`

# Predicate functions for Lists

- `list?`

- `null?`

## Examples:

1. `(list? 'A)`
2. `(list? '(A N) )`
3. `(list? '() )`
4. `(list? (+ 9 8) )`
5. `(null? 'A)`
6. `(null? '() )`

# pair? and equal?

1. `(pair? 1)`
  2. `(pair? (+ 9 8))`
  3. `(pair? (list 1 2))`
  4. `(pair? '(1 2))`
  5. `(pair? '())`
- 
1. `(eq? '(A N) '(A N))`
  2. `(equal? '(A N) '(A N))`

# Scheme – Define

- ▣ To bind a identifier to an expression

## Examples:

```
(define pi 3.141593)
```

```
(define two_pi (* 2 pi))
```

# Example

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```
(define lst (cons - (cons + ' ())))
```

```
((car lst) 2 4)
```

```
((cadr lst) 2 4)
```

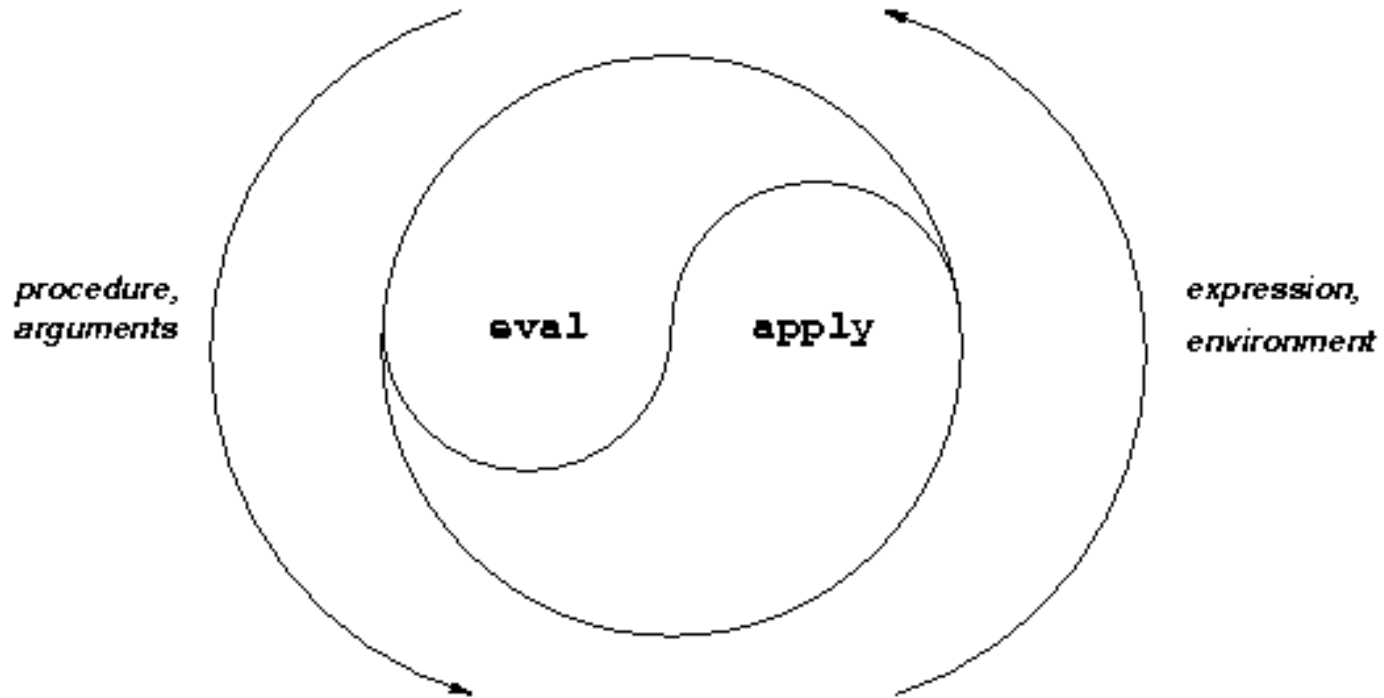


# Scheme - Simplicity

- Homogeneity:

- Program and data have the same representation
- Parentheses are NOT just grouping, as they are in Algol-family languages
- `quote` - takes one parameter; returns the parameter without evaluation

# Meta-circular Evaluator



H. Abelson and G.J. Sussman. *Structure and Interpretation of Computer Programs*, Fig. 4.1, p. 364

# Functions

- The function constructor builds **anonymous functions**
- A function is a list containing three things

(lambda (<parameters>) <body>)

# Scheme – Define

- ▣ To bind names to lambda expressions

- `(define square (lambda (x) (* x x)))`

**Example use:** `(square 5)`

# Functions - Examples

1. 

```
(define sum1  
  (lambda (x y)  
    (+ x y)))
```
2. 

```
(define sum2  
  (lambda() (lambda (x y)  
              (+ x y))))
```

# Scheme – Control Flow

- Multiple Selection - the special form, COND

General form:

```
(cond  
  (predicate_1 expr {expr} )  
  (predicate_1 expr {expr} )  
  . . .  
  (predicate_1 expr {expr} )  
  (else expr {expr} ) )
```

# Scheme – Control Flow

## Example:

```
(define (compare x y)
  (cond
    ((> x y) "x is greater than y")
    ((< x y) "y is greater than x")
    (else "x and y are equal")
  ))
```

# Scheme – Control Flow

```
(cond
  ((< 2 1) 2)
  ((< 1 2) 1))
```

---

```
(cond
  ((< 2 1)2)
  ((< 3 2) 3))
```



# Scheme – Control Flow

- Selection- the special form, IF

`(if predicate then_exp else_exp)`

**Example:**

```
(if (= count 0)
    0 (/ sum count))
```

# Scheme – Control Flow



**Example:**

```
(( (if (null? '(a)) cdr car)
   (cons cdr (cons car '())))) '(9 8 7))
```

# Local Binding



```
(let  
  ((var1 exp1) ... (varn expn))  
  body)
```

# Local Binding



```
(let ((x 2) (y 3))  
  (* x y))
```

# Local Binding

```
(let ((x 2) (y 3))  
  (let ((x 7)  
        (z (+ x y))))  
    (* z x)))
```

---

```
(let ((a 2) (b (* a a)))  
  (* a b))
```

# Example 1 – Recursive Functions



**Write a function that returns the length of a list /**

# Example 2 – Recursive Functions



Write a function that returns the sum of a list of numbers /

# Example 3 – Recursive Functions

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- Write a function that takes a list of numbers as input. The function should then return the list where each element is double its original value.



# Example 3 – Recursive Functions

```
(define (double lst)
  (cond
    ((null? lst) '())
    (else (cons (* (car lst) 2) (double
                      (cdr lst))))
  ))
```

# Example 4 – Recursive Functions

- Write a function called *member* that takes two args: a symbol *s* and a list of symbols *ls*. The function returns the index of the first element (0-based), if such an element exists. Otherwise, the function returns *#f*.

- `(member 'x ' (a b c) )`  $\Rightarrow$  `#f`

- `(member 'a ' (a b c) )`  $\Rightarrow$  `0`

- `(member 'b ' (w x a b c) )`  $\Rightarrow$  `3`

# Scheme vs Lisp

<b>Lisp</b>	<b>Scheme</b>	<b>Lisp</b>	<b>Scheme</b>
defun	define	rplacaset	car!
defvar	define	rplacdset	cdr!
car, cdr	car, cdr	mapcar	map
cons	cons	t	#t
null	null?	nil	#f
atom	atom?	nil	nil
eq, equal	eq?, equal?	nil	'()
Setq	set!	progn	begin
cond...t	cond...else		

# Functions That Build Code

## ❏ DRRacket → *Pretty Big language*

```
(define adder
  (lambda (lst)
    (cond
      ((null? lst) 0)
      (else (eval (cons '+ lst))))
  ))
```

# Variable Arity Procedures



```
(define fun  
  (lambda x x) )
```

# Apply-to-All Functions

```
(map (lambda (num)
      (* num num num)) '(2 3 4 5))
```

---

```
(map * '(2 3 4 5) '(1 2 3 4))
```

# Variable Arity Procedures



```
(define plus (lambda x
  (cond
    ((null? x) "Undefined")
    ((andmap number? x) (apply + x))
    (else #f))))
```

# First Class Functions



When a function can be

1. passed to another function
2. returned from a function
3. stored in a data structure



# First Class Functions



```
(define rem (lambda (test? a l)
  (cond
    ((null? l) '())
    ((test? (car l) a) (cdr l))
    (else
     (cons (car l) (rem test? a (cdr l)))))))
```

# Functional Programming in Perspective



## □ Advantages of Scheme

- Simple semantics
- Simple syntax
- Lack of side effects makes programs easier to understand
  - Programs can automatically be made concurrent
- Programs are short
  - 10 to 25% as large

# Functional Programming in Perspective

## □ Disadvantages

- Was not designed to benefit from the von Neumann architecture
- Requires a different mode of thinking by the programmer
- Execution time:
  - lots of copying of data through parameters
  - heavy use of pointers
  - frequent recursive calls
  - requires garbage collection

# References



- Michael L. Scott, Programming Language Pragmatics, Morgan Kaufmann, 3<sup>rd</sup> edition, 2009.
- Robert W. Sebesta, Concepts of Programming Languages, Addison Wesley, 10<sup>th</sup> edition, 2012.
- John C. Mitchell, Concepts in Programming Languages, Cambridge University Press, 2002.