

Probability & Statistics :-

Random variable :-

ex:- rolling dice \rightarrow 6 sides = $\{1, 2, 3, 4, 5, 6\}$

when rolled \downarrow any one of these equal outcome

Random Experiment

random variable $X = \{1, 2, 3, 4, 5, 6\}$

tossing a coin $\rightarrow Y = \{H, T\}$

Sample Space

$P(X=1) = 1/6$ $P(X=2) = 1/6 \dots$
 $P(X \text{ is even}) = 3/6 = 1/2$
 (probability of X being even)

$(P(X=2) + P(X=4) + P(X=6)) = 1/6 + 1/6 + 1/6$

$P(X \text{ is odd}) = 1/2$

$P(X=x_i) \rightarrow P(x_i)$ same thing diff notation

Finite set of values \rightarrow Discrete random variable

\rightarrow Height of randomly picked student

Y could be 162, 180, 120, 140, \dots

\rightarrow infinite values \rightarrow Continuous Random Variable

Outliers :-

Y : height of student

$\{122.2, 146.4, 132.5, \dots, 12.2, 156.3, 92.7, \dots\}$

outliers \rightarrow could be human error (or) actual height

\rightarrow Outliers can corrupt data

\rightarrow A discrete value is obtained by counting

\rightarrow A continuous value is obtained by measuring

Sample Space :- Set of all possible outcomes of an experiment

\rightarrow A random variable value depends on the outcome of a random phenomenon

Population & Sample :-

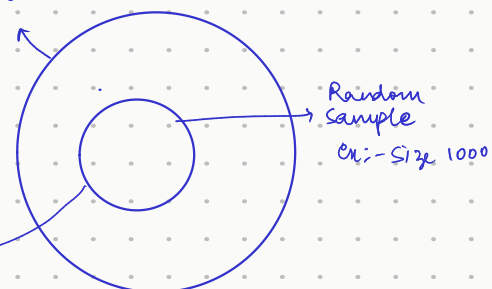
\rightarrow Estimating the average height of human

$$\mu = \frac{1}{\text{Pop}} \sum_{i=1}^{\text{Pop}} h_i \quad (\text{IMPOSSIBLE})$$

So we estimate

often represented by $\bar{x} = \frac{1}{1000} \sum_{i=1}^{1000} h_{is}$

Set of all humans in the world



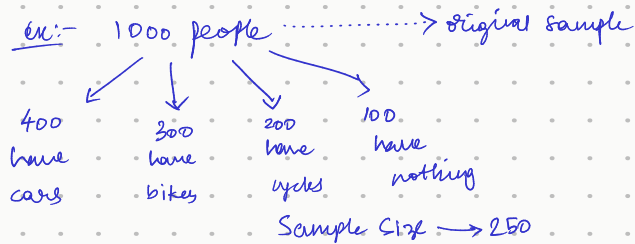
→ As sample size increases



Sampling is of two types:-

(i) Simple Sampling

(ii) Stratified Sampling → Unbiased sampling & more accurate results.



Simple Random Sampling

250 could have cars
(5%)

250 could have bikes
(8%)

100 bikes + 150 cars

Stratified Random Sampling

Cars → 100
bikes → 75
cycles → 50
nothing → 25

} There are random
but equal
imp to all
classes