

### Article 3 :

Publié dans la revue : *Journal of the Brazilian Society of Mechanical Sciences and Engineering*.

- **Éditeur** : Springer Nature (Berlin/Heidelberg)
- **ISSN** : **1678-5878** **E-ISSN** : **1806-3691**
- **Lien article DOI** : <https://doi.org/10.1007/s40430-025-05812-6>
- **Période de couverture par Scopus** : de 2003 à 2025
- **Domaines scientifiques** : Génie civil ; Mathématiques (Mathématiques générales)
- **Impact facture** : **2.1 (2024)** ;
- **Type de source** : Revue classée A (*lien* :  
[https://www.dgrstd.dz/fr/revues\\_A?search=Journal+of+the+Brazilian+Society+of+Mechanical+Sciences+and+Engineering](https://www.dgrstd.dz/fr/revues_A?search=Journal+of+the+Brazilian+Society+of+Mechanical+Sciences+and+Engineering))



Revues & publications scientifiques

## Moteur de recherche - Revues scientifiques

Journal of the Brazilian Society of Mechanical Sciences and Engineering

Résultat : 1

Télécharger

TITRE DE LA REVUE--	EDITEUR	ISSN	EISSN
JOURNAL OF THE BRAZILIAN SOCIETY OF MECHANICAL SCIENCES AND ENGINEERING	SPRINGER HEIDELBERG	1678-5878	1806-3691

# Static, free vibration, and buckling analysis of functionally graded plates using strain approach and Reissner–Mindlin elements

Review Paper | Published: 08 August 2025

Volume 47, article number 498, (2025) [Cite this article](#)



**Journal of the Brazilian Society of  
Mechanical Sciences and Engineering**

[Aims and scope →](#)

[Submit manuscript →](#)

Taqiyeddine Assas Messaoud Bourezane & Madjda Chenafi

94 Accesses [Explore all metrics →](#)

[Access this article](#)

[Log in via an institution →](#)



Check for  
updates

## Cite this article

Assas, T., Bourezane, M. & Chenafi, M. Static, free vibration, and buckling analysis of functionally graded plates using strain approach and Reissner–Mindlin elements. *J Braz. Soc. Mech. Sci. Eng.* **47**, 498 (2025). <https://doi.org/10.1007/s40430-025-05812-6>

[Download citation ↓](#)

Received

18 February 2024

Accepted

09 July 2025

Published

08 August 2025

DOI

<https://doi.org/10.1007/s40430-025-05812-6>

## Keywords

[Static](#)

[Free vibration](#)

[Buckling analysis](#)

[Reissner–Mindlin](#)

[Functionally graded](#)

[Strain based](#)



# Static, free vibration, and buckling analysis of functionally graded plates using strain approach and Reissner–Mindlin elements

Taqiyeddine Assas<sup>1</sup> · Messaoud Bourezane<sup>1</sup> · Madjda Chenaf<sup>1</sup>

Received: 18 February 2024 / Accepted: 9 July 2025 / Published online: 8 August 2025

© The Author(s), under exclusive licence to The Brazilian Society of Mechanical Sciences and Engineering 2025

## Abstract

The novelty of the present work lies in the development of a new four-node rectangular finite element using strain-based and Reissner–Mindlin theory. This paper is the first to apply this innovative approach to study the static, free vibration, and buckling responses of functionally graded materials (FGMs) plates. The mechanical properties of the FGM plate are considered to vary along the thickness direction by the power-law distributions. The notion of a neutral surface has been used to prevent the stretching–bending effect. The developed element has six degrees of freedom (DOFs) per node, obtained by combining two strain-based elements. The first one is a membrane which has three DOFs per node, and the second one is a Reissner–Mindlin plate which has three DOFs per node. The displacement fields of these components are represented by higher-order expressions based on the strain approach, which satisfy both rigid body modes and compatibility equations. The performance of the proposed element is evaluated through various numerical problems, and the results are compared with those published in the literature, showing good agreement. The impact of the gradient index, side-to-thickness ratio, aspect ratio, and loading types on the stresses, transverse displacements, frequency response, and critical buckling load of FGM plates is also investigated and discussed.

**Keywords** Static · Free vibration · Buckling analysis · Reissner–Mindlin · Functionally graded · Strain based

## 1 Introduction

In recent decades, the notion of functionally graded materials (FGM) has emerged from the work of a Japanese scientist in 1984 [1], which are used in industrial environments due to their excellent performance compared to conventional materials. FGM is a family of composite inhomogeneous materials consisting of a combination of isotropic materials, generally ceramics and metals, and it has many advantages, including progressive and continuous changes in their mechanical and thermal characteristics across the thickness, which prevents problems associated with traditional laminated composite structures, like higher inter-laminar stresses between the layers of a composite laminate [2].

As a result, these materials are attracting significant attention in various engineering disciplines, such as aerospace, mechanical, automotive, civil, and biomedical engineering. Many researches have been studied for static, free vibrational, and buckling behaviors of FGM beams, plates, and shells using several analytical and numerical approaches, relying on various theories, including classical plate theory (CPT), which neglects the effects of transverse shear deformation [3–7], first-order shear deformation theory (FSDT) having a linear variation in displacements [8–12], and higher-order shear deformation theory (HSDT) involving higher-order variations in displacements across the plate thickness, such as third-order shear deformation plate theory (TSDT), sinusoidal shear deformation plate theory (SSDT), and hyperbolic shear deformation plate theory (HDT) [13–23].

Several developers have employed the strain approach to design finite elements that are both efficient and durable. Initially, Ashwell et al. [24] introduced this methodology specifically for curved elements. Subsequently, this approach was employed in the analysis of shell structures [25–27]. It was later expanded to encompass plane-elasticity elements

---

Technical Editor: Samikkannu Raja.

---

✉ Taqiyeddine Assas  
taqiyeddine.assas@univ-biskra.dz

<sup>1</sup> Hydraulic and Environmental Development Laboratory (LAHE), Department of Civil and Hydraulic Engineering, University of Biskra, Biskra, Algeria