



Conservation statement

$$A+B = M$$

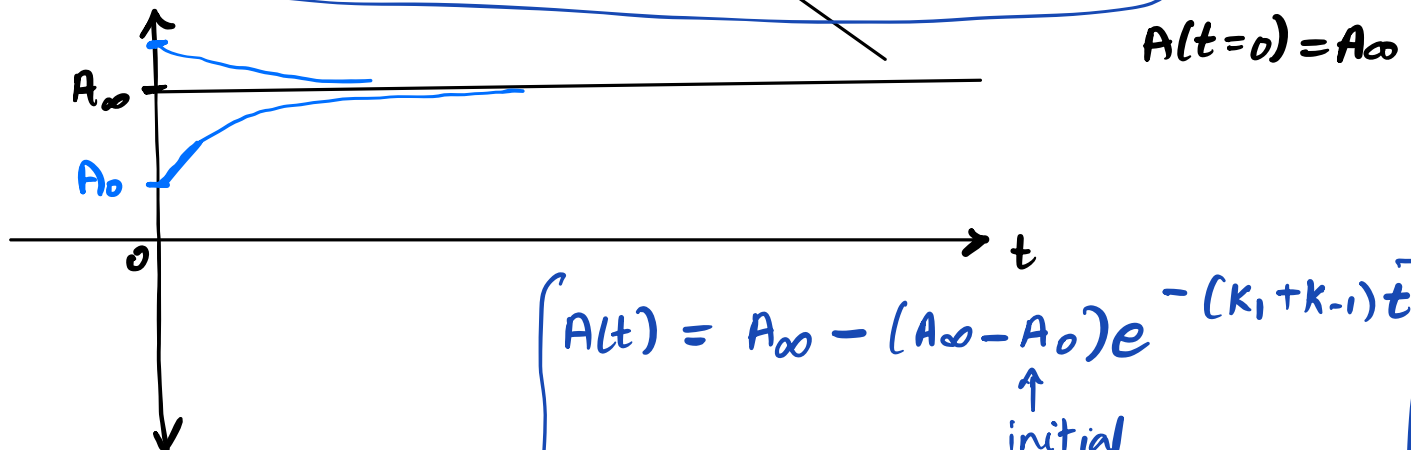
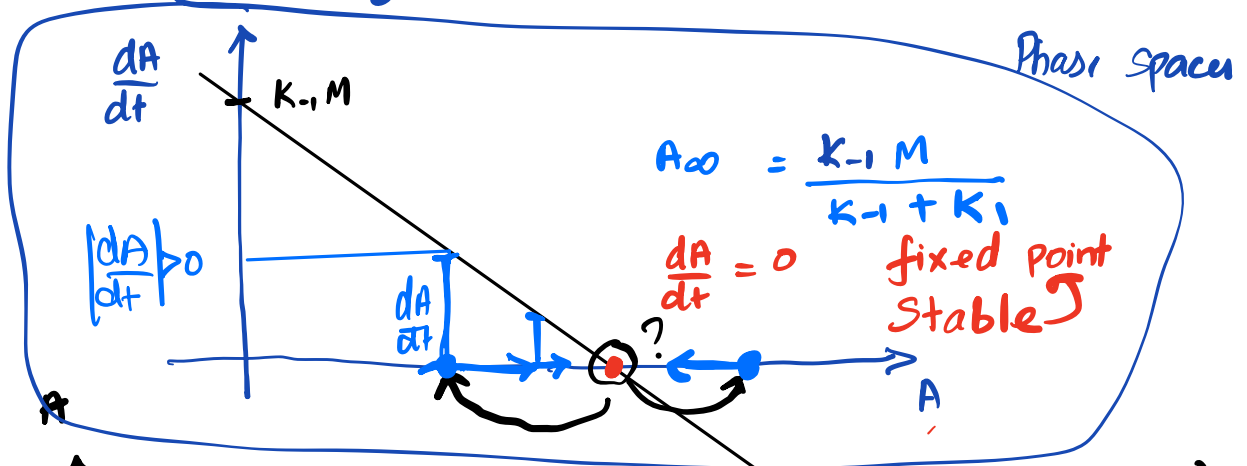
$$B = M - A$$

$$\frac{dA}{dt} = -k_1 A + k_{-1} B$$

$$\frac{dB}{dt} = k_1 A - k_{-1} B$$

$$\frac{dA}{dt} = -\underbrace{(k_1 + k_{-1})}_0 A + \underbrace{k_{-1} M}$$

Linear ordinary differential equation.



$$\left[ \begin{aligned} A(t) &= A_{\infty} - (A_{\infty} - A_0) e^{-(k_1 + k_{-1})t} \\ B(t) &= M - A(t) \end{aligned} \right]$$

↑  
initial





$[A] \Rightarrow$  concentration of A

Law of mass action -

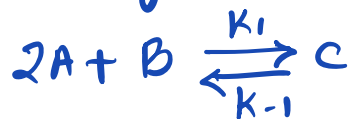
$$\frac{\text{moles}}{\text{time}} \left[ \frac{dP}{dt} \right] = \frac{\text{moles}^2}{-} k_1 [A][B] - \frac{-}{-} k_{-1} [P]$$

$k_1$   $\frac{1}{\text{moles time}}$



$$\frac{d[C]}{dt} = K A^3$$

Stoichiometry.



Forward

molecules	Stoichiometry
A	-2
B	-1
C	+1

Reverse

molecules	Stoichiometry
A	+2
B	+1
C	-1

$$\left[ \begin{array}{l} \frac{dA}{dt} = -2 \underbrace{k_1 A^2 B}_{\text{reaction}} + 2 k_{-1} C \\ \frac{dB}{dt} = -1 k_1 A^2 B + 1 k_{-1} C \\ \frac{dC}{dt} = k_1 A^2 B - k_{-1} C \end{array} \right] \begin{array}{l} A(t) \\ B(t) \\ C(t) \end{array}$$



Dimensionalization.

$$\frac{dA}{dt} = -2k_1 A^2 + 2k_{-1} C$$

$$\frac{dC}{dt} = k_1 A^2 - k_{-1} C$$

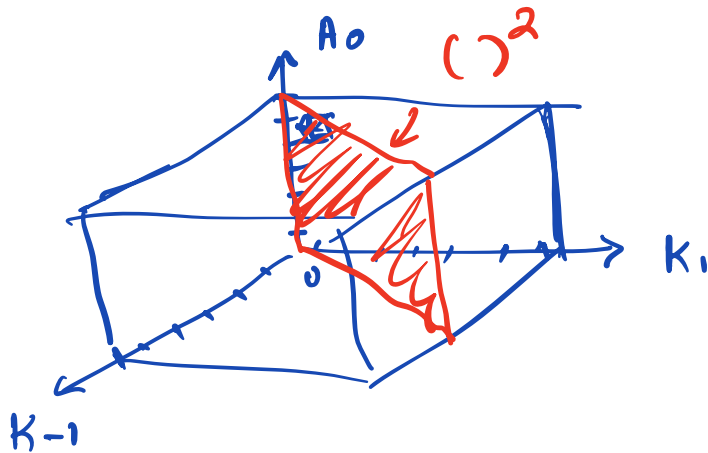
Conservation statement

$$\frac{dA}{dt} + 2\frac{dC}{dt} = 0$$

$$A + 2C = A_0$$

$A(t)$

$A_0, k_1, k_{-1}$



$( )^3$

$k_1 f(k_{-1}, \dots)$

'composite' parameters

$$k' = \underline{f(k_1, k_{-1})}$$

'Non-dimensionalization and scaling'