$\quad \text{thus} \quad$

$$a \equiv b \pmod{p}$$

it follows that $a,b\in\mathbb{Z}$