

# The Relational Data Model

COMP9311 25T3; Week 2.1

*By Wenjie Zhang, UNSW*

# Notice

Lab 01 this week:

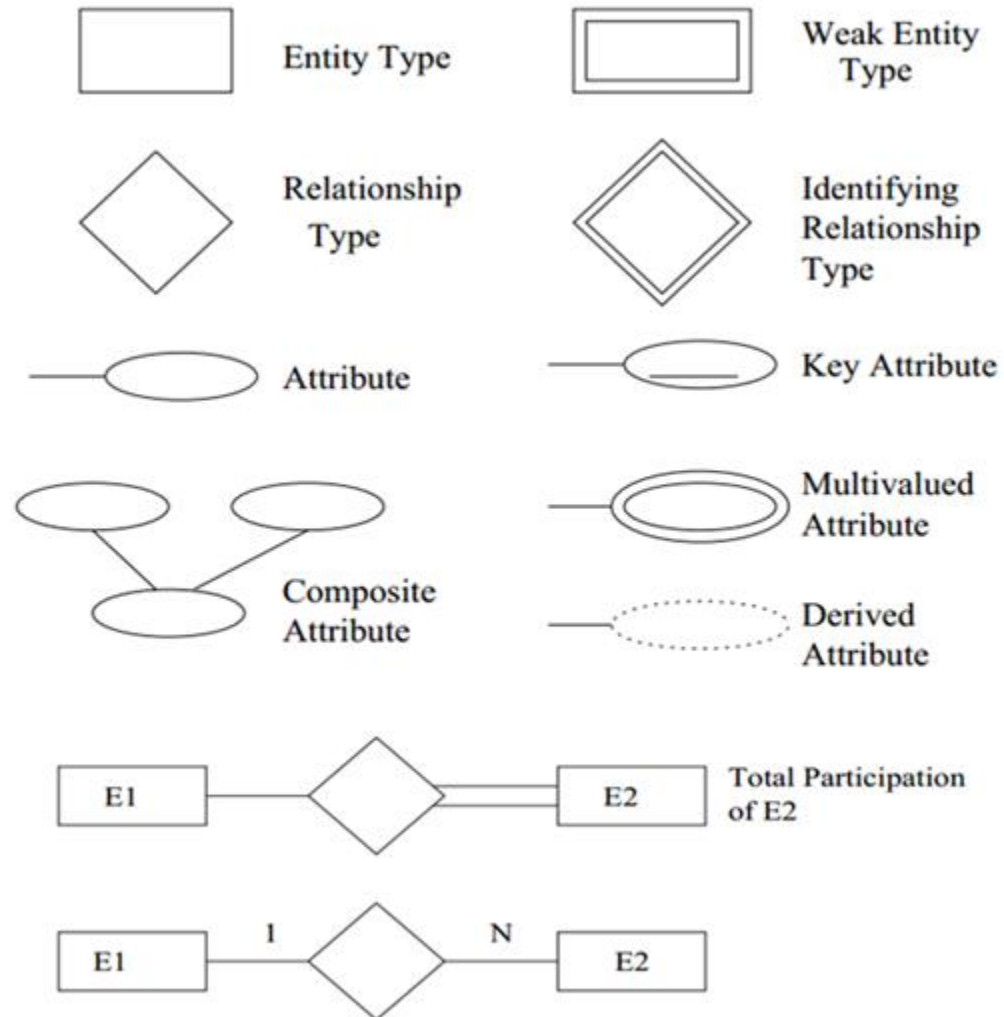
- **Bring Your Own Device**
- Setting up your PostgreSQL server

# Recap – Data Modelling

## Checklist on ER modeling

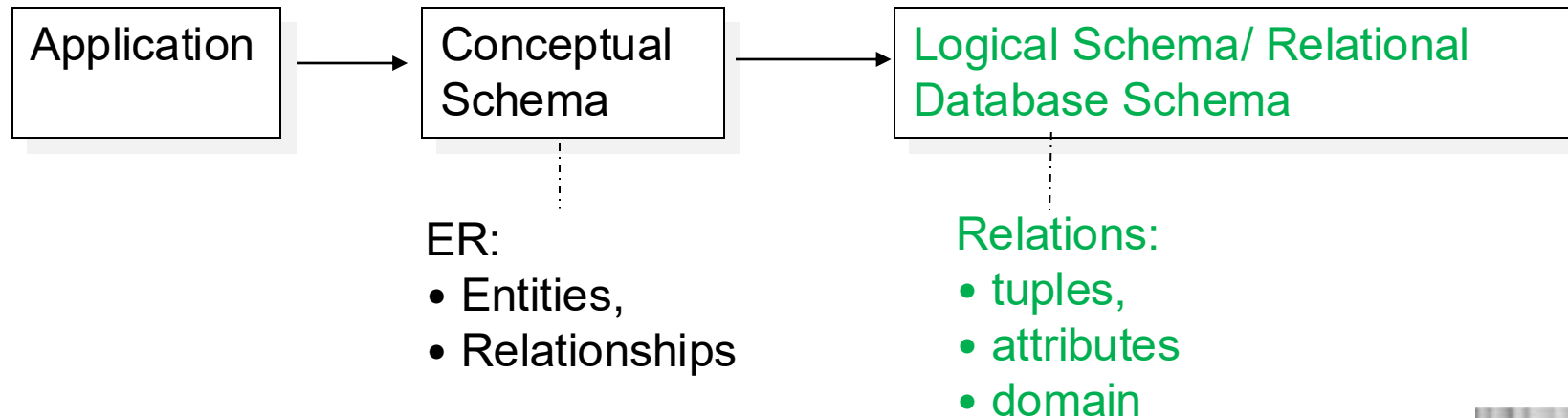
1. Did you model every significant **entity** that has independent instances?
2. Did you model the entity in the correct type? **Strong entity** or **weak entity**?
3. Did you capture all the main **relationships** between entities?
4. Does every relationship have the correct **cardinality**
5. Did you correctly capture **participation**? Is it too loose? Too strict?
6. Is each **attribute** modeled with the most appropriate attribute type?
7. (For comp9311) did you use the comp9311 notation?

# Recap – Standard Notation



# Introduction

The most popular data model for database systems (see Week1 Monday)



English computer scientist [Edgar F. Codd](#)

**A Relational Model of Data for Large Shared Data Banks (1970)**

<https://www.seas.upenn.edu/~zives/03f/cis550/codd.pdf>



# Relational Data Model Concepts

The relational data model is the most widely used data model for database systems.

The *relational data model* describes the world as

- a **collection** of inter-connected *relations*

The goal of the relational model:

- a simple, general data modelling formalism
- which maps easily to file structures (i.e. implementable)

The relational model has **two styles** of terminology:

- mathematical: relation, tuple, attribute, ...
- data-oriented: table, record, field/column, ...

# Structures

In the relational model, everything is described using **relations**.

A relation can be thought of as a **named table**.


- Each column of the table corresponds to a *named attribute*.
- Each row of the table is called a ***tuple*** of the relation.

The set of allowed values for an attribute is called its *domain*.

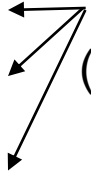
# Example of a Relation

Name	Position	Goals	Age	Height	Weight
Heady	Half-forward	17	24	183	83
Sumich	Full-forward	59	26	191	92
Langdon	Utility	23	23	189	86

attributes  
(or columns)



tuples  
(or rows)





# Relational Data Model

Mathematically,

- a *domain*  $D$  is a set of **atomic** values (having some fixed data type) representing some semantic meaning.
- an *attribute*  $A$  is the name of a role played by a *domain*,  $dom(A)$ .
- a *relation schema*  $R$ , denoted by  $R(A_1, A_2, \dots, A_n)$ , is a set of attributes  $R = \{A_1, A_2, \dots, A_n\}$ .

**Composite and multivalued attributes are not allowed!**

# Relations are Unordered

- Why is the order of tuples irrelevant?
- An ***unordered collection*** of elements is a ***set***:  
 $\{1, 2, 3\} = \{2, 1, 3\}.$
- An ***ordered collection*** of elements is a ***list***:  
 $(1, 2, 3) \neq (2, 1, 3).$
- A ***set*** expresses ***membership***.
- Example: we care that you are a student, but we don't care whether you're the 6th student to register (the order).

# Example of Unordered Relation

Both are ***the same*** relation. The ordering of columns or rows is irrelevant.

PLAYER					
Name	Position	Goals	Age	Height	Weight
Heady	Half-forward	17	24	183	83
Sumich	Full-forward	59	26	191	92
Langdon	Utility	23	23	189	86

=

PLAYER					
Name	Age	Height	Weight	Goals	Position
Sumich	26	191	92	59	Full-forward
Langdon	23	189	86	23	Utility
Heady	24	183	83	17	Half-forward

***Question: Ordering within a tuple?***

***Yes, but an alternative definition exists that contains no ordering.***

# Why Relational Model?

- Very simple model
- Often a good match for the way we think about our data
- Foundations in logic and set theory (will be introduced in later parts of the course)

# Keys

Keys are used to identify tuples in a relation.

A ***superkey*** is a set of attributes that uniquely determines a tuple.

A ***candidate key*** is a *minimal* superkey, i.e., none of whose subsets is a superkey.

# Example

Assuming no two people have the same name, then {Name} is unique and therefore is a **candidate key** for PLAYER

{Goals} usually cannot be a candidate key since different players might have the same number of goals.

{Name, Goals} is a *super key* but not a **candidate key** (because {Name} is a key).

PLAYER					
Name	Position	Goals	Age	Height	Weight
Heady	Half-forward	17	24	183	83
Sumich	Full-forward	59	26	191	92
Langdon	Utility	23	23	189	86

# Keys

PLAYER						
Person_ID	Name	Position	Goals	Age	Height	Weight
1	Heady	Half-forward	17	24	183	83
2	Sumich	Full-forward	59	26	191	92
3	Langdon	Utility	23	23	189	86

A **primary key** is a designated candidate key.

In many applications, it is necessary to invent a primary key if there is no natural one - often this would be a non-negative integer.

e.g. Person\_ID.

When a relation schema has several candidate keys, choosing a primary key with a single attribute or a small number of attributes is usually better.

# Number of Superkeys

$\{A\}$ :  $\{A\}$  1

$\{A,B\}$ :  $\{A\}, \{B\}, \{A,B\}$  3

$\{A,B,C\}$ :  $\{A\}, \{B\}, \{C\}, \{A,B\}, \{B,C\}, \{A,C\}, \{A,B,C\}$  7

$(2^n)-1$



# Relation Referring to Another Relation

How do we store relationships? For example, ENROLLMENT in this case?

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
4	Ms J.Gledill
5	Ms B.K.Lee

RESEARCHER:

<u>Person#</u>	Name
1	Dr C.C.Chen
2	Dr R.G.Wilkinson

COURSE:

<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

# Store the values of the Primary Key?

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
4	Ms J.Gledill
5	Ms B.K.Lee

RESEARCHER:

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1	Dr C.C.Chen
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COURSE:

<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

ENROLMENT:

<u>Enrolment#</u>	Student	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.

# Relation Referring to Another Relation

**Foreign key:** *an attribute that keeps the value of a primary key of another relation.*

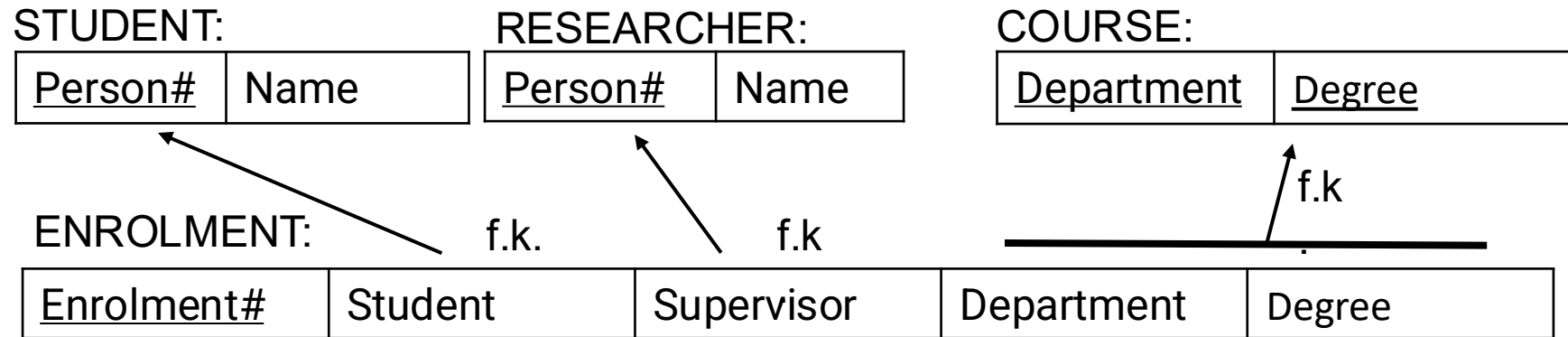
A set of attributes from a relation schema  $R_1$  may be a foreign key,  $FK$ , if

- the attributes have *the same domains* as the attributes in the primary key of another relation schema  $R_2$ , and
- a value of  $FK$  in a tuple  $t_1$  of  $R_1$  either occurs as a value of PK for some tuple  $t_2$  in  $R_2$  or is null.

**Referential integrity:** The value of  $FK$  must occur in the other relation or be entirely NULL.

# Example of Foreign keys

This is what we mean



# Relational Integrity Constraints

We need to keep the relational database in a ***valid state***:

Three integrity constraints are important

1. **Key constraint**: candidate key values must be unique for every relation instance.
2. **Entity integrity**: an attribute that is part of a primary key cannot be NULL.
3. **Referential integrity**

*Valid state: a relation does not violate any integrity constraints.*

*Invalid state: a relation violates at least one integrity constraint*

# Relational Integrity Constraints

How can a valid relation become invalid?

A: Operations on the database can result in an invalid state.

Before proceeding with an ***update***, we need to...

- check that the result of the update will not violate any integrity constraints.

# Insertions

*Insertions:* When inserting, we need to check

- that the candidate keys are not already present,
- that the value of each foreign key either
  - is all NULL, or
  - is all non-NULL and occurs in the referenced relation.

# Insertion: Key constraint violation

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
4	Ms J.Gledill
5	Ms B.K.Lee

RESEARCHER:

<u>Person#</u>	Name
1	Dr C.C.Chen
2	Dr R.G.Wilkinson

COURSE:

<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

1. Insert < 2,  
*Dr.V.Ciesielski* > into  
RESEARCHER

ENROLMENT:

<u>Enrolment#</u>	Student	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.



# Insertion: Key constraint violation

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
4	Ms J.Gledill
5	Ms B.K.Lee

RESEARCHER:

<u>Person#</u>	Name
1	Dr C.C.Chen
2	Dr R.G.Wilkinson

COURSE:

<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

1. Insert < 2,  
*Dr.V.Ciesielski* > into  
RESEARCHER

Allowed? No. Violates  
a key constraint.

ENROLMENT:

<u>Enrolment#</u>	Student	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.

Action? Reject or  
allow the user to  
correct.

# Insertion: Key constraint violation

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
4	Ms J.Gledill
5	Ms B.K.Lee

RESEARCHER:

<u>Person#</u>	Name
1	Dr C.C.Chen
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COURSE:

<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

2. Insert <  
*Comp.Sci., NULL*>  
into COURSE

ENROLMENT:

<u>Enrolment#</u>	Student	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.

# Insertion: Key constraint violation

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
4	Ms J.Gledill
5	Ms B.K.Lee

RESEARCHER:

<u>Person#</u>	Name
1	Dr C.C.Chen
2	Dr R.G.Wilkinson

COURSE:

<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

2. Insert <  
*Comp.Sci., NULL*>  
into COURSE

Allowed? No.  
“Degree” is a part of  
the primary key, it  
cannot be NULL.

ENROLMENT:

<u>Enrolment#</u>	Student	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.

Action: Reject or  
allow the user to  
correct.

# Insertion: Referential integrity violation

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
4	Ms J.Gledill
5	Ms B.K.Lee

RESEARCHER:

<u>Person#</u>	Name
1	Dr C.C.Chen
2	Dr R.G.Wilkinson

COURSE:

<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

3. Insert < 5, 6, 2, *Psychology, Ph.D.* > into ENROLMENT

ENROLMENT:

<u>Enrolment#</u>	Student	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.

# Insertion: Referential integrity violation

STUDENT:

<u>Person#</u>	Name
1	Dr C.C.Chen
3	Ms K.Juliff
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5	Ms B.K.Lee

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<u>Department</u>	<u>Degree</u>
Psychology	Ph.D.
Comp.Sci.	Ph.D.
Comp.Sci.	M.Sc.
Psychology	M.Sc.

3. Insert < 5, 6, 2, *Psychology, Ph.D.* > into ENROLMENT

Allowed? No.  
Violates a referential integrity constraint (There is no person 6).

ENROLMENT:

<u>Enrolment#</u>	Student	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.

Action: Reject, correct or accept after insertion of person number

# Deletion

*Deletions:* When deleting, we need to check **referential integrity** – check whether the primary key occurs in another relation.

Example: Delete tuple with Person# = 2 from RESEARCHER

RESEARCHER:

Person#	Name
1	Dr C.C.Chen
2	Dr R.G.Wilkinson

ENROLMENT:

Enrolment#	Supervisee	Supervisor	Department	Degree
1	1	2	Psychology	Ph.D.
2	3	1	Comp.Sci.	Ph.D.
3	4	1	Comp.Sci.	M.Sc.
4	5	1	Comp.Sci.	M.Sc.

Allowed? No. Violates the referential integrity.

Action: Reject, correct or modify the ENROLMENT tuple by the actions on the next slides.

# Deletion: Constraint Checks

We sometimes need to delete tuples from relations, and the record may be referenced in other relations.

What can we do?

1. Delete it (*this requires another integrity check, possibly causing a cascade of deletions*), **or**
2. Set the foreign key value to NULL (*note this can't be done if it is part of a primary key*) or other values

# Modifications

Can changing a value lead to an invalid state? Not unless you're modifying the value of a key.

If the modified attribute is the primary key

- the same issues as deleting PK1 and then immediately inserting PK2.
- make sure deletion and insertion don't violate any steps.

If the modified attribute is a foreign key

- check that the new value refers to an existing tuple.

Note: all relational integrity constraints have to do with the key values.



# Relational database definition

- A *relational database schema*, is a set of relation schema  $\{R_1, \dots, R_m\}$  and a set of integrity constraints.
- A relational database instance is a set of relation instances  $\{r_1, \dots, r_m\}$  such that each  $r_i$  is an instance of  $R_i$ , and the integrity constraints are satisfied.

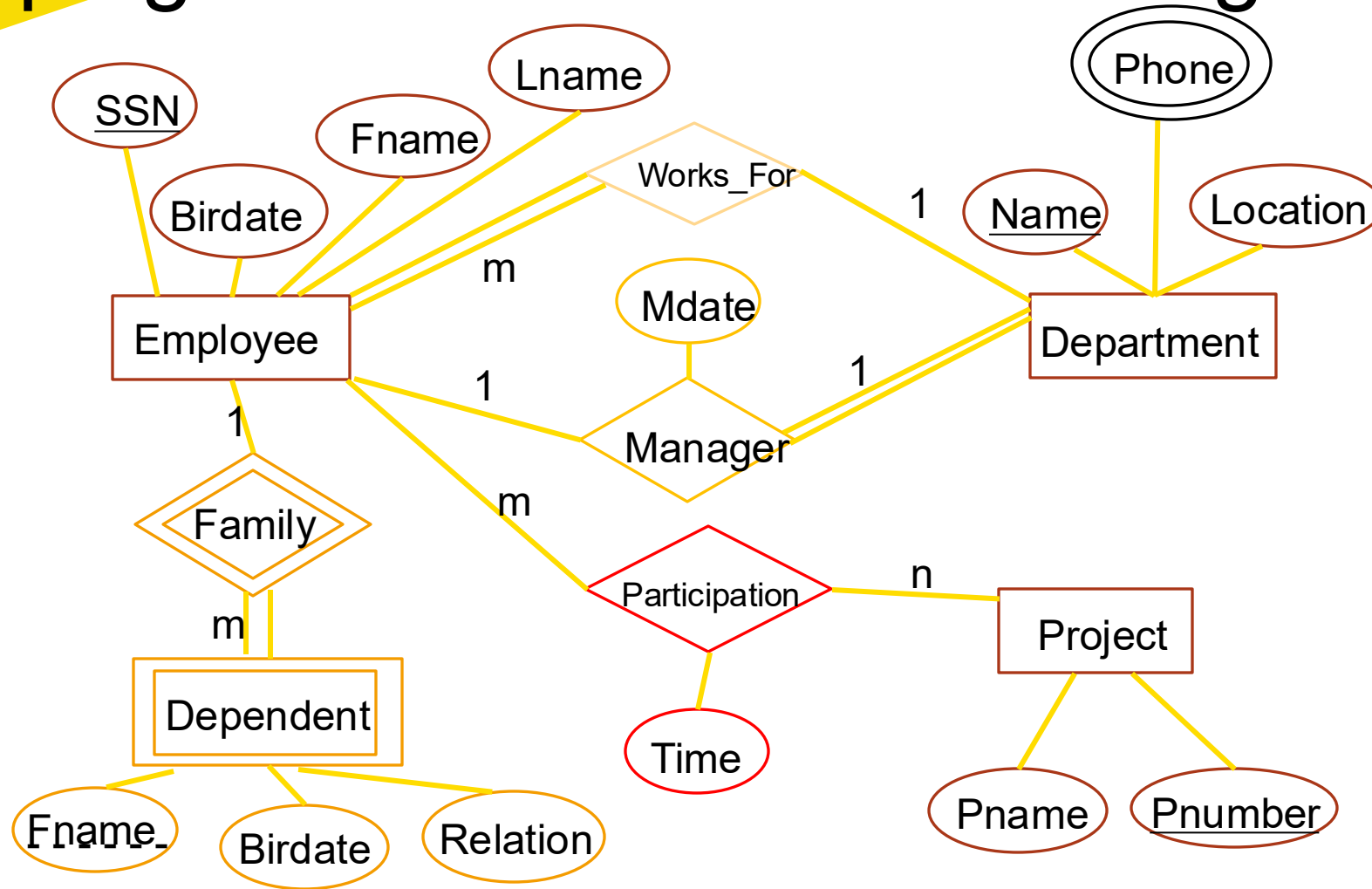
# ER to Relational Data Model Mapping

One technique for database design is to first design a conceptual schema using a high-level data model, and then map it to a conceptual schema in the DBMS data model for the chosen DBMS.

Here, we look at a way to do this mapping from the ER to the relational data model.

It involves the following **7 steps**.

# Mapping ER to Relational: Guiding Example

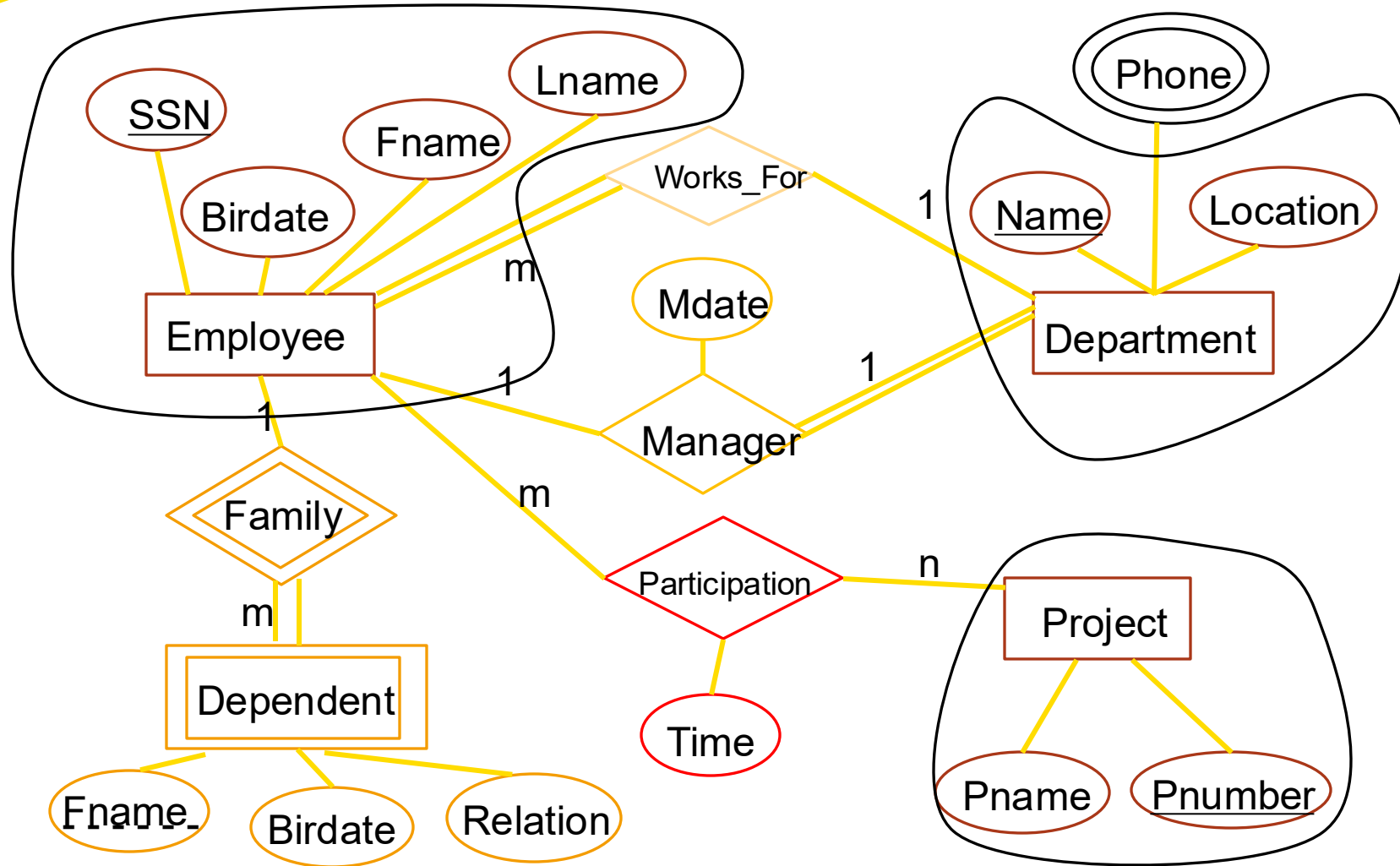


# Mapping Strong Entity Types

Step 1: For each ***strong entity*** (not weak entity) type E, create a new relation R with

- Attributes: all *simple attributes* (and simple components of composite attributes) of E.
- Key: key of E as the *primary key* for the relation.

# Mapping Strong Entity Types



# Mapping Strong Entity Types

Employee

<u>SSN</u>	Fname	Lname	Birdate
------------	-------	-------	---------

Department

<u>Name</u>	Location
-------------	----------

Project

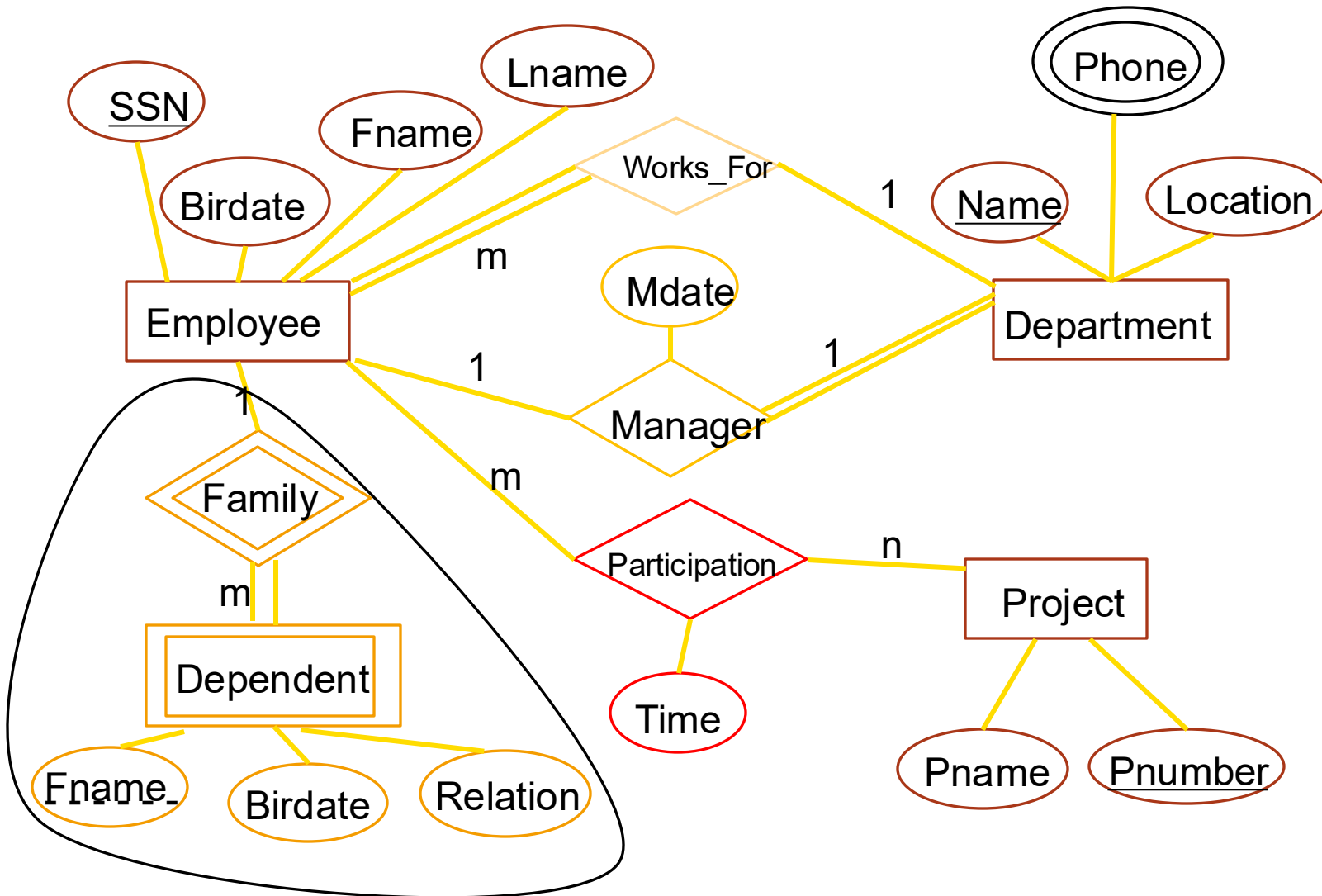
<u>Pnumber</u>	Pname
----------------	-------

# Mapping Weak Entity Types

Step 2 : For each ***weak entity type*** W with the owner entity type E, create a new relation R with

- Attributes :
  - all simple attributes (and simple components of composite attributes) of W,
  - and include the primary key attributes of the relation derived from E as the foreign key.
- Key of R: foreign key to E and partial key of W.

# Mapping Weak Entity Types





# Mapping Weak Entity Types

Employee

<u>SSN</u>	Fname	Lname	Birdate
------------	-------	-------	---------

Department

<u>Name</u>	Location
-------------	----------

Project

<u>Pnumber</u>	Pname
----------------	-------

Dependent

<u>SSN</u>	<u>Fname</u>	Birdate	Relation
------------	--------------	---------	----------

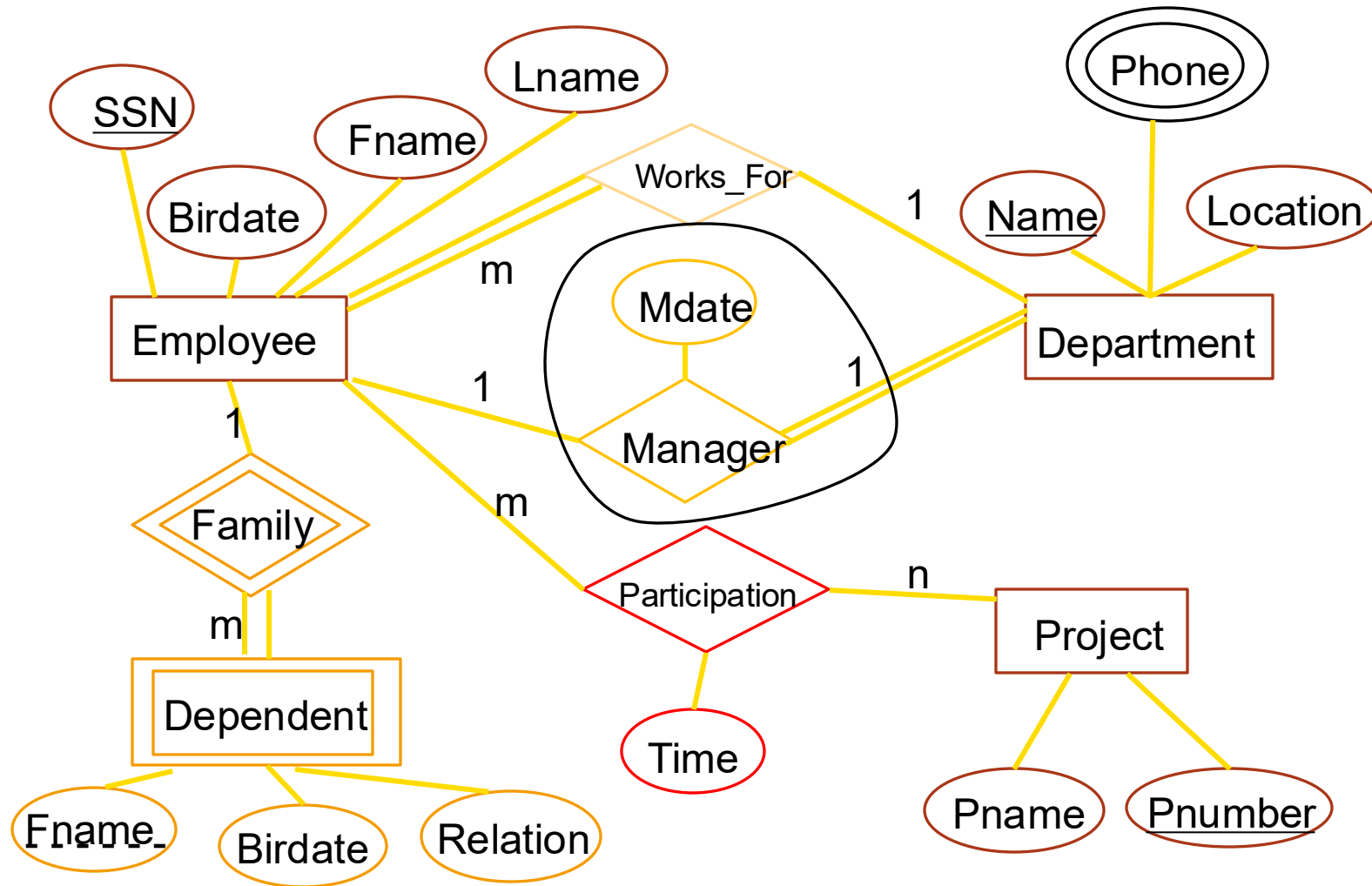
# Mapping 1:1 Relationship Types

Step 3 : For each **1:1 relationship type** B. Let E and F be the participating entity types. Let S and T be the corresponding relations.

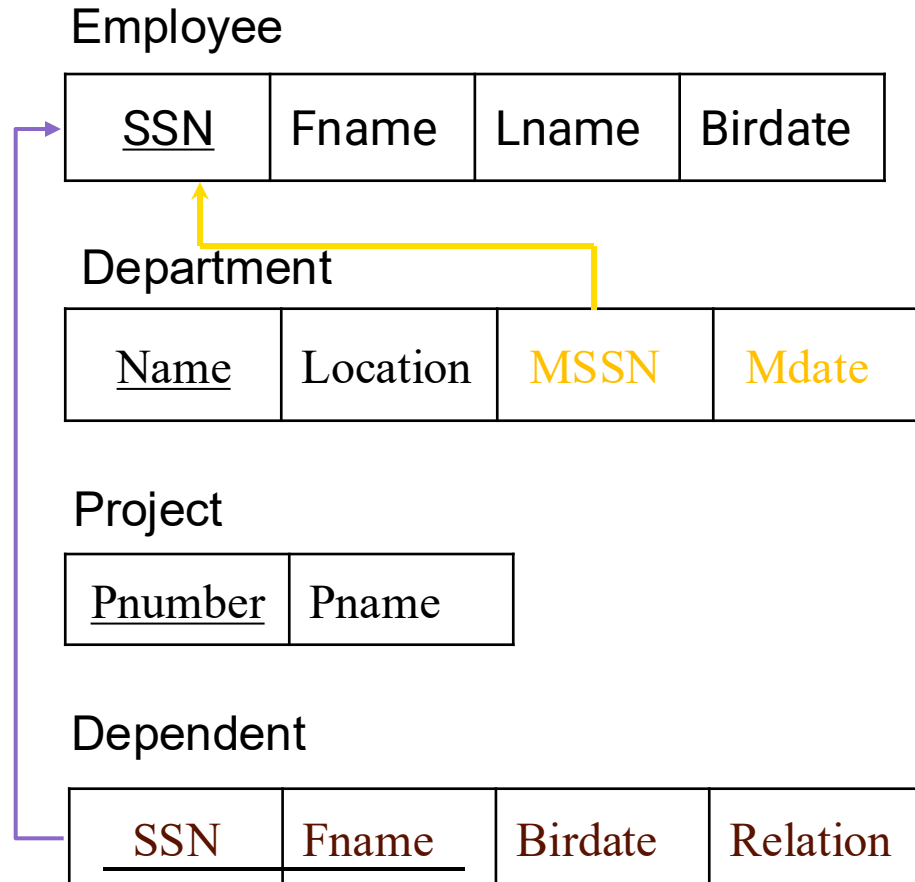
- Choose one of S and T (let S be the one that participates totally if there is one).
- Add attributes from the primary key of T to S as a foreign key.
- Add all simple attributes (and simple components of composite attributes) of B as attributes of S.

*(Alternatively, merge the two entity types and the relationship into a single relation, especially if **both participate totally and do not participate in other relationships**).*

# Relationship Types



# Mapping 1:1 Relationship Types



# Mapping 1:N Relationship Types

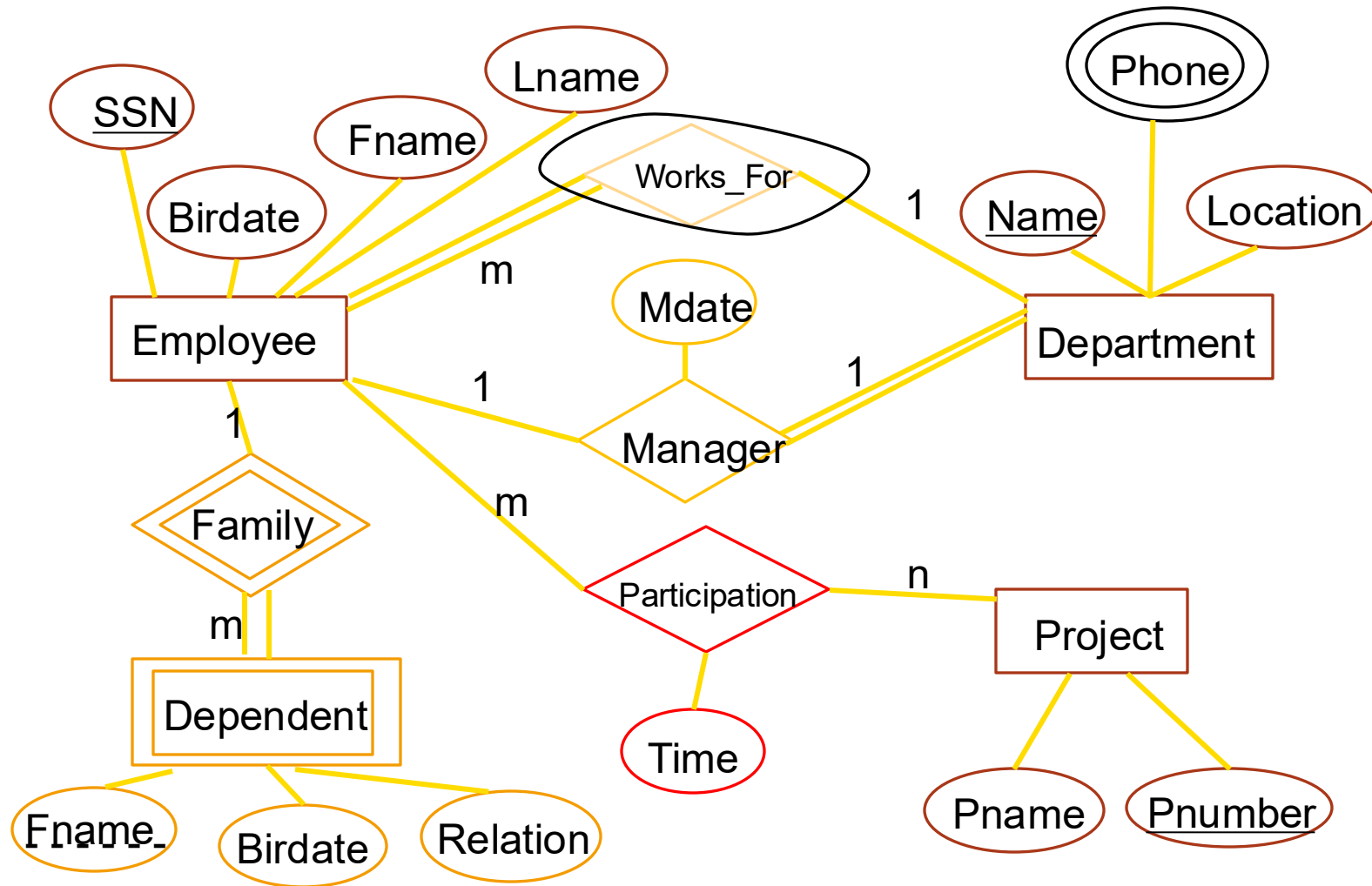
Step 4 : For each **1:N relationship type** B. Let E and F be the participating entity types. Let S and T be the corresponding relations. Let E be the entity on the 1 side and F on the N side.

Add to the relation belonging to entity T,

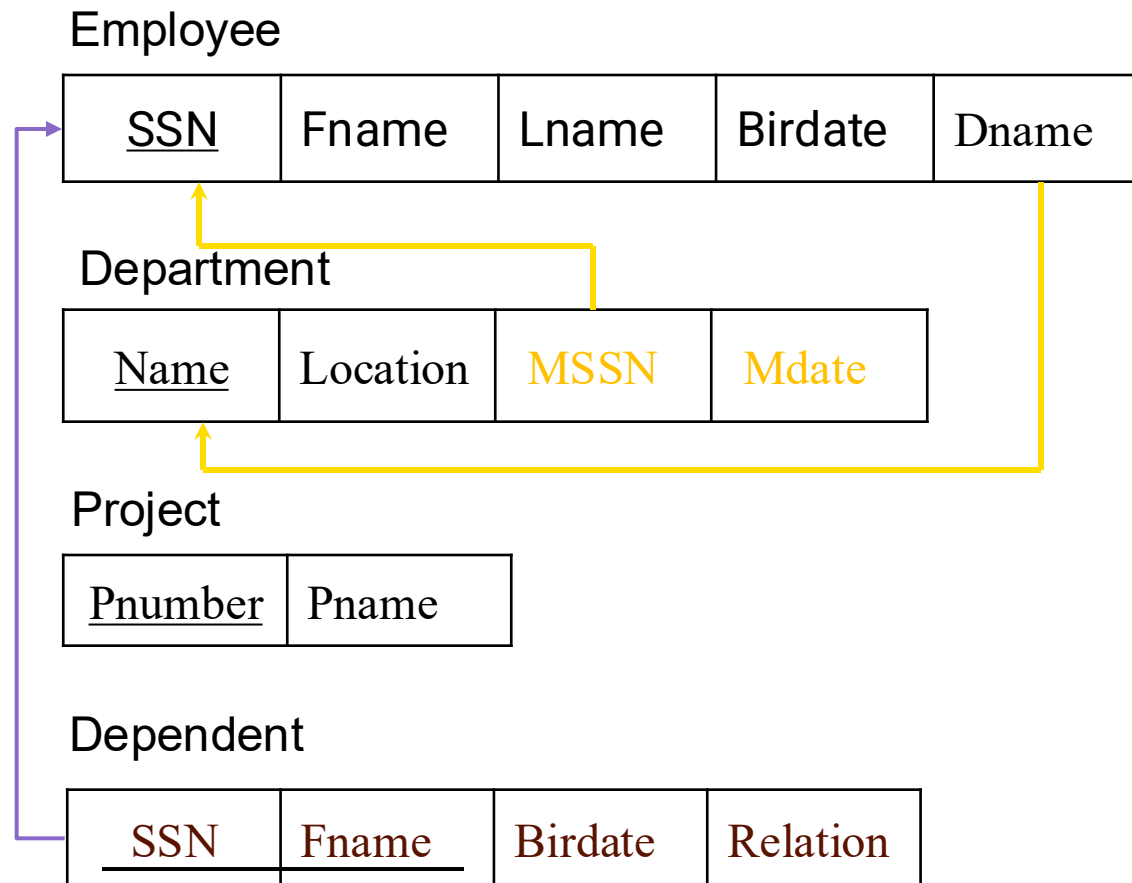
- the attributes from the primary key of S as a foreign key.
- any simple attributes (or simple components of composite attributes) from relationship B.

(Notice that this doesn't add any new tuples, just attributes.)

# Mapping 1:N Relationship Types



# Mapping 1:N Relationship Types



# Mapping M:N Relationship Types

Step 5: For each ***N:M relationship type*** B. Let E and F be the participating entity types. Let S and T be the corresponding relations

Create a new relation R (*cross-reference*) with

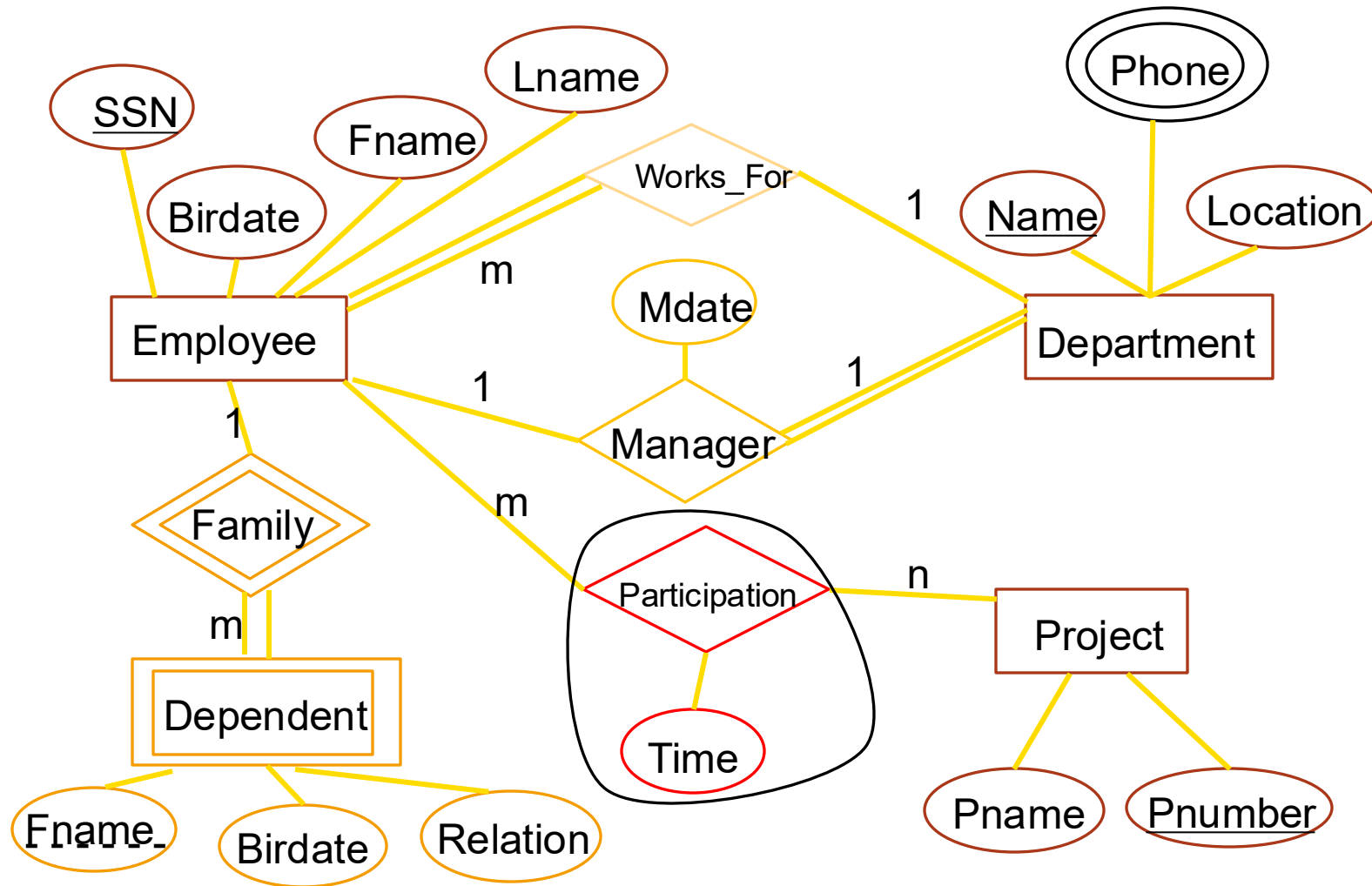
Attributes :

- Attributes from the key of S as a foreign key,
- Attributes from the key of T as a foreign key,
- Simple attributes and simple components of composite attributes of relation B.

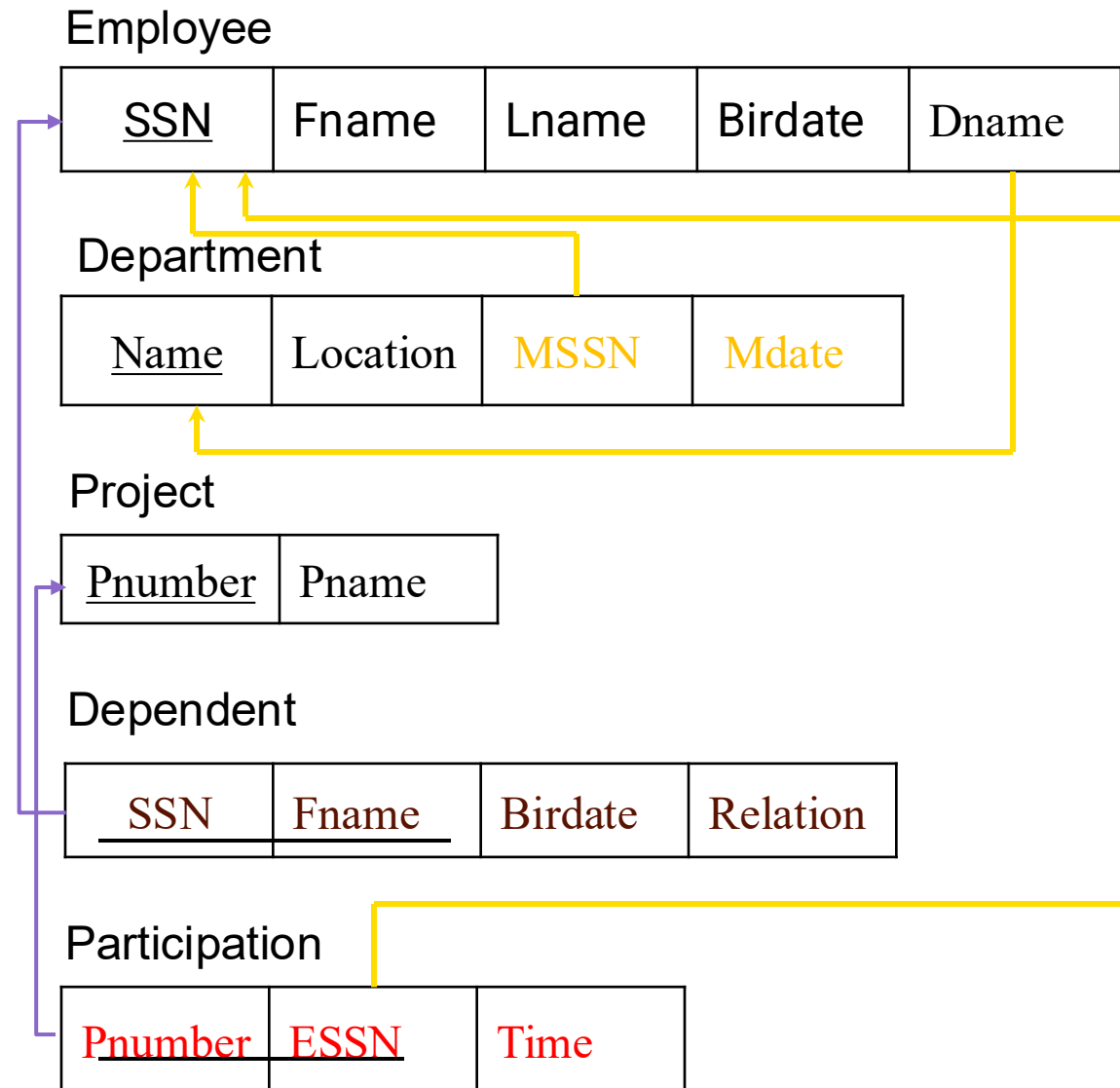
Key: All attributes from the key of S and T.



# Mapping M:N Relationship Types



# Mapping M:N Relationship Types



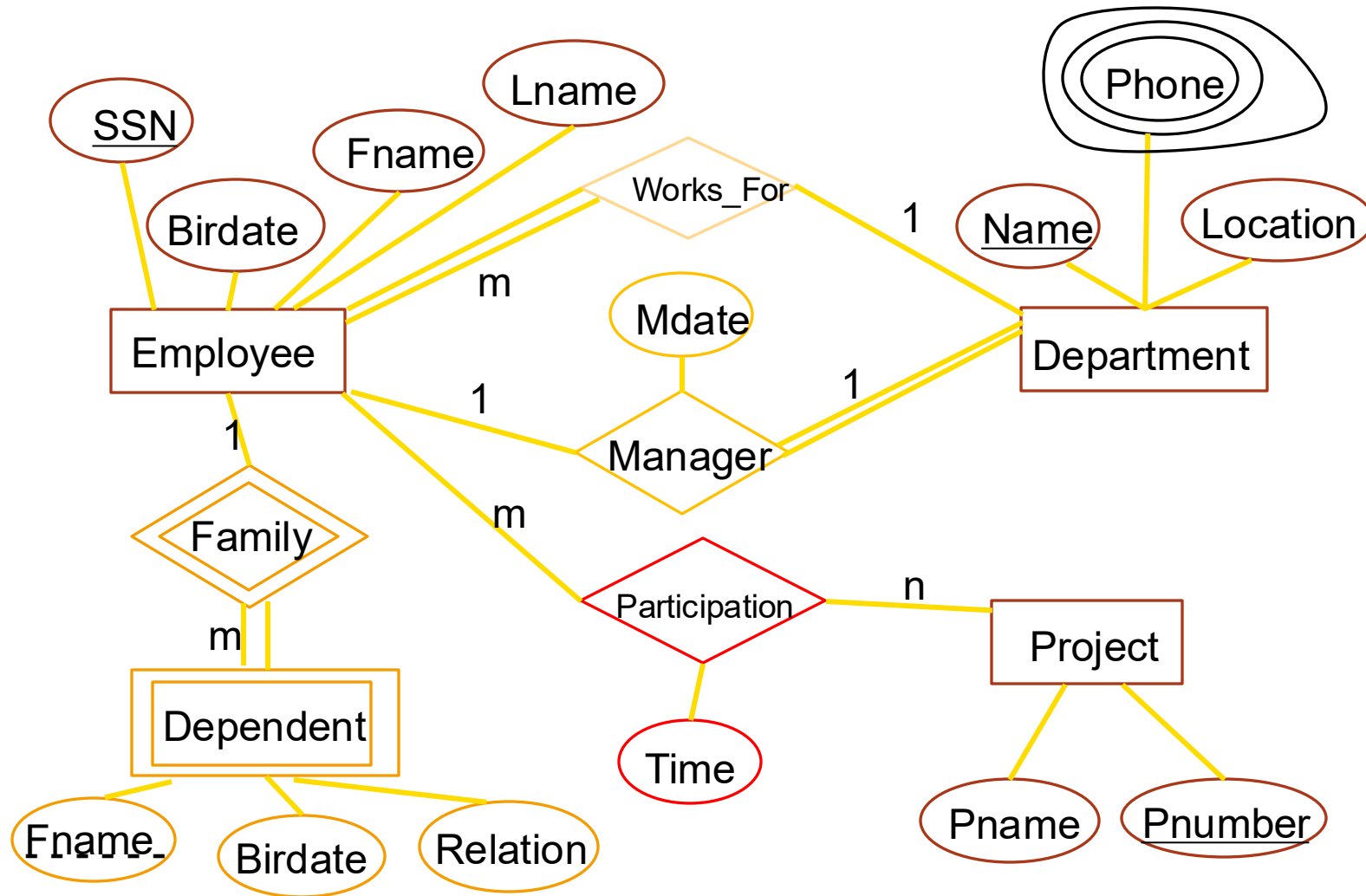
# Mapping Multivalued Attributes

Step 6: For each ***multivalued attribute*** A, where A is an attribute of E, create a new relation R.

- *If A is a multivalued simple attribute,*
  - Attributes of R = Simple attribute A, and key of E as a foreign key.
- *If A is a multivalued composite attribute,*
  - Attributes of R = All simple components of A, and key of E as a foreign key.

In both cases, the primary key of R is the set of all attributes in R.

# Mapping Multivalued Attributes



## Employee

<u>SSN</u>	Fname	Lname	Birdate	Dname
------------	-------	-------	---------	-------

## Department

<u>Name</u>	Location	MSSN	Msdate
-------------	----------	------	--------

## Project

<u>Pnumber</u>	Pname
----------------	-------

## Dependent

<u>SSN</u>	<u>Fname</u>	Birdate	Relation
------------	--------------	---------	----------

## Participation

<u>Pnumber</u>	<u>ESSN</u>	Time
----------------	-------------	------

## D\_number

<u>Dname</u>	<u>Dnumber</u>
--------------	----------------

# Mapping N-ary Relationship Types

Step 7: For each ***N-ary relationship type*** ( $n > 2$ ), create a new relation with

- Attributes: same as Step 5.
- Key: same as Step 5

*(Advice: binary relationships are simpler to model.)*

# Summary of Mapping

- Map Entities first
  - Strong Entity Types (Step 1)
  - Weak Entity Types (Step 2)
- Map Relationship
  - 1:1 Relationship Types (Step 3)
  - 1:N Relationship Types (Step 4)
  - M:N Relationship Types (Step 5)
  - N-ary Relationship Types (Step 7)
- Mapping
  - Multivalued Attributes (Step 6)

# ER vs Relational Model

ER MODEL	RELATIONAL MODEL
Entity Type	<i>Entity</i> relation
1:1 or 1:N relationship type	Foreign key (or <i>relationship</i> relation)
M:N relationship type	<i>Relationship</i> relation and two foreign key
<i>n</i> -ary relationship type	<i>Relationship</i> relation and <i>n</i> foreign key
Simple Attribute	Attribute
Composite Attribute	Set of simple component attributes
Multivalued Attribute	Relation and foreign key



# Takeaway

## Learning Outcomes

1. An understanding of relational model.
2. Knowing how to convert an ERD to relational model.