

Supporting information for “Beyond strain release: Delocalization-enabled organic reactivity

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Contents

S1 Computational methods	S2
S2 Linear free energy and geometric relationships	S3
S3 Hydrocarbon ring-opening reactivity	S6
S4 Heterocycle ring-opening reactivity	S13
S5 Tabulated strain release energies and delocalization values	S15
S6 ‘Rule of thumb’ worked example	S16
S7 Azide-alkyne (3+2) cycloaddition reactivity	S26
S8 References	S28

S1 Computational methods

All energies and thermodynamic quantities reported in this work were obtained using ORCA (v. 4.2.1).¹ Minima and transition states (TSs) were initially identified using *autodE* (v. 1.0.0b3),² with low energy conformers located using the ETKDGv2 algorithm implemented in RDKit v. 2019.03.4,³ and optimised using GFN2-xTB implemented in xTB (v 6.2.2)⁴ followed by PBE0-D3BJ/def2-TZVP//PBE0-D3BJ/def2-SVP in ORCA (v. 4.2.1).^{1,5,6} Anionic reactions were run using the GBSA⁷ / CPCM⁸ solvent models for THF in xTB / ORCA, respectively. Geometries and energy were then refined in ORCA at the [DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP] level of theory (CH_3^\bullet reactions) or [SMD(THF)-DLPNO-CCSD(T)/ma-def2-QZVPP (TightPNO)// SMD(THF)-B2PLYP-D3BJ/def2-TZVP (ma-def2-TZVP on N)] level of theory (NH_2^- reactions).^{5,6,9,10} All calculations used the resolution of the identity approximation (RIJCOSX),¹¹ with the appropriate auxiliary basis sets.¹² ‘Tight’ optimisation criteria (10^{-8} Ha tolerance for SCF, 10^{-6} Ha tolerance for optimisation step) were employed along with Grid6 / GridX6, corresponding to a Lebedev-590 angular grid, and a radial integral accuracy (IntAcc) of 5.34. Stationary points for the model systems were characterised through calculation of the Hessian. Minima were characterised by the absence of imaginary frequencies, and TSs by the presence of a single imaginary mode. Grimme’s quasi-RRHO method¹³ was used to calculate entropic corrections to obtain free energies at 298.15 K as implemented in the Python package *otherm*.¹⁴ For reactions calculated in the gas phase, a 1 atm standard state was employed. For reactions in implicit solvent, a 1 atm to 1 M standard state correction was applied by adding $RT \ln(24.5) = 1.89 \text{ kcal mol}^{-1}$ to the calculated free energy of each species. NBO occupation numbers were calculated using the NBO program (v. 7.0), and ELF descriptors were calculated with Multiwfn (v. 3.6).¹⁵

All data processing was carried out using the Scikit-learn package in Python 3.7,¹⁶ and MLR plots were generated with Matplotlib.¹⁷ A Python script to generate plots is included as part of the Supporting Information. Individual figures can be generated interactively, or to plot all figures using the terminal run:

```
for i in {1..20}; do echo $i | python main.py -v; done
```

Enthalpies were chosen for a direct comparison with strain energies, which are commonly reported instead of Gibbs free energies. Trends in enthalpy and Gibbs free energy were found to be in excellent agreement for all reactions studied here. Values of $2 - N_{occ}$ were found to be in good agreement with an alternative density-based delocalization parameter, $\frac{D_\sigma}{D_\sigma^0}$, which was evaluated at the bond critical point (Fig. S3).¹⁸

S2 Linear free energy and geometric relationships

Activation barrier prediction

The Marcus equation for a chemical reaction is given by eq 1, where ΔE^\ddagger is the activation barrier for a given reaction and ΔE_{int}^\ddagger is the intrinsic activation barrier in the absence of a driving force ($\Delta E_r = 0$).

$$\Delta E^\ddagger = \Delta E_{int}^\ddagger + \frac{1}{2}\Delta E_r + \frac{\Delta E_r^2}{16\Delta E_{int}^\ddagger} \quad (1)$$

For two similar reactions with equal driving force, according to eq 1 any difference in their activation barriers will be described by the difference in their intrinsic activation barriers, $\Delta\Delta E_{int}^\ddagger$:

$$\Delta\Delta E^\ddagger = \Delta\Delta E_{int}^\ddagger \quad (2)$$

Combining equations 1 and 2, we arrive at a variant of the Marcus model that accounts for the effect of varying both the reaction driving force (through ΔE_r) and the intrinsic activation barrier (through ΔE_{int}^\ddagger) on the observed activation energy (eq 3), relative to a reference intrinsic reaction barrier $\Delta E_{int}^\ddagger(0)$, where $\Delta E_{int}^\ddagger = \Delta E_{int}^\ddagger(0) + \Delta\Delta E_{int}^\ddagger$. The sensitivity of ΔE^\ddagger toward variation in the driving force and intrinsic activation barrier are given by equations 4a and 4b, respectively.

$$\Delta E^\ddagger = \Delta E_{int}^\ddagger(0) + \frac{1}{2}\Delta E_r + \frac{1}{16} \frac{\Delta E_r^2}{\Delta E_{int}^\ddagger(0) + \Delta\Delta E_{int}^\ddagger} + \Delta\Delta E_{int}^\ddagger \quad (3)$$

$$\left(\frac{\partial \Delta E^\ddagger}{\partial \Delta E_r} \right)_{\Delta\Delta E_{int}^\ddagger} = \frac{1}{2} + \frac{1}{8} \left(\frac{\Delta E_r}{\Delta E_{int}^\ddagger(0) + \Delta\Delta E_{int}^\ddagger} \right) \quad (4a)$$

$$\left(\frac{\partial \Delta E^\ddagger}{\partial \Delta\Delta E_{int}^\ddagger} \right)_{\Delta E_r} = 1 - \frac{1}{16} \left(\frac{\Delta E_r}{\Delta E_{int}^\ddagger(0) + \Delta\Delta E_{int}^\ddagger} \right)^2 \quad (4b)$$

While the value of $\Delta\Delta E_{int}^\ddagger$ is a priori unknown, we can replace it with a calculated parameter that captures the physical origin of the change in ΔE_{int}^\ddagger for the range of systems of interest. For example, in the context of small ring reactivity, we propose that a more delocalized bond will be associated with a lower intrinsic activation barrier; in other words, it will be inherently easier to break a more delocalized bond. We can formulate a linear free energy relationship (eq 5) based on this hypothesis in which we use the parameterization

$\Delta\Delta E_{int}^\ddagger = \kappa\chi$, where χ is a variable that captures bond delocalization (vide infra) and κ is a proportionality constant that gives $\kappa\chi$ the units of energy. The sensitivity constants defined in equations 4a and 4b are replaced by fitting parameters α and β , respectively, where κ has been absorbed into the β parameter. An increase in driving force is expected to decrease ΔE^\ddagger ($\alpha > 0$), and an increase in bond delocalization is also predicted to decrease ΔE^\ddagger ($\beta > 0$). These parameters may be found by MLR using a Bell-Evans-Polanyi-type approximation, through which ΔE_r and $\Delta\Delta E_{int}^\ddagger$ are assumed to be uncorrelated. The quality of this assumption can be assessed through deviation of α and β from $\frac{1}{2}$ and κ , respectively.

$$\Delta E^\ddagger = \Delta E_{int}^\ddagger(0) + \alpha\Delta E_r + \beta\chi \quad (5)$$

Transition state geometry prediction

We may derive an equation to predict the extension of a breaking bond from its equilibrium value to that found at the TS as follows:

The equations of two parabolas, E_1 and E_2 , that describe the diabatic potential energy surfaces of a reaction are given by

$$E_1 = \frac{1}{2}kr^2 \quad (6a)$$

$$E_2 = \frac{1}{2}k(r - r')^2 + \Delta E_r \quad (6b)$$

where k is the force constant associated with the stretch of each bond, r is the length of the breaking bond, r' is the hypothetical length at which the breaking bond is fully cleaved, and ΔE_r is the reaction driving force. The x coordinate of the intersection point of the two parabolas (Δr^\ddagger), representing the position of the TS, is given by

$$\Delta r^\ddagger = \frac{1}{2}r' + \frac{\Delta E_r}{kr'} \quad (7)$$

Using a Marcus-type approach, we can define $\frac{1}{2}r'$ as the intrinsic TS bond extension (Δr_{int}^\ddagger), for a symmetrical TS in which $\Delta E_r = 0$ such that eq 7 becomes

$$\Delta r^\ddagger = \Delta r_{int}^\ddagger + \frac{\Delta E_r}{2k\Delta r_{int}^\ddagger} \quad (8)$$

This equation represents a Bell-Evans-Polanyi-like equation for the prediction of TS geometric parameters using knowledge of only the reaction driving force, the force constant associated with the breaking bond, and the intrinsic bond extension.

To enable examination of the effect of varying Δr_{int}^\ddagger on Δr^\ddagger , we may use the substitution $\Delta r_{int}^\ddagger = \Delta r_{int}^\ddagger(0) + \Delta\Delta r_{int}^\ddagger$, resulting in eq 9, where $\Delta r_{int}^\ddagger(0)$ is the intrinsic TS bond extension for $\Delta E_r = 0$ and $\Delta\Delta r_{int}^\ddagger = 0$. Partial derivatives with respect to ΔE_r (fixed Δr_{int}^\ddagger) and Δr_{int}^\ddagger (fixed ΔE_r) give the sensitivity of Δr^\ddagger toward changes in driving force (eq 10a) and intrinsic bond extension (eq 10b), respectively.

$$\Delta r^\ddagger = \Delta r_{int}^\ddagger(0) + \frac{1}{2k} \frac{\Delta E_r}{\Delta r_{int}^\ddagger(0) + \Delta\Delta r_{int}^\ddagger} + \Delta\Delta r_{int}^\ddagger \quad (9)$$

$$\left(\frac{\partial \Delta r^\ddagger}{\partial \Delta E_r} \right)_{\Delta\Delta r_{int}^\ddagger} = \frac{1}{2k} \left(\frac{1}{\Delta r_{int}^\ddagger(0) + \Delta\Delta r_{int}^\ddagger} \right) \quad (10a)$$

$$\left(\frac{\partial \Delta r^\ddagger}{\partial \Delta\Delta r_{int}^\ddagger} \right)_{\Delta E_r} = 1 - \frac{1}{2k} \left(\frac{\Delta E_r}{(\Delta r_{int}^\ddagger(0) + \Delta\Delta r_{int}^\ddagger)^2} \right) \quad (10b)$$

Since $\Delta\Delta r_{int}^\ddagger$ is *a priori* unknown, we can replace it with a calculated parameter, in the same way as for the prediction of TS barriers in eq 5. For example, to investigate the role of bond delocalization on TS geometry, we can formulate a linear geometric relationship, first using the parameterization $\Delta\Delta r_{int}^\ddagger = \lambda\chi$, where χ has the same meaning as before, and λ is a proportionality constant that gives $\lambda\chi$ the units of distance. Second, the sensitivity constants defined in equations 10a and 10b may be replaced by fitting parameters γ and δ , respectively, where λ has been absorbed into the δ parameter. An increase in driving force is expected to decrease Δr^\ddagger ($\gamma > 0$), and an increase in bond delocalization is also predicted to decrease Δr^\ddagger ($\delta > 0$). As before, we may find these parameters using MLR, where we again make a Bell-Evans-Polanyi-type approximation through which ΔE_r and $\Delta\Delta r_{int}^\ddagger$ are assumed to be uncorrelated. The quality of this assumption can be assessed through deviation of γ and δ from $(2k\Delta r_{int}^\ddagger(0))^{-1}$ and λ , respectively.

$$\Delta r^\ddagger = \Delta r_{int}^\ddagger(0) + \gamma\Delta E_r + \delta\chi \quad (11)$$

A value of $k = 474.4 \text{ kcal mol}^{-1} \text{ \AA}^{-2}$ is obtained from a plot of ΔH^\ddagger vs $(\Delta r^\ddagger)^2$, and assuming $\Delta r_{int}^\ddagger(0) = 0.438 \text{ \AA}$ for the intrinsic bond extension of ethane, a value of $(2k\Delta r_{int}^\ddagger(0))^{-1} = 0.0024 \text{ mol kcal}^{-1}$ is obtained – in satisfactory agreement with the value of γ ($0.0017 \text{ mol kcal}^{-1}$) from MLR.

S3 Hydrocarbon ring-opening reactivity

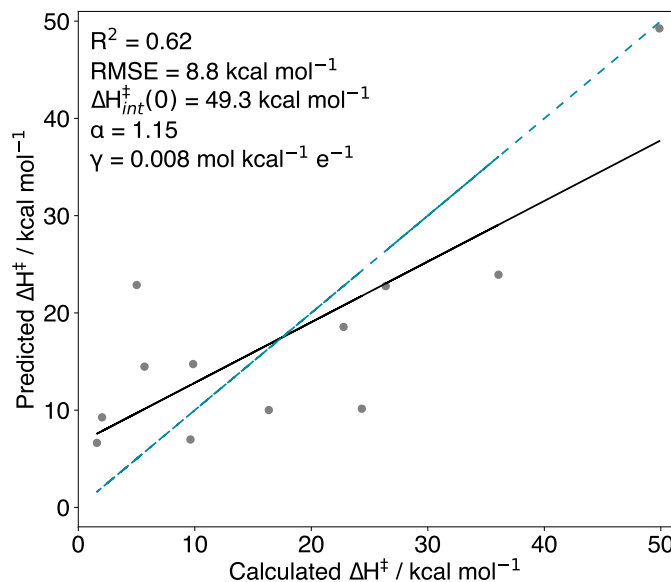


Figure S1: MLR plot ($\text{CH}_3^\bullet + \text{hydrocarbon}$) for the prediction of ΔH^\ddagger from ΔH_r and ΔH_r^2 (Marcus) using $\Delta H^\ddagger = \Delta H_{int}^\ddagger + \alpha \Delta H_r + \beta \Delta H_r^2$, where α and β are optimised coefficients. The blue dashed line denotes perfect correlation.

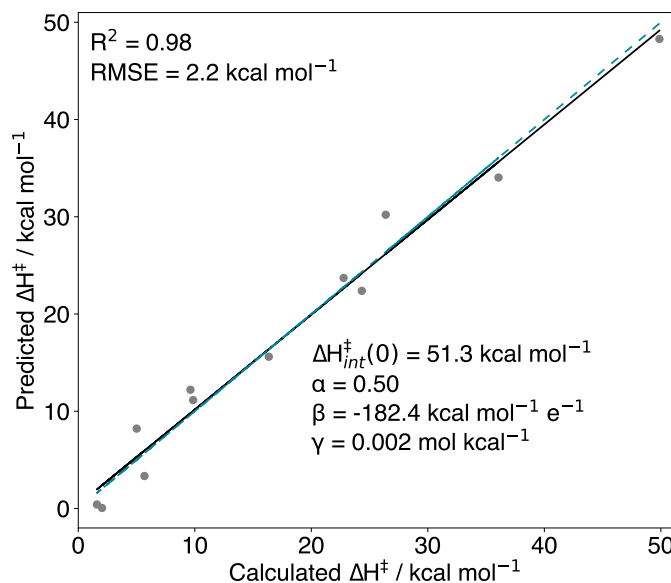


Figure S2: MLR plot ($\text{CH}_3^\bullet + \text{hydrocarbon}$) for the prediction of ΔH^\ddagger from ΔH_r , ΔH_r^2 and $2 - N_{occ}$ (Marcus + delocalization) using $\Delta H^\ddagger = \Delta H_{int}^\ddagger + \alpha \Delta H_r + \beta(2 - N_{occ}) + \gamma \Delta H_r^2$, where α , β and γ are optimised coefficients. The blue dashed line denotes perfect correlation.

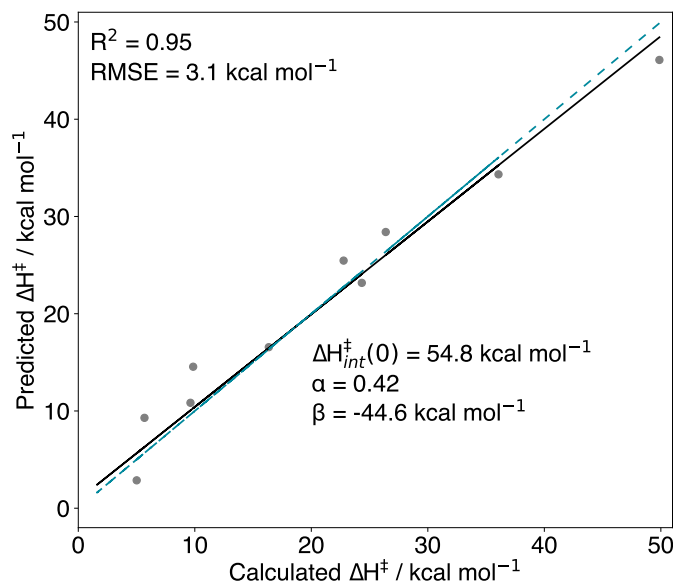


Figure S3: MLR plot ($\text{CH}_3^\bullet + \text{hydrocarbon}$) for the prediction of ΔH^\ddagger from ΔH_r and $\frac{D_\sigma}{D_\sigma^0}$ using $\Delta H^\ddagger = \Delta H_{\text{int}}^\ddagger + \alpha \Delta H_r + \beta \frac{D_\sigma}{D_\sigma^0}$, where α and β are optimised coefficients. The blue dashed line denotes perfect correlation.

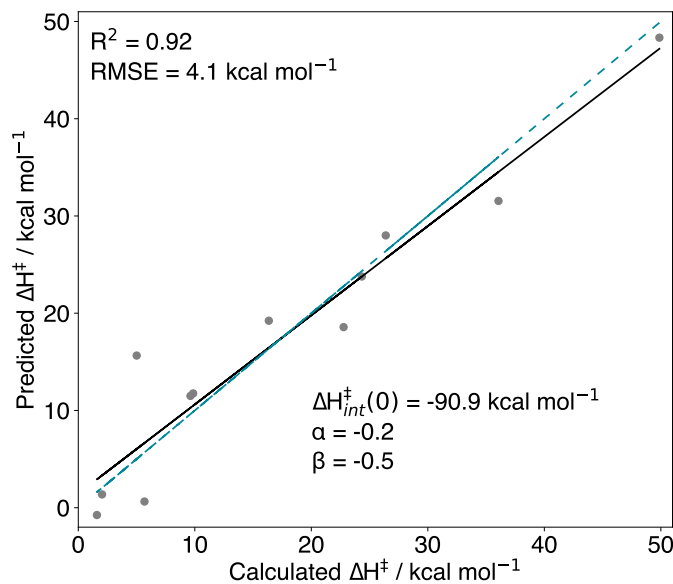


Figure S4: MLR plot ($\text{CH}_3^\bullet + \text{hydrocarbon}$) for the prediction of ΔH^\ddagger from ΔH_r and E_{HOMO} using $\Delta H^\ddagger = \Delta H_{\text{int}}^\ddagger + \alpha \Delta H_r + \beta E_{\text{HOMO}}$, where α and β are optimised coefficients. The blue dashed line denotes perfect correlation.

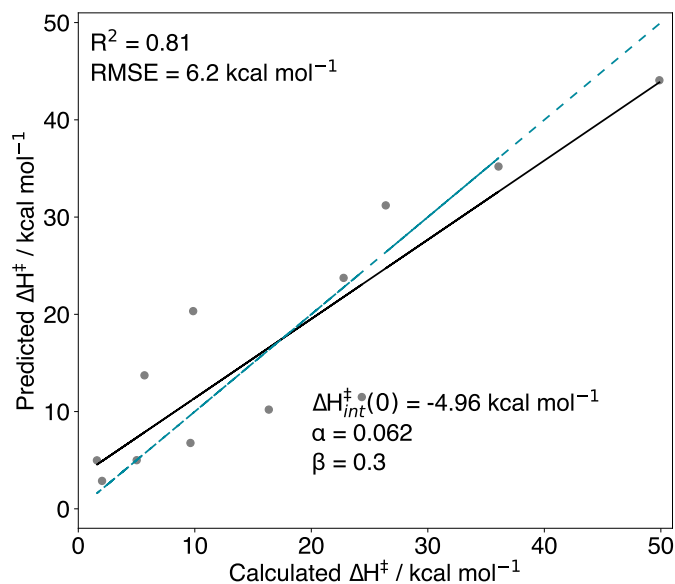


Figure S5: MLR plot ($\text{CH}_3^\bullet + \text{hydrocarbon}$) for the prediction of ΔH^\ddagger from ΔH_r and E_{LUMO} using $\Delta H^\ddagger = \Delta H^\ddagger_{\text{int}} + \alpha \Delta H_r + \beta E_{LUMO}$, where α and β are optimised coefficients. The blue dashed line denotes perfect correlation.

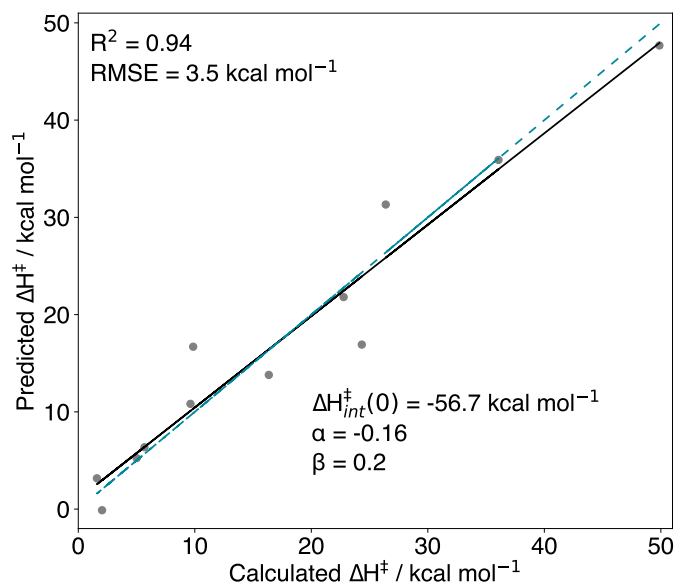


Figure S6: MLR plot ($\text{CH}_3^\bullet + \text{hydrocarbon}$) for the prediction of ΔH^\ddagger from ΔH_r and $\Delta E_{HOMO-LUMO}$ using $\Delta H^\ddagger = \Delta H^\ddagger_{\text{int}} + \alpha \Delta H_r + \beta \Delta E_{HOMO-LUMO}$, where α and β are optimised coefficients. The blue dashed line denotes perfect correlation.

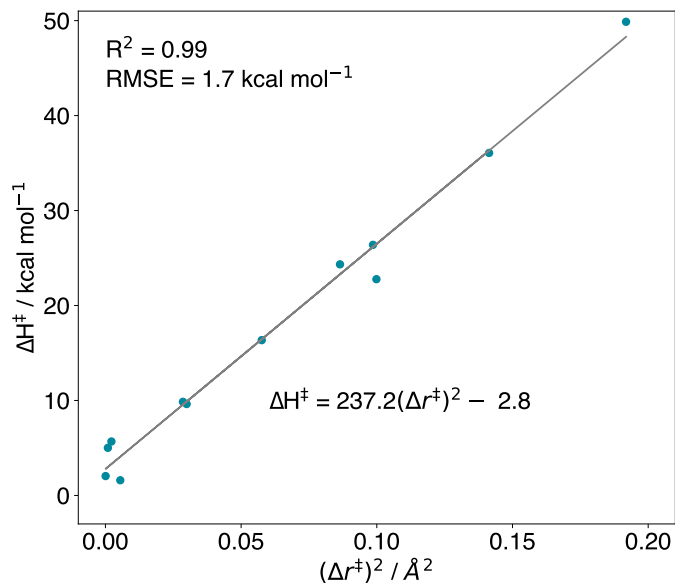


Figure S7: Prediction of ΔH^\ddagger from the TS bond extension, Δr^\ddagger , where $\Delta r^\ddagger = r^\ddagger - r_0$. Bond lengths in \AA , energies in kcal mol^{-1} .

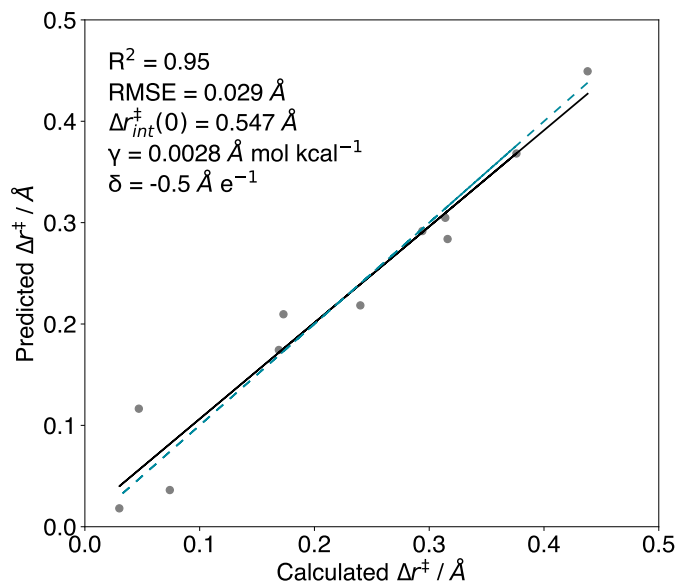


Figure S8: Prediction of Δr^\ddagger from ΔH_r and $\frac{D_\sigma}{D_\sigma^0}$ using . The blue dashed line denotes perfect correlation.

CCl ₃ [•] addition		B2PLYP-D3BJ					DLPNO-CCSD(T)		
		ΔE_{el}	ΔZPE	ΔH	$T\Delta S$	ΔG	ΔE	ΔH	ΔG
[1.1.1]Propellane, H	vdW complex	-2.7	0.3	-1.5	-10.5	9.1	-1.6	-0.4	10.2
	TS	-1.0	0.3	-0.6	-12.2	11.6	0.1	0.5	12.8
	rxn	-25.8	2.2	-24.0	-13.8	-10.2	-26.6	-24.8	-11.0
Bicyclo[1.1.0]butane, D	vdW complex	-2.9	0.4	-1.7	-9.9	8.3	-2.2	-0.9	9.0
	TS	2.5	0.3	2.8	-12.2	15.0	3.6	4.0	16.2
	rxn	-40.3	1.4	-39.0	-12.9	-26.1	-41.4	-40.1	-27.2
Bicyclo[2.1.0]pentane, E	vdW complex	-3.3	0.4	-2.1	-10.6	8.5	-2.5	-1.3	9.3
	TS	8.8	-0.1	8.8	-12.4	21.3	10.6	10.7	23.2
	rxn	-51.3	1.6	-49.8	-13.1	-36.7	-51.7	-50.2	-37.1

Table S1: Differences in thermodynamic quantities (kcal mol⁻¹) for the addition of CCl₃[•] to [1.1.1]propellane (**H**), bicyclo[1.1.0]butane (**D**) and bicyclo[2.1.0]pentane (**E**), optimised at the B2PLYP-D3BJ/def2-TZVP level, with single point energies calculated at the DLPNO-CCSD(T)/ma-def2-QZVPP (TightPNO) level. ΔH and ΔG at the DLPNO-CCSD(T) level calculated using thermal corrections from the B2PLYP level.

CH ₃ [•] addition		B2PLYP-D3BJ				ΔG	DLPNO-CCSD(T)		
		ΔE_{el}	ΔZPE	ΔH	$T\Delta S$		ΔE	ΔH	ΔG
Ethane, A	TS	49.2	1.2	49.5	-10.4	59.9	49.7	49.9	60.3
	rxn	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
Cyclopropane, B	TS	25.2	1.6	25.9	-10.5	36.5	25.7	26.4	36.9
	rxn	-31.2	3.8	-28.3	-10.7	-17.7	-31.2	-28.4	-17.7
Cyclobutane, C	TS	35.1	1.6	35.7	-11.0	46.6	35.5	36.1	47.0
	rxn	-30.1	3.1	-27.5	-9.8	-17.7	-29.4	-26.8	-16.9
Bicyclo[1.1.0]butane, D	TS	7.8	1.9	8.9	-10.5	19.4	8.8	9.9	20.4
	rxn	-45.2	4.6	-41.8	-11.2	-30.6	-45.0	-41.6	-30.3
Bicyclo[2.1.0]pentane, E	TS	14.4	1.6	15.3	-10.6	25.9	15.5	16.4	27.0
	rxn	-57.3	4.8	-53.6	-11.4	-42.2	-56.5	-52.9	-41.4
Bicyclo[3.1.0]hexane, F	TS	21.0	2.0	22.0	-11.3	33.4	21.7	22.8	34.1
	rxn	-38.9	4.8	-35.3	15.4	-23.5	-38.3	-34.7	-23.0
Bicyclo[2.2.0]hexane, G	TS	22.8	1.8	23.6	-11.1	34.8	23.5	24.3	35.5
	rxn	-57.9	5.5	-53.7	-11.9	-41.8	-56.7	-52.4	-40.5
[1.1.1]Propellane, H	TS	2.9	1.7	3.9	-10.3	14.1	4.0	5.0	15.3
	rxn	-32.4	5.5	-28.4	-12.2	-16.2	-32.2	-28.2	-16.0
[2.1.1]Propellane, I	TS	0.3	1.4	1.2	-9.9	11.1	1.1	2.0	12.0
	rxn	-59.7	6.2	-55.1	-12.6	-42.5	-59.8	-55.3	-42.7
[3.1.1]Propellane, J	TS	3.4	1.8	4.4	-10.7	15.2	4.7	5.7	16.4
	rxn	-46.2	5.9	-41.9	-12.4	-29.5	-46.4	-42.1	-29.7
[2.2.1]Propellane, K	TS	-0.4	1.4	0.5	-10.2	10.6	0.7	1.6	11.8
	rxn	-83.5	7.1	-78.2	-12.9	-65.3	-83.8	-78.5	-65.6
[2.2.2]Propellane, L	TS	7.2	1.8	8.1	-11.1	19.3	8.6	9.6	20.8
	rxn	-88.6	7.8	-82.5	-13.1	-69.4	-88.1	-82.1	-69.0

Table S2: Differences in thermodynamic quantities (kcal mol⁻¹) for the addition of a methyl radical to each of the molecules in the H12 set, optimised at the B2PLYP-D3BJ/def2-TZVP level, with single point energies calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO) level. ΔH and ΔG at the DLPNO-CCSD(T) level calculated using thermal corrections from the B2PLYP level.

NH ₂ ⁻ addition		B2PLYP-D3BJ				ΔG	DLPNO-CCSD(T)		
		ΔE_{el}	ΔZPE	ΔH	$T\Delta S$		ΔE	ΔH	ΔG
Ethane, A	TS	66.2	-1.5	64.4	-8.1	72.5	68.5	66.7	74.8
	rxn	24.5	-0.2	24.3	0.8	23.5	22.4	22.3	21.4
Cyclopropane, B	TS	40.1	-0.3	39.3	-8.8	48.2	41.3	40.6	49.4
	rxn	1.7	3.3	4.1	-9.9	14.0	-2.2	0.2	10.0
Cyclobutane, C	TS	48.4	-0.2	47.5	-9.6	57.1	50.3	49.5	59.0
	rxn	3.8	2.8	6.0	-9.3	15.2	1.0	3.2	12.4
Bicyclo[1.1.0]butane, D	TS	19.7	1.2	20.2	-9.4	29.6	20.9	21.4	30.7
	rxn	-11.1	4.6	-8.0	-11.1	3.1	-15.2	-12.1	-1.0
Bicyclo[2.1.0]pentane, E	TS	27.2	-0.1	26.8	-9.0	35.8	29.0	28.6	37.6
	rxn	-18.4	4.4	-15.4	-11.0	-4.4	-21.2	-18.2	-7.2
Bicyclo[3.1.0]hexane, F	TS	36.4	-0.2	35.7	-9.4	45.1	39.3	38.7	48.0
	rxn	-3.5	4.0	-0.9	-11.5	10.6	-6.1	-3.5	8.0
Bicyclo[2.2.0]hexane, G	TS	32.6	0.4	32.4	-9.7	42.0	34.8	34.6	44.3
	rxn	-14.9	4.4	-11.7	-10.9	-0.8	-17.5	-14.3	-3.4
[1.1.1]Propellane, H	TS	12.1	1.0	12.4	-9.5	21.9	12.9	13.2	22.7
	rxn	-9.0	3.9	-6.5	-11.3	4.7	-13.1	-10.7	0.6
[2.1.1]Propellane, I	TS	6.5	1.0	6.9	-9.4	16.3	7.0	7.5	16.8
	rxn	-32.7	4.7	-29.6	-11.7	-18.0	-37.2	-34.1	-22.4
[3.1.1]Propellane, J	TS	17.0	0.8	17.1	-9.8	26.9	18.1	18.2	28.1
	rxn	-10.4	4.1	-7.7	-11.3	3.6	-14.9	-12.2	-0.9
[2.2.1]Propellane, K	TS	5.2	1.0	5.8	-9.0	14.8	6.0	6.6	15.6
	rxn	-54.1	5.7	-50.2	-12.1	-38.1	-58.2	-54.3	-42.2
[2.2.2]Propellane, L	TS	19.0	0.7	19.1	-9.8	28.8	21.1	21.2	30.9
	rxn	-54.5	6.1	-50.1	-12.0	-38.1	-57.0	-52.6	-40.7

Table S3: Differences in thermodynamic quantities (kcal mol⁻¹) for the addition of an amide anion (NH₂⁻) to each of the molecules in the H12 set, optimised at the SMD(THF)-B2PLYP-D3BJ/def2-TZVP (ma-def2-TZVP on N) level, with single point energies calculated at the SMD(THF)-DLPNO-CCSD(T)/ma-def2-QZVPP (TightPNO) level. ΔH and ΔG at the DLPNO-CCSD(T) level calculated using thermal corrections from the B2PLYP level.

S4 Heterocycle ring-opening reactivity

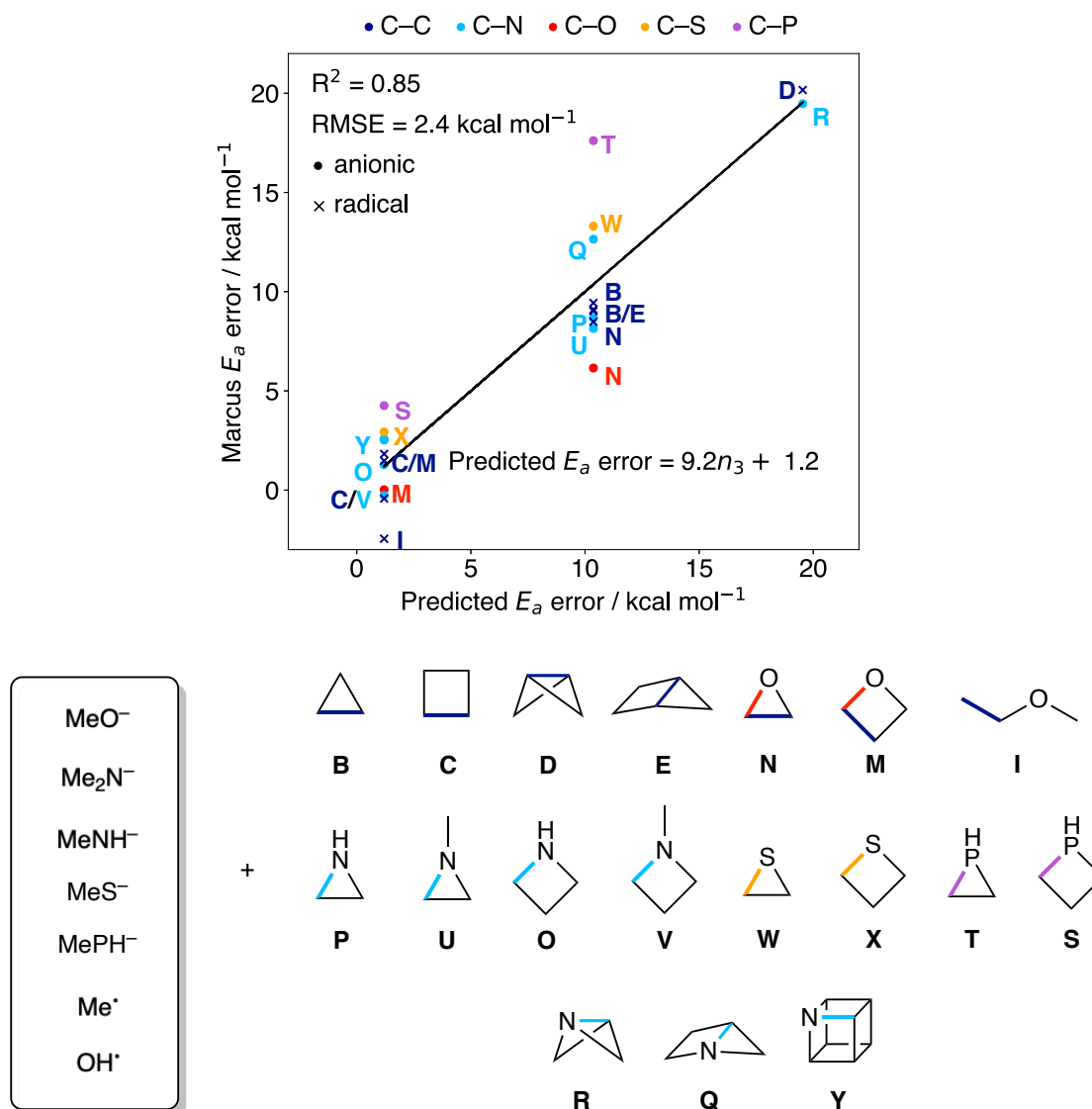


Figure S9: Anionic and radical additions to a set of 18 heterocyclic molecules (Fig. S10, and the error in activation energy (E_a) predicted by Marcus theory vs $2 - N_{occ}$. Reaction data from refs. [19, 20].

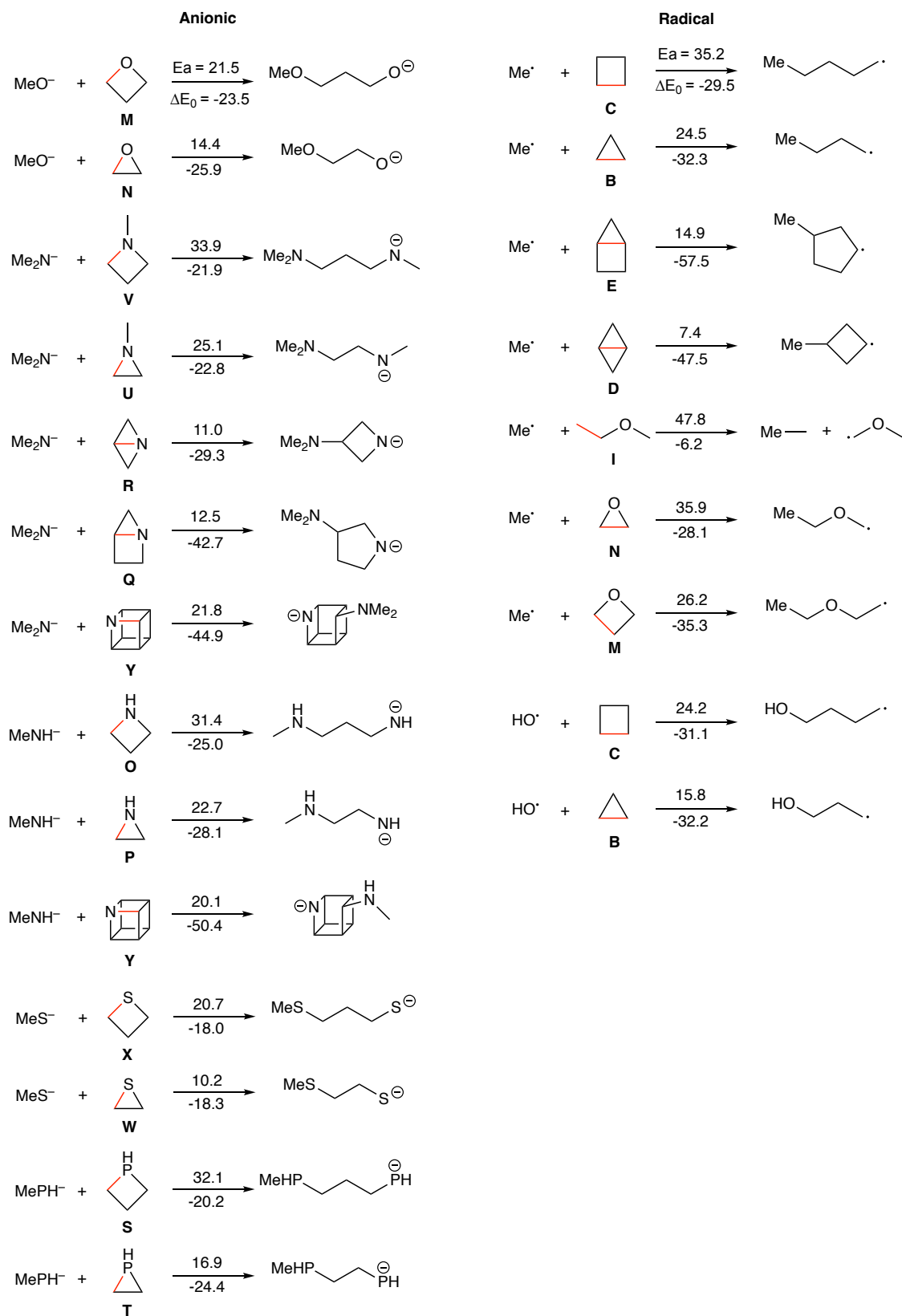
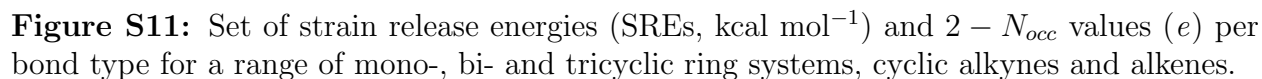


Figure S10: Anionic and radical reactions used to generate Fig. S9, with data taken from refs. [19, 20].

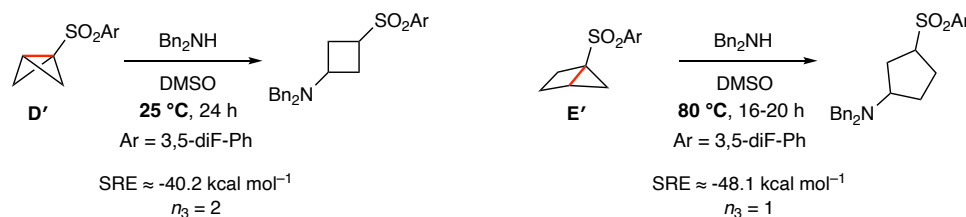
Example balanced reactions: _____



S6 ‘Rule of thumb’ worked example

Shown in Fig. 5d, and reproduced here, is the addition of Bn_2NH to a sulfonyl bicyclo[1.1.0]butane (**D'**) or bicyclo[2.1.0]pentane (**E'**). While the former reaction takes place at 25 °C (298 K), the latter requires heating to 80 °C (353 K).

‘Strain-release’ amination (ref. 48 in main text)



Using the ‘rule of thumb’ of $\Delta\Delta H^\ddagger \approx 0.5\Delta\text{SRE} - 10\Delta n_3$, for these reactions $\Delta\text{SRE} = -7.9 \text{ kcal mol}^{-1}$ and $\Delta n_3 = -1$. Based on strain release alone, **E'** should have an activation enthalpy $\approx 4 \text{ kcal mol}^{-1}$ lower than **D'** – therefore a reaction rate $\approx 10^3$ times greater than **D'** at 298 K. However, barrier lowering due to three-membered ring delocalization should independently lower the intrinsic barrier for **D'** by $\approx 10 \text{ kcal mol}^{-1}$ relative to **E'**. The net effect is a prediction of a $\approx 6 \text{ kcal mol}^{-1}$ lower enthalpic barrier to the reaction for **D'** than **E'**, with delocalization overturning the strain release bias.

Based on the experimental data, we can roughly estimate the relative reaction rates for the two reactions at a given temperature ($k_{\text{rel}} = k_{\text{D}'}(T)/k_{\text{E}'}(T)$) using the Eyring equation, if we assume that the experimental conditions are identical except for changes in temperature, that the two mechanisms are identical, and that the reactions occur at identical rates at the two different temperatures used in the reactions (*i.e.*, $k_{\text{D}'}(T)/k_{\text{E}'}(T') = 1$).

Using the latter condition, the relationship between the free energy barriers of the two reactions and the two reaction temperatures is

$$\Delta G_{\text{E}'}^\ddagger = \frac{T'}{T} \Delta G_{\text{D}'}^\ddagger + RT' \ln \frac{T'}{T}$$

where R is the gas constant. Using $T'/T = 1.2$, we obtain $\Delta G_{\text{E}'}^\ddagger = 1.2\Delta G_{\text{D}'}^\ddagger + 0.1 \text{ kcal mol}^{-1}$. Based on the reported reaction time of 24 h for **D'** at 298 K, we can estimate a value of $\Delta G_{\text{D}'}^\ddagger \approx 24 \text{ kcal mol}^{-1}$ ($t_{1/2} = 12 \text{ h}$). The resulting estimate for $\Delta G_{\text{E}'}^\ddagger$ is then 29 kcal mol^{-1} – therefore the free energy barrier is $\approx 5 \text{ kcal mol}^{-1}$ lower for **D'** than **E'**, a difference of only 1 kcal mol^{-1} from the rule of thumb prediction. Despite completely neglecting entropic effects and avoiding any electronic structure calculations or experiments, the rule of thumb gives a good estimate of the expected reactivity difference based only on tabulated data and visual inspection.

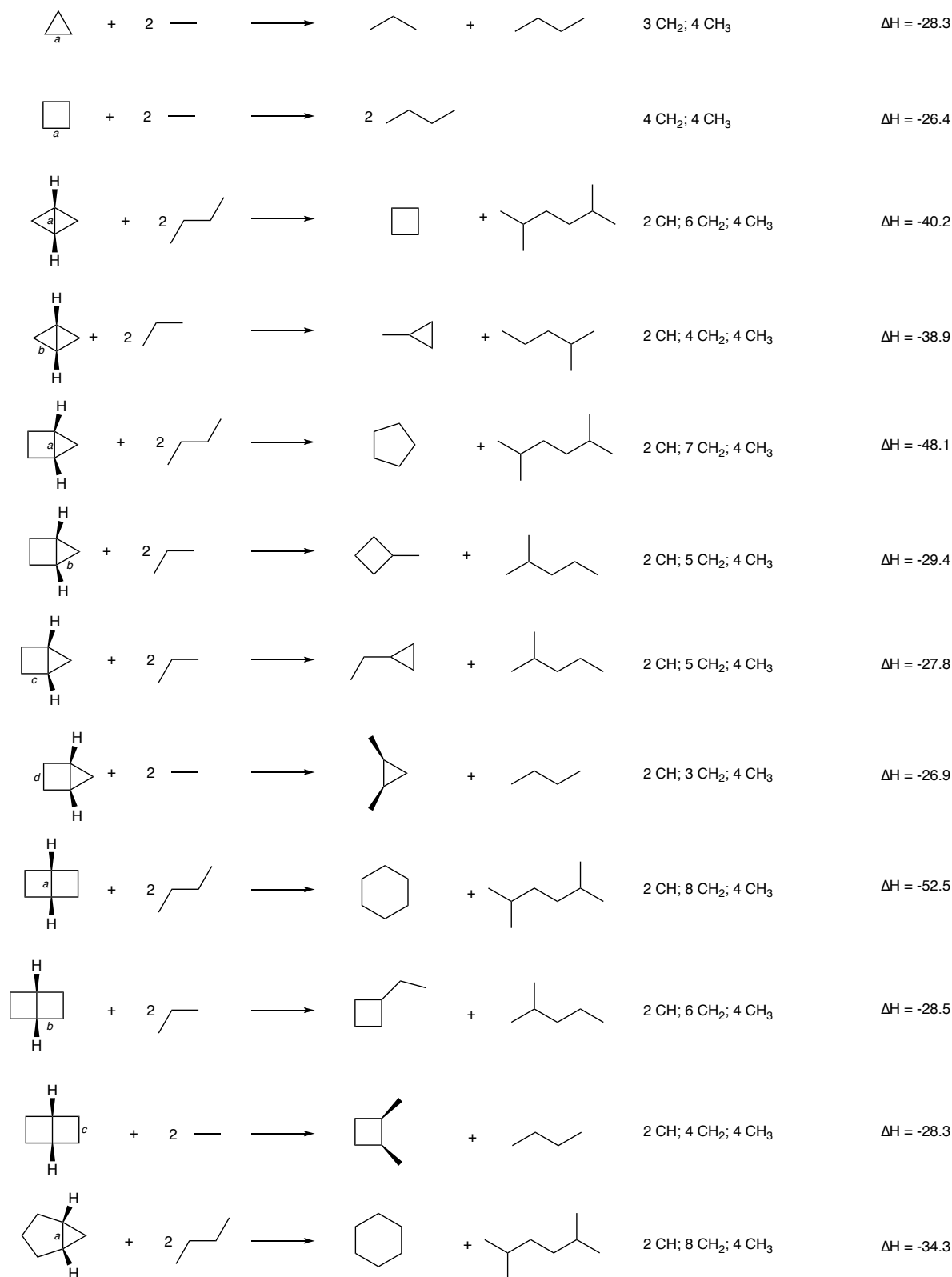


Figure S12: Balanced hydrogen transfer reactions by bond type, group classifications and reaction enthalpies (kcal mol⁻¹) calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level.

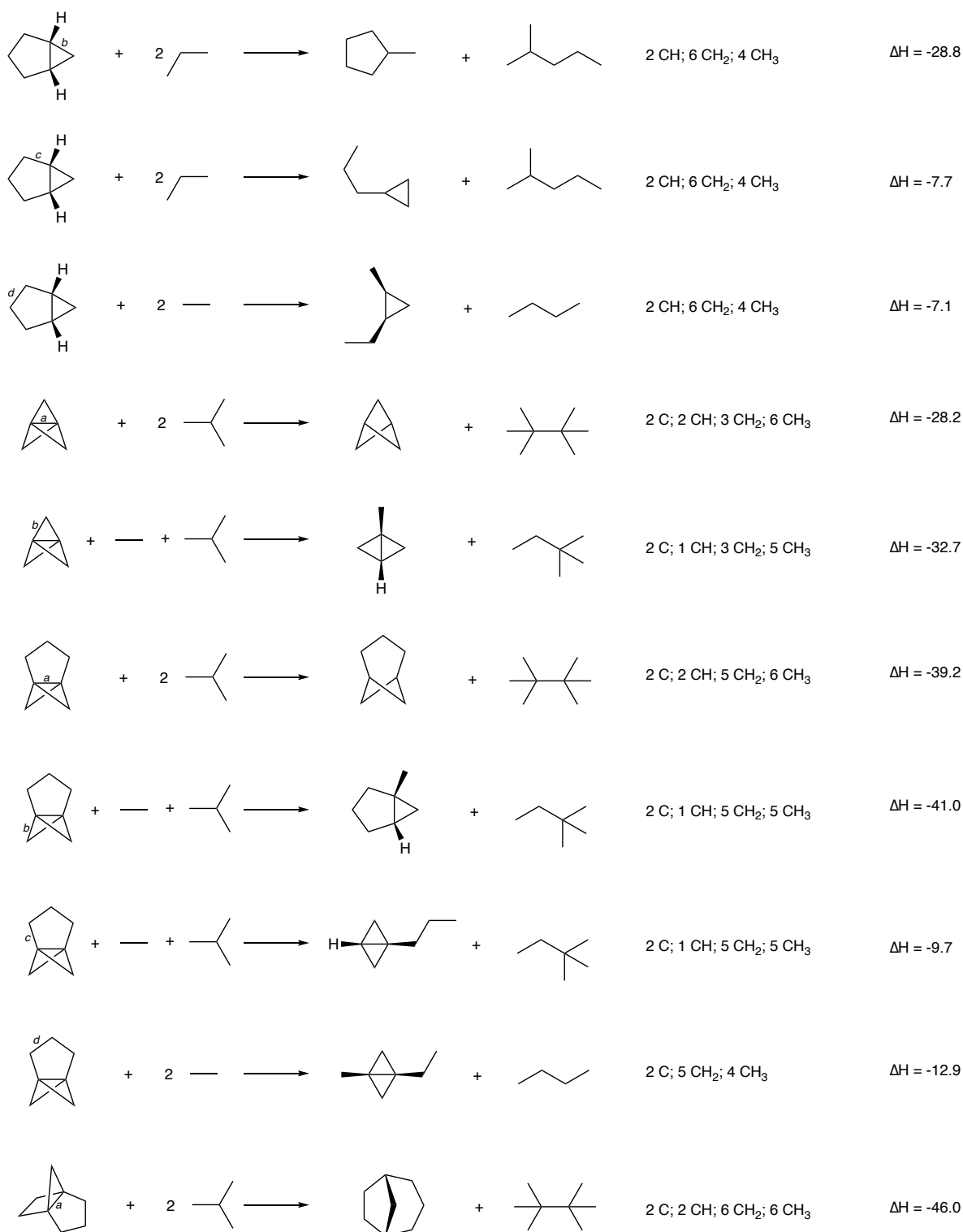


Figure S13: Balanced hydrogen transfer reactions by bond type, group classifications and reaction enthalpies (kcal mol⁻¹) calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level.

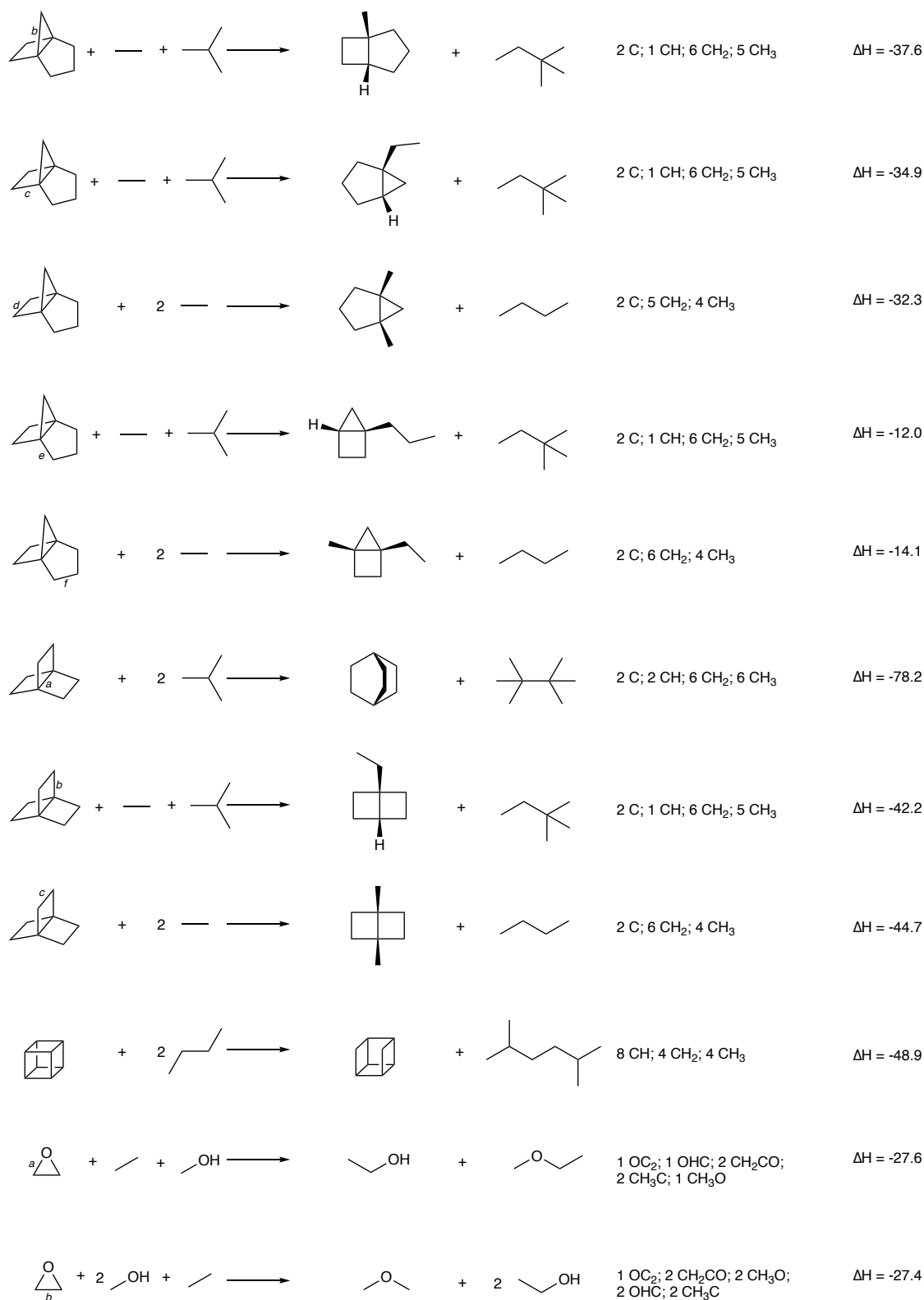


Figure S14: Balanced hydrogen transfer reactions by bond type, group classifications and reaction enthalpies (kcal mol⁻¹) calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level.

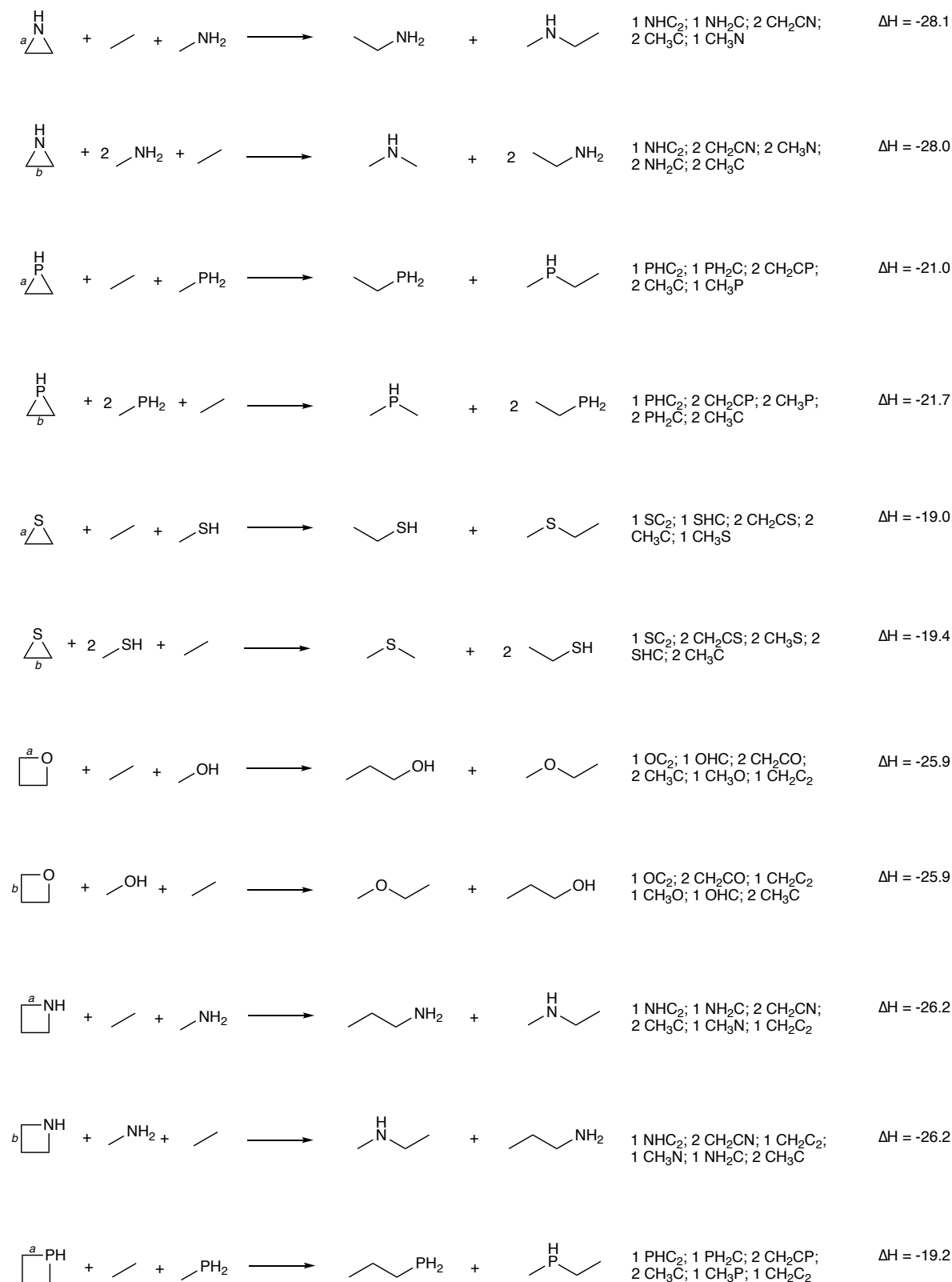


Figure S15: Balanced hydrogen transfer reactions by bond type, group classifications and reaction enthalpies (kcal mol⁻¹) calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level.

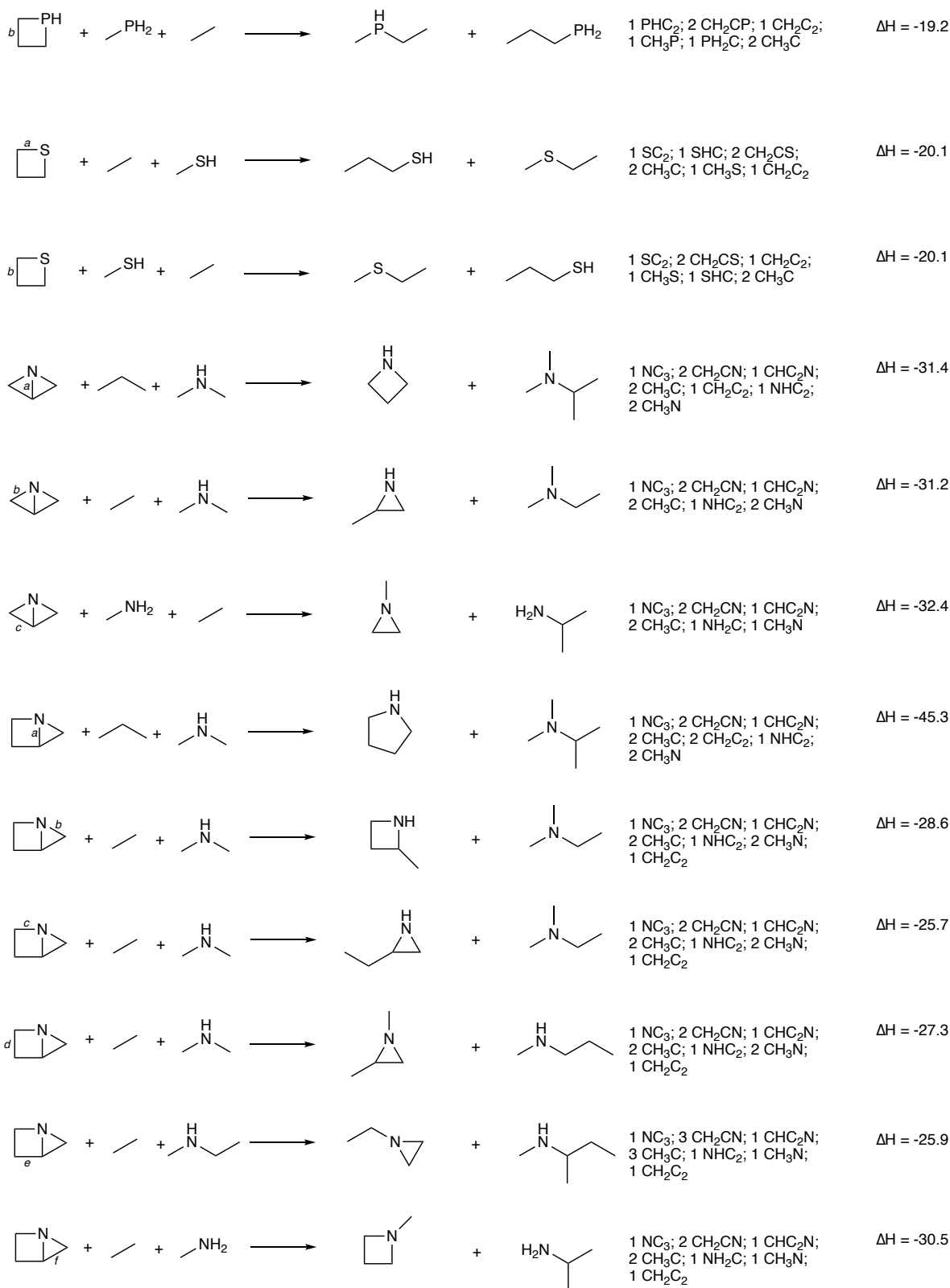


Figure S16: Balanced hydrogen transfer reactions by bond type, group classifications and reaction enthalpies (kcal mol⁻¹) calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level.

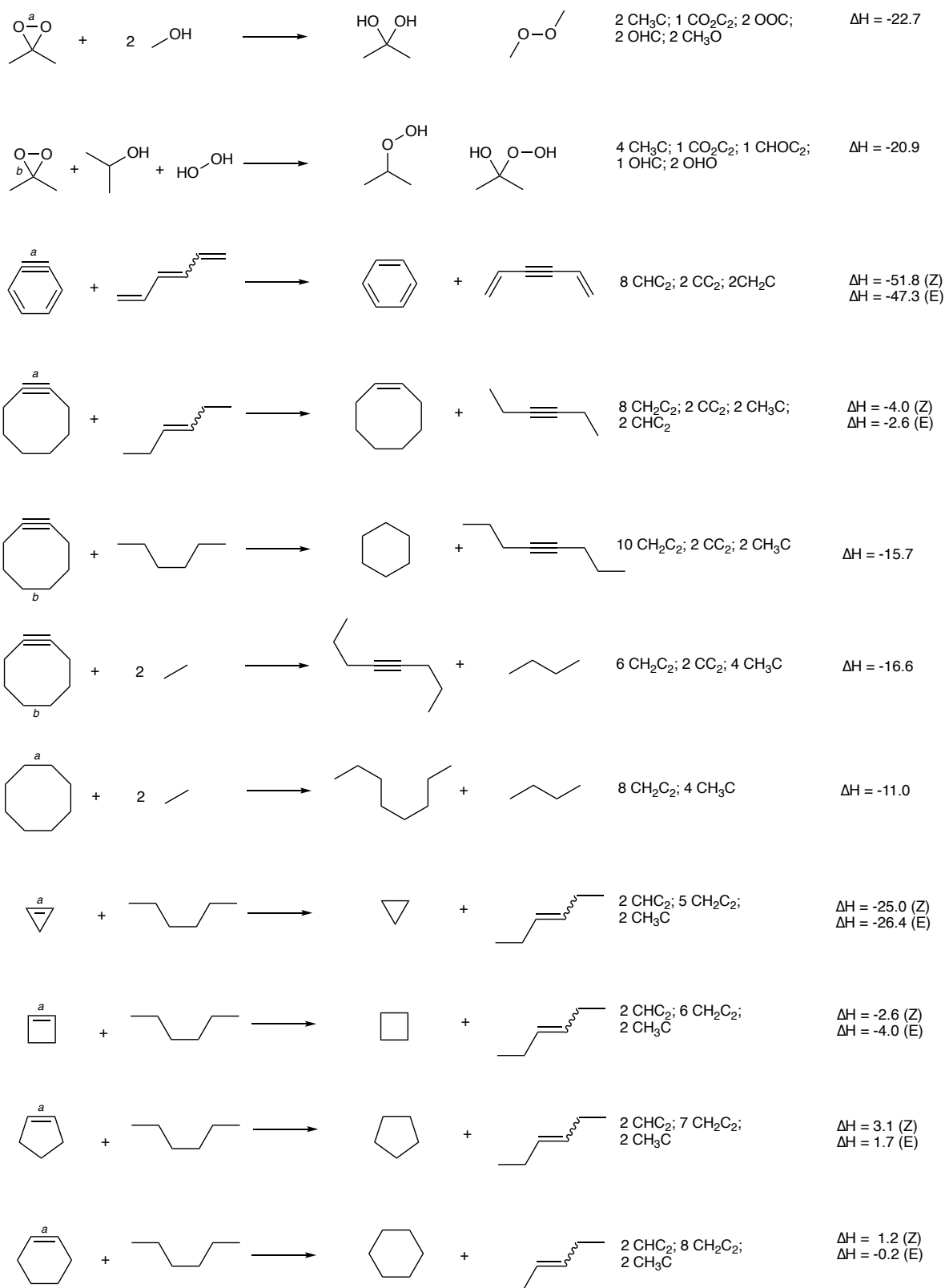


Figure S17: Balanced hydrogen transfer reactions by bond type, group classifications and reaction enthalpies (kcal mol⁻¹) calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level.

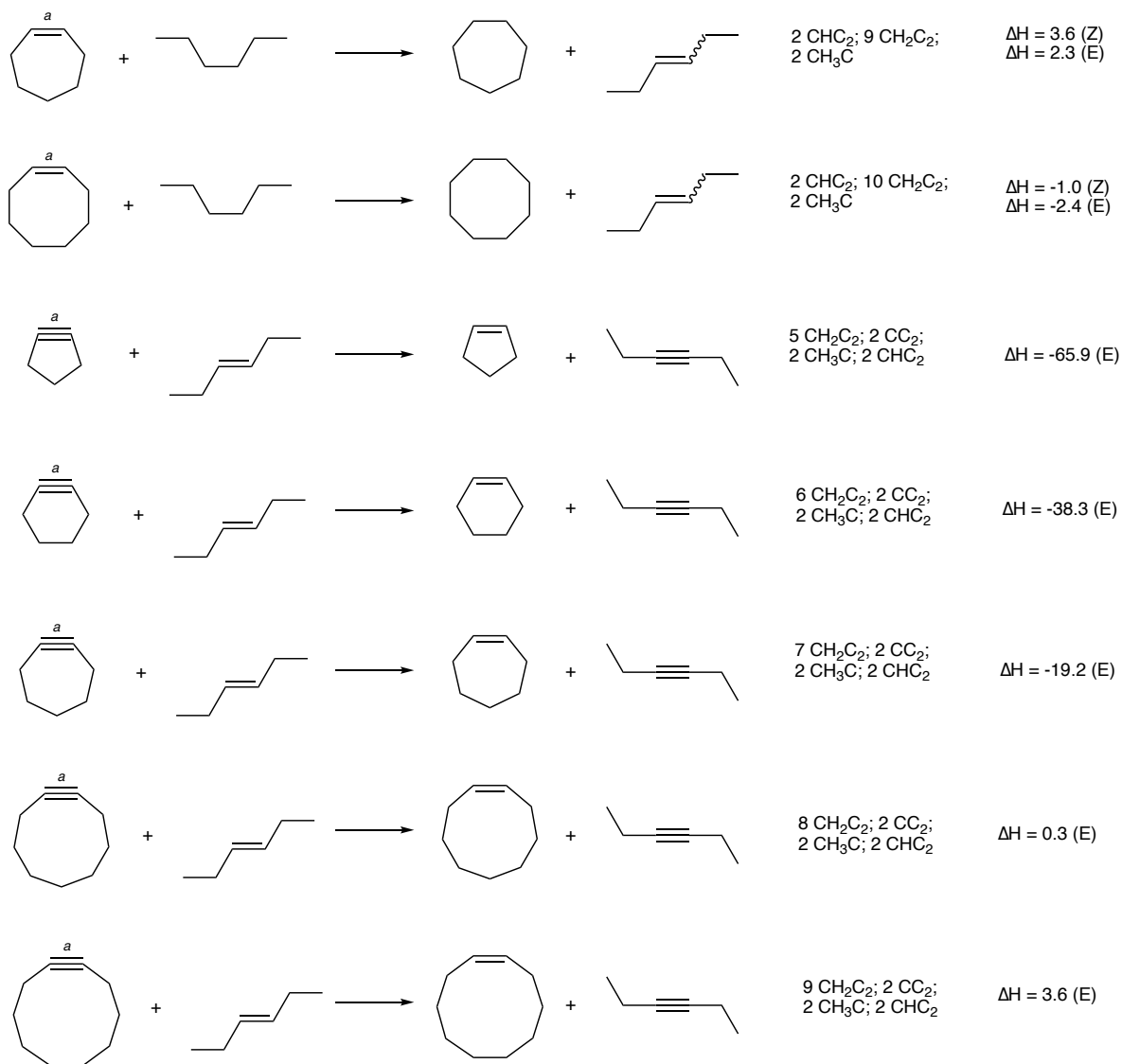


Figure S18: Balanced hydrogen transfer reactions by bond type, group classifications and reaction enthalpies (kcal mol^{-1}) calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level.

Molecule	Strain release energy (bond ‘a’) / kcal mol ⁻¹			
	This work	Rablen 2020 ²¹	Wiberg 1986 ²²	L&G 1976 ²³
<i>ortho</i> -Benzyne	-51.8	—	—	-44
Cyclopentyne	-65.9	—	—	—
Cyclohexyne	-38.3	—	—	—
Cycloheptyne	-19.2	—	—	—
Cyclooctyne	-2.6	—	—	—
Cyclononyne	0.3	—	—	—
Cyclodecyne	3.6	—	—	—
Cyclopropene	-26.4	-26.3	-27.7	—
Cyclobutene	-4.0	-3.5	-1.9	—
Cyclopentene	1.7	2.1	2.1	—
Cyclohexene	-0.2	-1.5	0.3	—
Cycloheptene	2.3	—	2.7	—
Cyclooctene	-2.4	—	5.5	—

Table S4: Strain release energies (kcal mol⁻¹ for the type ‘a’ bonds (π) shown in Figures S5–S11, calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3bJ/def2-TZVP level (this work). Comparison is made with a variety of values from other sources using different computational methods.^{21–23}

Strain release energy (bond ‘a’) / kcal mol ⁻¹					
Molecule	This work	Rablen 2020 ²¹	Wiberg 1986 ²²	Morgan 2013 ²⁴	Expt
Cyclopropane	-28.3	-27.9	-27.5	—	-27.5 ^a / -27.6 ^b
Cyclobutane	-26.4	-26.8	-26.5	—	-26.5 ^a / -26.2 ^b
Bicyclo[1.1.0]butane	-40.2	-39.7	-37.4	—	-40.3 ^b
Bicyclo[2.1.0]pentane	-48.1	-48.1	-48.5	—	-50.8 ^b
Bicyclo[2.2.0]hexane	-52.5	-52.3	-51.8	—	-50.7 ^b
Bicyclo[3.1.0]hexane	-34.3	-30.6	-31.0	—	-33.9 ^b
[1.1.1]Propellane	-28.2	-32.3	-30.0	—	—
[3.1.1]Propellane	-39.2	—	—	—	—
[3.2.1]Propellane	-46.0	-46.0	—	—	—
[2.2.2]Propellane	-78.2	-82.3	-81.6	—	—
Cubane	-48.9	—	—	—	—
Oxirane	-27.6	—	—	-27.1	-27.4 ^a
Aziridine	-28.1	—	—	-27.5	-27.1 ^a
Epiphosphine	-21.0	—	—	-19.4	—
Episulfide	-19.0	—	—	-17.6	—
Oxetane	-25.9	—	—	—	—
Azetidine	-26.2	—	—	—	—
Phosphetane	-19.2	—	—	—	—
Thietane	-20.1	—	—	—	—
1-Azabicyclo[1.1.0]butane	-31.4	—	—	—	—
1-Azabicyclo[2.1.0]pentane	-45.3	—	—	—	—
Dimethyldioxirane	-22.7	—	—	—	—

^aTaken from ref. [24]. ^bTaken from ref. [23].

Table S5: Strain release energies (kcal mol⁻¹ for the type ‘a’ bonds (σ) shown in Figures S5–S11, calculated at the DLPNO-CCSD(T)/def2-QZVPP (TightPNO)//B2PLYP-D3BJ/def2-TZVP level (this work). Comparison is made with a variety of values from other sources using different computational or experimental methods.^{21–24}

S7 Azide-alkyne (3+2) cycloaddition reactivity

Alkyne	π NBO 1	π NBO 2	Mean π 2 - N_{occ}
Hex-3-yne	0.070	0.070	0.070
Cyclooctyne	0.076	0.078	0.077
F ₂ -Cyclooctyne	0.085	0.091	0.088
Dibenzocyclooctyne	0.088	0.166	0.127
Cycloheptyne	0.078	0.086	0.082
Cyclononyne	0.075	0.075	0.075
Cyclodecyne	0.073	0.075	0.074
Monobenzocyclooctyne	0.080	0.124	0.102
Distal monobenzocyclooctyne	0.078	0.085	0.082
N,S-Cyclooctyne	0.077	0.093	0.085

Table S6: delocalization values ($2 - N_{occ}$, in e) for the triple bonds of a selection of alkynes.

Alkyne		ΔE	ΔZPE	ΔH	$T\Delta S$	ΔG
Hex-3-yne	TS	18.3	0.7	18.5	-13.5	32.0
	rxn	-64.7	4.6	-61.5	-15.1	-46.4
Cyclooctyne	TS	9.2	0.6	9.5	-12.8	22.3
	rxn	-76.8	4.9	-73.2	-15.4	-57.8
F ₂ -Cyclooctyne, syn	TS	5.9	0.8	6.4	-12.9	19.3
	rxn	-78.5	5.2	-74.7	-15.6	-59.1
F ₂ -Cyclooctyne, anti	TS	8.4	0.7	8.8	-12.7	21.5
	rxn	-76.5	5.0	-72.8	-15.6	-57.2
Dibenzocyclooctyne	TS	5.8	0.9	6.4	-13.4	19.8
	rxn	-70.7	4.5	-67.3	-14.8	-52.5
Cycloheptyne	TS	4.1	0.7	4.5	-12.1	16.6
	rxn	-88.1	5.1	-84.4	-14.9	-69.5
Cyclononyne	TS	15.5	0.5	15.7	-12.5	28.3
	rxn	-68.8	4.7	-65.4	-14.9	-50.5
Cyclodecyne	TS	13.7	0.9	14.1	-13.3	27.4
	rxn	-66.9	5.0	-63.4	-15.7	-47.7
Monobenzocyclooctyne, syn	TS	8.2	0.7	8.6	-12.9	21.4
	rxn	-78.0	5.0	-74.4	-15.5	-58.9
Monobenzocyclooctyne, anti	TS	7.8	0.8	8.2	-13.0	21.2
	rxn	-76.9	4.7	-73.4	-15.1	-58.3
Distal monobenzocyclooctyne	TS	6.4	0.6	6.7	-12.5	19.2
	rxn	-75.2	4.9	-71.6	-14.8	-56.7
N,S-Cyclooctyne, anti	TS	8.8	0.5	9.1	-12.7	21.8
	rxn	-78.6	5.1	-75.0	-15.9	-59.1
N,S-Cyclooctyne, syn	TS	6.5	0.8	6.9	-13.5	20.4
	rxn	-78.8	5.1	-75.3	-16.4	-58.9

Table S7: Differences in thermodynamic quantities (kcal mol⁻¹) for the cycloaddition between methyl azide and a range of alkynes, at the B2PLYP-D3BJ/def2-TZVP level.

S8 References

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