

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time: Friday, March 17 2017 at 17:30
Duration: 2 hours
Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED
Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 16 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)5^{2k+1}} - 4 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)239^{2k+1}} = \left(\frac{16}{1 \cdot 5} - \frac{4}{1 \cdot 239} \right) - \left(\frac{16}{3 \cdot 5^3} - \frac{4}{3 \cdot 239^3} \right) + \left(\frac{16}{5 \cdot 5^5} - \frac{4}{5 \cdot 239^5} \right) - \dots$$

The initial value of `float compensation` is `0.0`.

```
double Sum (int [], int Size) {
    double array-Sum = 0;
    for (int i=0; i < Size; i++) {
        array-Sum += a[i];
    }
    return array-Sum;
}

int main() {
    for (int i=0; i < 20; i++)
        cin >> a[i];
    cout << Sum(a, 20);
    return 0;
}
```

Use the backside, if needed

```
float pi(int n) {
```

1

Problem 1 of 4

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Section, Name and ID#:

Problem 2: Write a Java method `public static double[] expReg(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the exponent of an exponential regression and the second element being the amplitude. The exponential regression approximates the data points by a formula

$$y = a e^{mx},$$

where the exponent m and the amplitude a are computed as

$$m = \frac{\overline{xy} - \bar{x}\bar{y}}{\bar{x}^2 - \bar{x}^2}, a = \bar{y} - m\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the natural logarithm of y coordinates, \bar{x}^2 is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and natural logarithm of y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. For natural logarithm, use the method `double Math.log()`.

Both result elements are zeros, if at least one data element is non-positive.

```
public static double[] expReg(double[] data) {
    double result = new double[] {0, 0};
    double xy = 0, x2 = 0, y = 0, x = 0;
    for (x = 0; x < data.length; x++) for (int i = 0; i < data.length; i++) {
        if (data[i] <= 0)
            return new double[] {0, 0};
        x += 1;
        y += Math.log(data[i]);
        xy += i * Math.log(data[i]);
        x2 += i * i;
    }
    x /= data.length;
    y /= data.length;
    xy /= data.length;
    x2 /= data.length;
    result[0] = (xy - x * y) / (x2 - Math.pow(x, 2));
    result[1] = y - result[0] * x;
    return result;
}
```

Use the backside, if needed

Problem 2 of 4

COP.MT-170317.L032

Section, Name and ID#:

Problem 3: Write a Java function `public static boolean isInside(double[][] vertex, double x, double y)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row, and `double x` and `double y` coordinates of a point. It checks, if the point is inside the polygon.

Assume and use a method `boolean toLeft(double x1, double y1, double x2, double y2, double x0, double y0)` that takes as its arguments coordinates of three points and returns `true`, if the third point (x_0, y_0) is in the left-hand side, when moving from the first point (x_1, y_1) to the second one (x_2, y_2) ; and `false`, if it is in the right-hand side.

```
public boolean isInside(double[][] vertex, double x, double y) {  
    int
```

```
    for (int i = 0; i < vertex.length; i++) {
```

```
        for (int j = 0; j < vertex[i].length; j++) {
```

```
            for (int k = 0; k < vertex[i].length; k++) {
```

```
                if (length(i, m, n, l) {
```

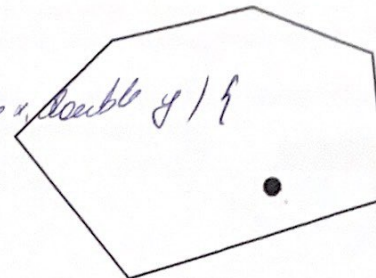
```
                    if (y1) {
```

```
                        return true
```

```
                    } else {
```

```
                        return false
```

```
                }  
            }  
        }  
    }
```



if our point
is in left side of
line or right then
it is inside else
it is outside
the polygon.

Problem 4: Write a Java method `public static void magicOdd(int[][] square)` that creates a magic square of an *odd* size using the following algorithm:

1. The number 1 goes in the middle of the top row;
2. All numbers are then placed one *column to the right* and one *row up* from the previous number;
3. Whenever the next number placement is above the top row, stay in the same column and place the number in the bottom row (note the place of 2 instead of the shaded location);
4. Whenever the next number placement is outside of the rightmost column, stay in the same row and place the number in the leftmost column (note the place of 3 instead of the shaded location);
5. When encountering an already filled-in square, place the next number directly below the previous number;
6. When the next number position is outside both a row and a column, place the number directly beneath the previous number (note the place of 7 instead of the shaded location).

`public static void magicOdd(int[][] square)`

	9	2	7
8	1	6	3
3	5	7	4
4	9	2	

1
 to take the place for 1
 and then continue to fill our
 magic square. we write
 function which will start from
 initial point then go column
 to the right and one row up ^(col++ row--)
 then repeat the same step
 for next number, but if
 our step is outside of the
 rightmost column then fill leftmost
 column being in the same row.
 and with a for loop repeat
 this situation until fill
 all empty spaces