

Section, Name and ID#

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED
Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1}{2} * \frac{2}{3} + \frac{1*3}{2*4} * \frac{2}{5} + \frac{1*3*5}{2*4*6} * \frac{2}{7} + \dots$$

Recall that $n!!$ is the product of odd numbers from 1 to n , if n is odd; and is the product of even numbers from 2 to n , if n is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

Another problem.

create a function that takes as an argument a matrix of any size and returns the (row, col) of the left upper corner of the region 5×5 that has the greatest number of 1s.

```
public static int getMax(int[][] mat, int sc, int sr) { // sc-starting column, sr-start. row
    int count = 0;
    for (int row = sr; row < sr+4; row++) {
        for (int col = sc; col < sc+4; col++) {
            if (mat[row][col] == 1) {
                count++;
            }
        }
    }
    return count;
}
```

```
if (sc < 0 || sr < 0 || sc+4 > mat.length || sr+4 > mat.length) {
```

```
    return 0;
}
```

Use the backside, if needed

Problem 1 of 4

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```
int maximum = 0;
```

```
int mr = 0;
```

```
int mc = 0;
```

// mr, mc - the coord. of the upper left region
that has the greatest num of ones

```
for (int r = 0; r < mat.length; r++) {
```

```
    for (int c = 0; c < mat.length; c++) {
```

```
        int count = getNum(mat, r, c);
```

```
        if (count >= maximum) {
```

```
            maximum = count;
```

```
            mr = r;
```

```
            mc = c;
```

```
        }  
    }  
}
```

```
System.out.print(mr + " " + mc);
```

2

Section, Name and ID#:

Problem 2: Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope k and the intercept b are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the y coordinates, $\overline{x^2}$ is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. You may assume and use the method `double mean(double[] a)`.

```
public static double[] lin(double[] data) {
    double[] result = new double[2];
    double[] xs = new double[data.length];
    for (int i = 0; i < data.length; i++) {
        xs[i] = i;
    }
    double meanX, meanY, meanPr, meanXsq, k, b;
    meanX = mean(xs);
    meanY = mean(data);
    for (int i = 0; i < data.length; i++) {
        productxy[i] = i * data[i];
        xsq[i] = i * i;
    }
    meanPr = mean(productxy);
    meanXsq = mean(xsq);
    k = (meanPr - meanX * meanY) / (meanXsq - meanX * meanX);
    b = meanY - k * meanX;
    result[0] = k;
    result[1] = b;
    return result;
}
```

[2, 4, 7, 6]

`double[] xsq = new double[data.length];`
`double[] productxy = new double[data.length];`

Use the backside, if needed

Problem 2 of 4

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Section, Name and ID#:

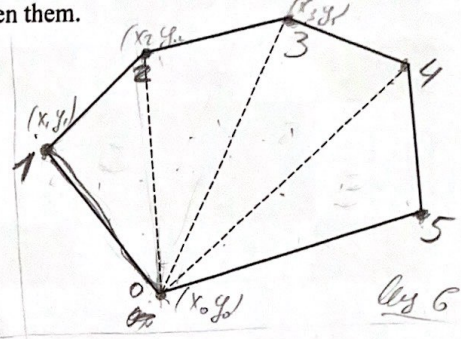
$x_1, x_2, x_3, \dots, x_n$
 $y_1, y_2, y_3, \dots, y_n$

Problem 3: Write a Java function `public static double area(double[][] vertex)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` - the x coordinates in the first row and y coordinates in the second row. It returns polygon's area as follows:

1. Divides the polygon into triangles by connecting the first vertex with the n^{th} and $(n+1)^{st}$ vertices;
2. Adds the areas of the constructed triangles using the formula $area = \sqrt{p(p-a)(p-b)(p-c)}$, where a, b and c are the sides and $p = (a + b + c) / 2$.

You may assume and use a method `double dist(double x1, double y1, double x2, double y2)` that takes as its arguments coordinates of two points and returns the distance between them.

```
public static double area(double[][] vertex) {
    double area = 0;
    double a = 0;
    double b = 0;
    double c = 0;
```



```
    for (int i = 0; i < vertex.length - 2; i++) {
        double a = dist(vertex[0][0], vertex[i][0], vertex[0][i], vertex[i][i]);
        double b = dist(vertex[0][0], vertex[i][0], vertex[0][i+2], vertex[i][i+2]);
        double c = dist(vertex[0][i], vertex[i][i], vertex[0][i+2], vertex[i][i+2]);
        double p = (a + b + c) / 2;
        area += sqrt(p * (p - a) * (p - b) * (p - c));
    }
    return area;
```

// use library for computing the square root or create a function called sqrt

4

Section, Name and ID#:

Problem 4: Write a Java method `public static void magic4N(int[][] square)` that creates a magic square of a $4N$ -by- $4N$ size using the following algorithm:

1. Creates an array of the same size as `int[][] square` and fills it forward with successive integers assigning 1 to the top-left element;
2. Creates another array of the same size as `int[][] square` and fills it backward with successive integers assigning 1 to the bottom-right element;
3. Divides the original `int[][] square` into 16 blocks of the same size – 4 blocks per row and column. In the on-diagonal (shaded) blocks copies the elements from the first array, and in the off-diagonal blocks copies the elements from second array.

0	1	2					7	8
1	9	10					15	16
2			19	20	21	22		
3			27	28	29	30		
4			35	36	37	38		
5			43	44	45	46		
6	49	50					55	56
7	57	58					63	64

		62	61	60	59		
		54	53	52	51		
48	47					42	41
40	39					34	33
32	31					26	25
24	23					18	17
		14	13	12	11		
		6	5	4	3		

```

public static void magic4N(int[][] square) {
    int[][] arrf = new int[square.length][square.length]; int value = 1;
    while(value <= square.length * square.length) {
        for(int row = 0; row < arrf.length; row++) {
            for(int col = 0; col < arrf[0].length; col++) {
                arrf[row][col] = value;
                value++;
            }
        }
        int[][] arrb = new int[square.length][square.length];
        int value1 = square.length * square.length;
        while(value1 > 0) {
            for(int row = 0; row < arrb.length; row++) {
                for(int col = 0; col < arrb[0].length; col++) {
                    arrb[row][col] = value1;
                    value1--;
                }
            }
        }
    }
}

```

2

I did not notice 4 by 4, so I wrote for general case. :)

Use the backside, if needed

Problem 4 of 4

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