

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1}{2} * \frac{2}{3} + \frac{1*3}{2*4} * \frac{2}{5} + \frac{1*3*5}{2*4*6} * \frac{2}{7} + \dots$$

Recall that $n!!$ is the product of odd numbers from 1 to n , if n is odd; and is the product of even numbers from 2 to n , if n is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

Use the backside, if needed

Problem 1 of 4

```
float pi(int n) {
    double a = 1.0;
    double b = 1.0;
    double c = 0.0;
    for (int i = 0; i <= n; i++) {
        for (int j = 1; j <= n; j++) {
            if (j % 2 != 0) {
                b = b * j;
            }
            if (j % 2 == 0) {
                c = c * j;
            }
        }
        a = a * c / (b * (2*i+1));
    }
    return (float) (2*a);
}
```

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See RS

Section, Name and ID#:

Problem 2: Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope k and the intercept b are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the y coordinates, $\overline{x^2}$ is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. You may assume and use the method `double mean(double[] a)`.

```
public static double[] lin(double[] data) {  
    double[] ans = new double[2];  
    double[] vx = new double[data.length];  
    for (int i = 0; i < data.length; i++) {  
        double x = data[i];  
        vx[i] = x * x;  
    }  
    double sumX = mean(vx);  
    double sumY = mean(data);  
    double sumXY = 0;  
    for (int i = 0; i < data.length; i++) {  
        sumXY += data[i] * vx[i];  
    }  
    double k = (sumXY - sumX * sumY) / (sumX - sumX * sumX);  
    double b = sumY - k * sumX;  
    ans[0] = k;  
    ans[1] = b;  
    return ans;  
}
```

Use the backside, if needed

Problem 2 of 4

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Section, Name and ID#: _____

Problem 3: Write a Java function `public static double area(double[][] vertex)` that takes as its argument a 2-by- n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row. It returns polygon's area as follows:

1. Divides the polygon into triangles by connecting the **first** vertex with the n^{th} and $(n+1)^{\text{st}}$ vertices;
2. Adds the areas of the constructed triangles using the formula $\text{area} = \sqrt{p(p-a)(p-b)(p-c)}$, where a, b and c are the sides and $p = (a + b + c) / 2$.

You may assume and use a method `double dist(double x1, double y1, double x2, double y2)` that takes as its arguments coordinates of two points and returns the distance between them.

public

static

double area(double[][] vertex)

return

double result = 0

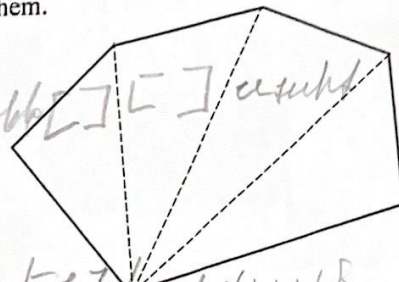
for (int i = 1; i < vertex[0].length; i++)

double a = dist(vertex[0][0], vertex[0][i], vertex[0][i+1])

double b = dist(vertex[0][i], vertex[0][i+1])

double c = dist(vertex[0][0], vertex[0][i+1])

double h = dist(vertex[0][0], vertex[0][i]) * Math.sin(Math.toRadians(Math.atan2(vertex[1][i] - vertex[1][0], vertex[0][i] - vertex[0][0])))



section, Name and ID#:

Problem 4: Write a Java method `public static void magic4N(int[][] square)` that creates a magic square of a $4N$ -by- $4N$ size using the following algorithm:

1. Creates an array of the same size as `int[][] square` and fills it forward with successive integers assigning 1 to the top-left element;
2. Creates another array of the same size as `int[][] square` and fills it backward with successive integers assigning 1 to the bottom-right element;
3. Divides the original `int[][] square` into 16 blocks of the same size – 4 blocks per row and column. In the on-diagonal (shaded) blocks copies the elements from the first array, and in the off-diagonal blocks copies the elements from second array.

1	2					7	8
9	10					15	16
		19	20	21	22		
		27	28	29	30		
		35	36	37	38		
		43	44	45	46		
49	50					55	56
57	58					63	64

		62	61	60	59		
		54	53	52	51		
48	47					42	41
40	39					34	33
32	31					26	25
24	23					18	17
		14	13	12	11		
		6	5	4	3		

Rewrite
 forward and backward one int min int $[4n][4n]$
 $(row=0; row < row \leq column \text{ length} + 1)$
 $for (int column=0; column < forward \text{ length} + 1; column++)$
 $print forward [row][column] = row * forward \text{ length} + column$
 $+ ed \text{ backward}$
 $int backward = min int [4n][4n]$
 $for (int row=0; row < backward \text{ length} + 1; row++)$
 $for (int col=0; col < backward \text{ length} + 1; col++)$
 $backward [row][col] = backward \text{ length} * (backward \text{ length} - row) + col$
 $int [][] = min int [4][4]$
 $for (int row=0; row < square \text{ length}; row++)$
 $for (int col=0; col < square \text{ length}; col++)$
 $print forward$
 $on else print backward$
 not sure →

Use the backside, if needed

Problem 4 of 4

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