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AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 121 Data Structures and Algorithms

MIDTERM 1 EXAM

Date:	Tuesday, October 18 2016
Starting time:	09:00
Duration:	1 hour 15 min
Attention:	**ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED**

Please write down your name and ID# at the top of all used pages

Problem 1: Consider below two recursive expressions:

$$a_n = 1 + a_1*b_1 + a_2*b_2 + a_3*b_3 + \ldots + a_{n-1}*b_{n-1}$$
$$b_n = 1 + 2*b_1 + 2*b_2 + 2*b_3 + \ldots + 2*b_{n-1} - b_{n-1}*b_{n-1}$$

The base cases are: $a_1 = b_1 = 1$.

Write an optimal C++ function or Java method that takes as its argument an int index ***int n*** and returns a_n.

```
double computeBn(int n)
{
    if( n == 1 )
    {
        b1 = 1
        return ;
    }
    return bn = 2*bn-1 - bn-1*bn-1
}
```

```
double computeAn(int n)
{
    if(n = 1)
        return An = 1;
    return An = ComputeAn(int n-1)*
                ComputeBn(int n-1);
}
```

nice try

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$a_1 = 1 + a_1 * b_1$

$b_1 = 1 + 2*b_1 + 2) b_0 - b_0 * b_0$

$b_0 = 1$

$a_0 = 1$

$b_1 = 1 + 2b_1 + 2 - 1$

$-b_1 = 2$

$b_1 = -2$

$a_1 = 1 = 1 + a_1 * b_1$

$b_2 = 1 + 2 b_1$

$b_1 = 0$

$b_4 = 2 * b_3 - b_3 * b_3 =$

$= 2(2b_2 + b_2 * b_2) - (2b_2 + b_2 * b_2)$

$b_2 = 2b_1 - b_1 * b_1 = 2 \cdot 1 - 1 \cdot 1$

$= 1$

$b_2 = 1 + 2 - 1 * 1 = 2$

$b_1 = 1 + 2 - 1 = 2$

Use the backside, if needed

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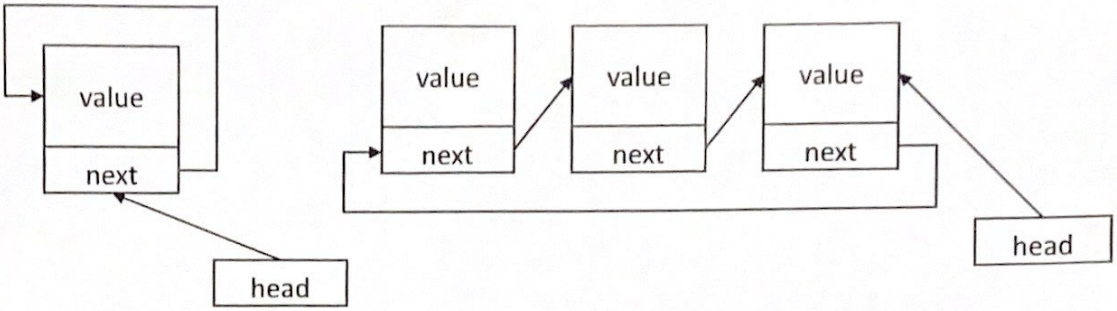
Problem 2: Consider the concept of a ***Circular Queue*** that implements ***Queue ADT*** as a circular list. It has a pointer ***node *head*** that points to the last node – the back, not the first one – the top. The address of the top, therefore, is kept in the pointer ***node *next*** of the last node – ***head->next***. If ***cqueue*** is empty, ***head*** = ***NULL***. If it has just one node, ***head*** = ***head->next***. Examples of one-node and three-node ***cqueue*** objects are shown below:



As usually, ***cqueue*** inserts a new value at the back, removes the top value and retrieves the top value. Derive a C++ ***class cqueue*** from ***class base*** that implements the concept of circular queue. Write the header and source files. The header file of ***class base*** and all its functions are implemented:

```
class base
{
public:
      base(); //the default constructor creates an empty base
      base(const base &that); //copy constructor
      ~base(); //destructor
      bool is_empty();
protected:
      struct node
      {
            int value;
            node *next;
            node(int new_value, node *new_next) : value(new_value), next(new_next){} ;
      };
      node *head;

      void insert(int new_value, int at, node* &from);
      bool remove(int at, node* &from);
      int retrieve(int at, node* from);
}
```

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header

```
class cqueue:base
{
public:  cqueue();
         cqueue(const base &that);
         ~cqueue;
   void insert(int new_value, int at, node* &from);
   bool remove(int at, node* &from);
   int  retrieve(int at, node* &from);

protected:
   struct node
   { int value;
     node *next;
     node(int new_value, node* new_next): value(new_value),
                                          next(new_next){};
   node *head;
};
```

Source file-?

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