

Section, Name and ID#: _____

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 16 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)5^{2k+1}} - 4 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)239^{2k+1}} = \left(\frac{16}{1 \cdot 5} - \frac{4}{1 \cdot 239} \right) - \left(\frac{16}{3 \cdot 5^3} - \frac{4}{3 \cdot 239^3} \right) + \left(\frac{16}{5 \cdot 5^5} - \frac{4}{5 \cdot 239^5} \right) - \dots$$

The initial value of `float compensation` is `0.0`.

`float pi(int n) {`

`float sum = 0;`

`for(int i=0; i<=n; i++) {`

~~`float step = 16.0f / 1.0f`~~

`float step = 16.0f / (1.0f * pow(5.0f, i))`

Use the backside, if needed

Problem 1 of 4

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float sum = 0

~~A~~

for(int i = 1; i <= n; i += 2) {

float ~~step~~ part1 = (16 / (i * pow(5, i)));

float part2 = (4 / (i * pow(239, i)));

float step = Kahan(part1, part2, 0.0f);

sum = Kahan(sum, step, 0.0f);

}

return sum;

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Problem 2: Write a Java method `public static double[] expReg(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the exponent of an exponential regression and the second element being the amplitude. The exponential regression approximates the data points by a formula

where the exponent m and the amplitude a are computed as

$$m = \frac{\overline{xy} - \bar{x}\bar{y}}{\bar{x}^2 - \bar{x}^2}, a = \bar{y} - m\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the natural logarithm of y coordinates, \bar{x}^2 is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and natural logarithm of y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. For natural logarithm, use the method `double Math.log()`.

Both result elements are zeros, if at least one data element is non-positive.

find m, x

$$\bar{y} = \frac{\text{Math.log(arraySum)}}{\bar{x}}$$

$$\bar{x} = \frac{\text{sum(cords)}}{n}$$

```
float expReg(double[] data) {
```

```
    float xsum = 0; //
```

```
    float ysum = 0;
```

```
    float ymean = 0;
```

```
    float xsgsum = 0;
```

```
    float xgmean = 0
```

```
    int n = data.length;
```

```
    for(int i=0; i<n; i++) {
```

```
        float dat = data[i];
```

```
        if(dat < 0) {
```

```
            return new float[] {0, 0};
```

Use the backside, if needed

Problem 2 of 4

}

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```

xsum += i;
ysum += dat;
gmean += Math.log(dat);
xsqsum += Math.pow(dat, 2);
xgmean = i * Math.log(dat);

```

```

}

```

```

xsum = xsum / (float)n;

```

```

gmean = gmean / (float)n;

```

```

xsqsum = xsqsum / (float)n;

```

```

xgmean = xgmean / (float)n;

```

```

float m = (xgmean - (gmean * xsum)) / (xsqsum - Math.pow(xsum, 2));

```

```

float a = gmean - m * xsum;

```

```

return new float[] {m, a};

```

```

}

```

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Problem 3: Write a Java function `public static boolean isInside(double[][] vertex, double x, double y)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row, and `double x` and `double y` coordinates of a point. It checks, if the point is inside the polygon.

Assume and use a method `boolean toLeft(double x1, double y1, double x2, double y2, double x0, double y0)` that takes as its arguments coordinates of three points and returns `true`, if the third point (x_0, y_0) is in the left-hand side, when moving from the first point (x_1, y_1) to the second one (x_2, y_2) ; and `false`, if it is in the right-hand side.

```
isInside(double[][] vertex, double x, double y) {
```

~~float~~ ~~init~~ ~~i~~

bool initialvalue = true;

```
for (int i = 0, i < vertex.length; i += 2) {
```

~~if (i > 0) {~~

~~initialvalue =~~

~~that~~

~~int~~ if (i == 0) {

~~initialvalue~~ = isLeft(vertex[i][0], vertex[i][1];

~~vertex[i+1][0], vertex[i+1][1], x, y);~~

continue;

~~if (isLeft~~ = isLeft(vertex[i][0], vertex[i][1],

vertex[i+1][0], vertex[i+1][1], x, y);

if (isLeft != initialvalue) {

return false;

Use the backside, if needed

Problem 3 of 4

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```
for(int i = vertices[0].length - 1; i > 1; i--) {
```

```
    if(i == vertices[0].length - 1) {
```

```
        initial value = isLeft(vertices[i][0], vertices[i][1],
```

```
vertices[i-1][0], vertices[i-1][1], x, y);
```

```
    } continue;
```

```
    bool isLeft = isLeft(vertices[i][0], vertices[i][1],
```

```
vertices[i-1][0], vertices[i-1][1], x, y);
```

```
    if(!isLeft) {
```

```
        return false;
```

```
    }
```

```
}
```

```
return true;
```

```
}
```

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Problem 4: Write a Java method `public static void magicOdd(int[][] square)` that creates a magic square of an *odd* size using the following algorithm:

1. The number 1 goes in the middle of the top row;
2. All numbers are then placed one *column to the right* and *one row up* from the previous number;
3. Whenever the next number placement is above the top row, stay in the same column and place the number in the bottom row (note the place of 2 instead of the shaded location);
4. Whenever the next number placement is outside of the rightmost column, stay in the same row and place the number in the leftmost column (note the place of 3 instead of the shaded location);
5. When encountering an already filled-in square, place the next number directly below the previous number;
6. When the next number position is outside both a row and a column, place the number directly beneath the previous number (note the place of 7 instead of the shaded location).

	9	2	7
8	1	6	8
3	5	7	3
4	9	2	

```
magicOdd(int[][] square) {
```

```
    int n = square[0].length;
```

```
    int positionx = (n/2) + 1;
```

```
    int positiony = 0;
```

```
    for(int i = 0; i < pow(n, 2); i++) {
```

```
        for(int i = 0; i < pow(n, 2); i++) {
```

```
            if(positionx > n) {
```

```
                positionx = 0;
```

```
            }
```

```
            if(positiony < 0)
```

```
                positiony = n - 1;
```

```
            }
```

```
            square[positiony][positionx] = i;
```

```
            positiony--;
```

```
            positionx++;
```

overwrite?

Use the backside, if needed

Problem 4 of 4

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