

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA  
College of Science and Engineering  
CS 120 Introduction to Object-Oriented Programming  
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

**ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED**

Write down your section, name and ID# at the top of all used pages

Participation:

**Problem 1:** Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value  $\pi$  by the following formula:

$$\pi = 16 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)5^{2k+1}} - 4 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)239^{2k+1}} = \left( \frac{16}{1 \cdot 5} - \frac{4}{1 \cdot 239} \right) - \left( \frac{16}{3 \cdot 5^3} - \frac{4}{3 \cdot 239^3} \right) + \left( \frac{16}{5 \cdot 5^5} - \frac{4}{5 \cdot 239^5} \right) - \dots$$

#include <math.h>

The initial value of `float compensation` is 0.0.

```
float pi(int n) {
    float result; float compensation = 0.0;
    for (int c=0; c<=n; c++) {
        float arg1 = (math::pow(-1, c)) / (2*c+1) * math::pow(5, 2*c+1);
        float arg2 = (math::pow(-1, c)) / (2*c+1) * math::pow(239, 2*c+1);
        float step = 16 * arg1 - 4 * arg2;
        result = kahan(result, step, compensation);
    }
    return result;
}
```

Use the backside, if needed

Problem 1 of 4

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**Problem 2:** Write a Java method `public static double[] expReg(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the exponent of an exponential regression and the second element being the amplitude. The exponential regression approximates the data points by a formula

where the exponent  $m$  and the amplitude  $a$  are computed as

$$m = \frac{\overline{xy} - \bar{x}\bar{y}}{\bar{x}^2 - \bar{x}^2}, a = \bar{y} - m\bar{x}$$

$$\bar{x} = \frac{1}{n} \sum x_i$$

$$\bar{y} = \frac{1}{n} \sum y_i$$

$$\bar{xy} = \frac{1}{n} \sum x_i y_i$$

Here  $\bar{x}$  is the mean of the  $x$  coordinates,  $\bar{y}$  is the mean of the natural logarithm of  $y$  coordinates,  $\bar{x}^2$  is the mean of the squares of the  $x$  coordinates, and  $\bar{xy}$  is the mean of the products of the  $x$  and natural logarithm of  $y$  coordinates. Use the element indices of the array `double[] data` as  $x$  coordinates and the element values as  $y$  coordinates. For natural logarithm, use the method `double Math.log()`.

Both result elements are zeros, if at least one data element is non-positive.

```

public static double[] expReg(double[] data) {
    double[] answer = new double[2];
    for (int x = 0; x < data.length; x++) {
        double dy = Math.log(data[x]);
        double ny = Math.log(ny);
        double m = ((x * ny) - (x * ny)) / (x * x - dy * dy);
        double a = dy - m * x;
        answer[0] = m;
        answer[1] = a;
    }
    return answer;
}

```

return answer;

Use the backside, if needed



Section, Name and ID#:

**Problem 3:** Write a Java function `public static boolean isInside(double[][] vertex, double x, double y)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` - the x coordinates in the first row and y coordinates in the second row, and `double x` and `double y` coordinates of a point. It checks, if the point is inside the polygon.

Assume and use a method `boolean toLeft(double x1, double y1, double x2, double y2, double x0, double y0)` that takes as its arguments coordinates of three points and returns `true`, if the third point ( $x_0, y_0$ ) is in the left-hand side, when moving from the first point ( $x_1, y_1$ ) to the second one ( $x_2, y_2$ ); and `false`, if it is in the right-hand side.

```

public static boolean isInside(double[][] vertex, double x, double y) {
    boolean result;
    boolean[] checkArray = new boolean[vertex[0].length];
    for (int row = 0; row < vertex.length; row++) {
        for (int col = 0; col < vertex[0].length; col++) {
            if (col == 0) {
                state = toLeft(vertex[0][col], vertex[1][col],
                               vertex[row][col+1], vertex[row+1][col+1],
                               x, y);
            } else {
                state = toLeft(vertex[row][col], vertex[0][col],
                               vertex[0][0], vertex[1][1], x, y);
            }
            checkArray[col] = state;
        }
    }
    return result;
}

```

Diagram of a convex polygon with 6 vertices. A point is shown inside. Lines connect the point to each vertex, dividing the polygon into 6 triangles. The vertices are labeled with coordinates from the `vertex` array.

x	0	1	2	3	4
y	7	8	9	10	11

\* Assume there is a function checking if all the values in the array are true or false. If one of the values is not the same that as others it returns false.

result = isSame(checkArray)

return result;

Use the backside, if needed

Problem 3 of 4

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**Problem 4:** Write a Java method `public static void magicOdd(int[][] square)` that creates a magic square of an odd size using the following algorithm:

1. The number 1 goes in the middle of the top row; ✓
2. All numbers are then placed one column to the right and one row up from the previous number; ✓
3. Whenever the next number placement is above the top row, stay in the same column and place the number in the bottom row (note the place of 2 instead of the shaded location); ✓
4. Whenever the next number placement is outside of the rightmost column, stay in the same row and place the number in the leftmost column (note the place of 3 instead of the shaded location); ✓
5. When encountering an already filled-in square, place the next number directly below the previous number; ✓
6. When the next number position is outside both a row and a column, place the number directly beneath the previous number (note the place of 7 instead of the shaded location).

	9	2	7
8	1	6	3
3	5	7	4
4	9	2	

```

public static void magicOdd(int[][] square) {
    row = 0;
    int k, l, m; int firstC = middleCol(square.length);
    int midFirst = square[0][firstC];
    for (int c = 0, c <= int[0].length * int.length; c++) {
        firstC = c;
        square[0][firstC] = c;
        if (firstC > square[0].length) {
            firstC = 0;
        }
        else if (row < 0) {
            row = square.length - 1;
        }
        else if (square[row][firstC] <= c) {
            row = row + 2;
            firstC = firstC - 1;
        }
        else if (row >= 0 & col > square[0].length) {
            row = row + 2;
            firstC = firstC - 1;
        }
        square[row][firstC] = c;
        row = row - 1;
        firstC = firstC + 1;
    }
    return;
}

```

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