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AMERICAN UNIVERSITY OF ARMENIA  
College of Science and Engineering  
CS 121 Data Structures and Algorithms

MIDTERM 1 EXAM

Date: Tuesday, October 18 2016  
Starting time: 09:00  
Duration: 1 hour 15 min  
Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Please write down your name and ID# at the top of all used pages

Problem 1: Consider below two recursive expressions:

$$a_n = 1 + a_1 * b_1 + a_2 * b_2 + a_3 * b_3 + \dots + a_{n-1} * b_{n-1}$$
$$b_n = 1 + 2 * b_1 + 2 * b_2 + 2 * b_3 + \dots + 2 * b_{n-1} - b_{n-1} * b_{n-1}$$

The base cases are:  $a_1 = b_1 = 1$ .

Write an optimal C++ function or Java method that takes as its argument an int index *int n* and returns  $a_n$ .

int n; function?  
can >> n;  
if (n == 1) {  
return 1  
}  
if (n > 1) {  
int b[n]; int i;  
~~for (i = 1; i < n; i++) b[i] = 1;~~  
~~for (i = 1; i < n; i++) b[i] = 1;~~  
if (n > 1; b[n]; n--) {  
b[n] = 2 \* b[n-1] - b[n-2] \* b[n-1]  
if (n > 1; b[n]; n--) {  
return a[n-1] \* b[n-1];  
}

int n;  
if (n == 1) {  
return 1;  
}  
if (n > 1) { int i;  
return b[i] = 2 \* b[i-1] - b[i-2] \* b[i-1]  
? return a[i] = a[i-1] \* b[i-1]  
}

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**Problem 3:** Consider a text that can contain four types of braces: ( ), [ ], { } and < >. The braces are balanced, if the following two conditions hold:

1. Each time a closing brace is encountered, it matches an already encountered corresponding opening brace.
  2. At the end of the text, each opening brace is matching the respective closing one.
- For example, the braces are balanced in a text {ab(c[d]e)}, but not balanced in {ab(c)}.

Write a C++ function `bool balanced_brackets(string text)` or a Java method `public static boolean balancedBrackets(String text)` that take as the argument a string text and check, if the brackets of all four types are balanced or not. Use `stack<char>` in C++ or `Stack<Character>` in Java.

```
bool balanced_brackets(string text){
    stack<char> letter;
    string a;
    char c;
    int i, n;
// ...
    for (i=0; i<text.length(); i++) {
        if (text[i] == '(' || == '{' || == '[' || == '<') {
            letter.push(text[i]);
        }
        else if (text[i] == ')' || == '}' || == ']' || == '>') {
            if (letter.empty()) return false;
            char top = letter.top();
            if ((top == '(' && text[i] == ')') ||
                (top == '{' && text[i] == '}') ||
                (top == '[' && text[i] == ']') ||
                (top == '<' && text[i] == '>')) {
                letter.pop();
            }
            else return false;
        }
    }
    return letter.empty();
}
```

Use the backside, if needed

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