

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 16 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)5^{2k+1}} - 4 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)239^{2k+1}} = \left(\frac{16}{1 \cdot 5} - \frac{4}{1 \cdot 239} \right) - \left(\frac{16}{3 \cdot 5^3} - \frac{4}{3 \cdot 239^3} \right) + \left(\frac{16}{5 \cdot 5^5} - \frac{4}{5 \cdot 239^5} \right) - \dots$$

The initial value of `float compensation` is 0.0.

Handwritten code for pi(int n):

```
float pi(int n) {
    float result = 0;
    for (int k = 0; k <= n; k++) {
        result += kahan(pow(-1, k) / ((2 * k + 1) * pow(5, (2 * k + 1))), pow(-1, k) / ((2 * k + 1) * pow(239, (2 * k + 1))), compensation);
    }
    return result;
}
```

Handwritten note: 4 * kahan(pow, half?)

Use the backside, if needed

Problem 1 of 4

OOP.MT.170317.L088

Section, Name and ID#:

Problem 2: Write a Java method `public static double[] expReg(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the exponent of an exponential regression and the second element being the amplitude. The exponential regression approximates the data points by a formula

$$y = a e^{mx},$$

where the exponent m and the amplitude a are computed as

$$m = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, a = \bar{y} - m\bar{x}$$

1 means pow(bit, second)

$$3 \wedge 2 = 9.$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the natural logarithm of y coordinates, $\overline{x^2}$ is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and natural logarithm of y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. For natural logarithm, use the method `double Math.log()`.

Both result elements are zeros, if at least one data element is non-positive.

```
public static double[] expReg(double[] data) {
    double x2s = 0; double ylogs = 0; double x2s, ylogs, x2s, xproy;
    x2s = 0; ylogs = 0;
    for (int i = 0; i < data.length; i++) {
        xproy *= i;
        x2s += i * i;
        ylogs += Math.log(data[i]);
    }
    double xmean = x2s / 2; double ymeanlog = ylogs / 2;
    double x2mean = x2s / 2; double xproylogmean = (xproy + ylogs) / 2;
    double m = (xproylogmean - xmean * ymeanlog) / (
        x2mean - (xmean * xmean));
    double a = ymeanlog - m * xmean;
    double[] result; result = new double[2];
    result[0] = m; result[1] = a; return result;
}
```

This if statement must be in the for loop above.

```
if (data[i] <= 0) {
    result[0] = 0; result[1] = 0;
    return result;
}
```

3

Section, Name and ID#:

Problem 3: Write a Java function `public static boolean isInside(double[][] vertex, double x, double y)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row, and `double x` and `double y` coordinates of a point. It checks, if the point is inside the polygon.

Assume and use a method `boolean toLeft(double x1, double y1, double x2, double y2, double x0, double y0)` that takes as its arguments coordinates of three points and returns `true`, if the third point (x_0, y_0) is in the left-hand side, when moving from the first point (x_1, y_1) to the second one (x_2, y_2) ; and `false`, if it is in the right-hand side.

Handwritten code and diagram:

```

public static boolean isInside(
    double[][] vertex, double x, double y) {
    int g = 0;
    for (int i = 0; i < vertex.length; i++) {
        for (int j = 0; j < vertex[i].length; j++) {
            for (int q = 0; q < vertex[i].length; q++) {
                for (int e = 0; e < vertex[i].length; e++) {
                    if (toLeft(i, j, q, e, x, y)) {
                        if (g == 1) return true;
                        else g = 2;
                    }
                    if (!toLeft(i, j, q, e, x, y)) {
                        if (g == 2) return true;
                        else g = 1;
                    }
                }
            }
        }
    }
    return false;
}
    
```

Diagram: A convex polygon with 6 vertices. A point is shown inside the polygon. The code is annotated with "too many cases" and "all cases needed".

Use the backside, if needed

Problem 3 of 4

OP. MT. 170318. L 046