

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1}{2} * \frac{2}{3} + \frac{1*3}{2*4} * \frac{2}{5} + \frac{1*3*5}{2*4*6} * \frac{2}{7} + \dots$$

Recall that $n!!$ is the product of odd numbers from 1 to n , if n is odd; and is the product of even numbers from 2 to n , if n is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

```
int factorial(int k) {
    int mul = 1;
    for (int i = k; i > 0; i--)
        mul *= i;
    return mul;
}

float pi(int n) {
    float compensation = 0.0;
    float result = 0.0;
    for (int k = 0; k <= n; k++) {
        result += kahan(result, 2.0 / (2*k+1), compensation);
    }
    return result;
}
```

Use the backside, if needed

Problem 1 of 4

else {return t}

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```
11001 pi(int n) {
```

```
    int pre;  
    for (int k=0; k<=n; k++) {
```

```
        pre += factorial(2*k-1) / (factorial(2*k)*2^(k+1));
```

```
    }
```

```
    return 2*pre;
```

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Problem 2: Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope k and the intercept b are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the y coordinates, $\overline{x^2}$ is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. You may assume and use the method `double mean(double[] a)`.

```
double public static double[] lin(double[] data) {
    double mean_x;
    for (int i=0; i < data.length; i++) {
        mean_x += i;
    }
    double mean_y;
    for (i=0; i < data.length; i++) {
        mean_y += data[i];
    }
    double k = (mean_x * mean_y) - .
    double mean_xy;
    for (i=0; i < data.length; i++) {
        mean_xy += data[i] * (i+1)
    }
}
```

Use the backside, if needed

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Problem 3: Write a Java function `public static double area(double[][] vertex)` that takes as its argument a 2-by- n array of a convex polygon's vertex coordinates `double[][] vertex` - the x coordinates in the first row and y coordinates in the second row. It returns polygon's area as follows:

1. Divides the polygon into triangles by connecting the **first** vertex with the n^{th} and $(n+1)^{\text{st}}$ vertices;
2. Adds the areas of the constructed triangles using the formula $\text{area} = \sqrt{p(p-a)(p-b)(p-c)}$, where a , b and c are the sides and $p = (a + b + c) / 2$.

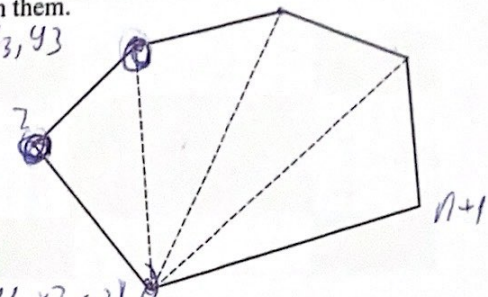
You may assume and use a method `double dist(double x1, double y1, double x2, double y2)` that takes as its arguments coordinates of two points and returns the distance between them.

`public static double p(x1, y1, x2, y2, x3, y3)`

`int p;`

`p = dist(x1, y1, x2, y2) +`

`dist(x2, y2, x3, y3) + dist(x1, y1, x3, y3);`



`public static double area(double[][] vertex) {`

`int a = vertex[0].length;`

`double P; double area;`

`for (i = 1; i < a; i++) {`

`P = dist(vertex[0][0], vertex[1][0], vertex[0][i])`

`dist(vertex[1][i], vertex[0][i+1]) + dist(vertex[0][i+1],`

`vertex[0][0]) * (P - dist(vertex[0][0], vertex[1][0], vertex[0][i], vertex[0][i+1])) * (P - dist(vertex[0][0], vertex[1][0], vertex[0][i+1], vertex[0][i])) * P;`

Use the backside, if needed

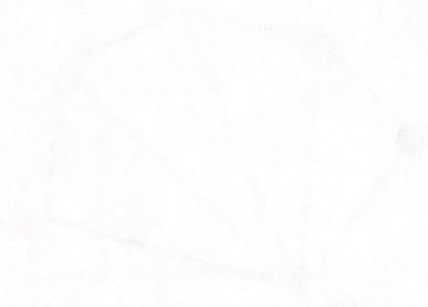
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`dist(vertex[0][i], vertex[1][i], vertex[0][i+1], vertex[1][i+1])`

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return area;

y



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Problem 4: Write a Java method `public static void magic4N(int[][] square)` that creates a magic square of a $4N$ -by- $4N$ size using the following algorithm:

1. Creates an array of the same size as `int[][] square` and fills it forward with successive integers assigning `1` to the top-left element;
2. Creates another array of the same size as `int[][] square` and fills it backward with successive integers assigning `1` to the bottom-right element;
3. Divides the original `int[][] square` into 16 blocks of the same size – 4 blocks per row and column. In the on-diagonal (shaded) blocks copies the elements from the first array, and in the off-diagonal blocks copies the elements from second array.

1	2					7	8
9	10					15	16
		19	20	21	22		
		27	28	29	30		
		35	36	37	38		
		43	44	45	46		
49	50					55	56
57	58					63	64

		62	61	60	59		
		54	53	52	51		
48	47					42	41
40	39					34	33
32	31					26	25
24	23					18	17
		14	13	12	11		
		6	5	4	3		

```

public static void magic4N(int[][] square) {
    int[][] square1 = new int[square[0].length][square[0].length]
    int[][] square2 = new int[square[0].length][square[0].length]

    for (int i = 0; i < square[0].length; i++) {
        for (int j = 0; j < square[0].length; j++) {
            square1[i][j] = square[0].length * i + j + 1
        }
    }

    for (int i = square[0].length; i >= 0; i--) {
        for (int j = square[0].length; j >= 0; j--) {
            square2[square[0].length - i][square[0].length - j] =
                square[0].length * i + j + 1.
        }
    }
}

```

Use the backside, if needed

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problem 4

the function by understanding the column chooses
the element sort places them in square 2D array

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