

Section, Name and ID#

AMERICAN UNIVERSITY OF ARMENIA  
College of Science and Engineering  
CS 120 Introduction to Object-Oriented Programming  
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

**ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED**

Write down your section, name and ID# at the top of all used pages

Participation:

**Problem 1:** Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

*(num1 + num2 - comp)*  
*- num1 + num2*

Using this function, write a C++ function `float pi(int n)` that computes the value  $\pi$  by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1}{2} * \frac{2}{3} + \frac{1*3}{2*4} * \frac{2}{5} + \frac{1*3*5}{2*4*6} * \frac{2}{7} + \dots$$

Recall that  $n!!$  is the product of odd numbers from 1 to  $n$ , if  $n$  is odd; and is the product of even numbers from 2 to  $n$ , if  $n$  is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

`float pi(int n)`

*result = 0;*  
*for (int k=0; k<=n; k++)*

*result = 2 \* (odd(2k-1) / even(2k) \* (2k+1));*

*for (int k=0; k<=n; k++)*

*result = result + 2 \* (odd(2k-1) / even(2k) \* (2k+1));*

*}*

*return result;*

*double odd(int n) {*  
*double result = 1;*  
*for (int i=1; i<=n; i++)*

*result = result \* i;*

*return result;*

*double even(int n) {*

*double result = 1;*

*for (int i=2; i<=n; i+=2)*

*result = result \* i;*

*return result;*

*Kahan?*

*3*

Use the backside, if needed

Problem 1 of 4

*2 \* (odd(2k-1) / even(2k) \* (2k+1))*

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**Problem 2:** Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope  $k$  and the intercept  $b$  are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

Here  $\bar{x}$  is the mean of the  $x$  coordinates,  $\bar{y}$  is the mean of the  $y$  coordinates,  $\overline{x^2}$  is the mean of the squares of the  $x$  coordinates, and  $\overline{xy}$  is the mean of the products of the  $x$  and  $y$  coordinates. Use the element indices of the array `double[] data` as  $x$  coordinates and the element values as  $y$  coordinates. You may assume and use the method `double mean(double[] a)`.

# include math.h

```
public static double[] lin(double[] data) {
```

```
    for (int i = 0; i < data.length; i++) {
```

```
        for (int j = data[0]; j <= data[data.length]; j++) {
```

```
            double k = (mean(i * j) - (mean(i) * mean(j))) /
```

```
                [mean(pow(i, 2)) - mean(i) pow(mean(i), 2)];
```

```
            double b = mean(j) - k * mean(i);
```

```
        }
```

```
    return double[] arr(k, b);
```

```
}
```

2

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**Problem 3:** Write a Java function `public static double area(double[][] vertex)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row. It returns polygon's area as follows:

1. Divides the polygon into triangles by connecting the *first* vertex with the  $n^{\text{th}}$  and  $(n+1)^{\text{st}}$  vertices;
2. Adds the areas of the constructed triangles using the formula  $\text{area} = \sqrt{p(p-a)(p-b)(p-c)}$ , where  $a, b$  and  $c$  are the sides and  $p = (a + b + c) / 2$ .

You may assume and use a method `double dist(double x1, double y1, double x2, double y2)` that takes as its arguments coordinates of two points and returns the distance between them.

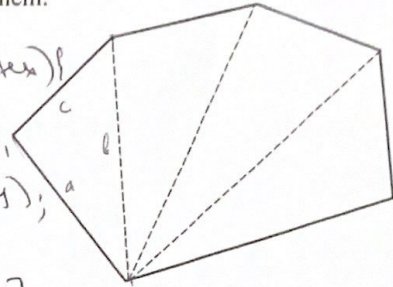
```

public static double area (double [][] vertex) {
    double A = 0;
    for (int i = 0; i < vertex.length; i++) {
        int a = double dist (vertex[i][0], vertex[i][1],
                             vertex[i+1][0], vertex[i+1][1]);
        int b = double dist (vertex[i][0], vertex[i][1],
                             vertex[i+2][0], vertex[i+2][1]);
        int c = double dist (a[0], a[1], b[0], b[1]);
        double p = (a+b+c)/2;
        double area = sqrt(p*(p-a)*(p-b)*(p-c));
        A = A + area;
    }
    return A;
}

```

*Handwritten notes:*

- double A = 0;* (written before the for loop)
- double A = 0;* (crossed out)
- A = A + area;* (written after the for loop)
- 3* (written before the return statement)
- return A;* (written after the return statement)



*2.*

*correct idea  
wrong implementation*

Use the backside, if needed

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