

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming

MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 2 \sum_{k=0}^{\infty} \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1*2}{2*3} + \frac{1*3*2}{2*4*5} + \frac{1*3*5*2}{2*4*6*7} + \dots$$

Recall that $n!!$ is the product of odd numbers from 1 to n , if n is odd; and is the product of even numbers from 2 to n , if n is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

```
float pi(int n) {
    float pi pi;
    // for (int z=0; z<=n; z++) {
    //     pi += sumOdd(z) / (sumEv(z) * (z+1));
    // }
    pi = kahan(sumOdd(z) / (sumEv(z) * (z+1)),
               sumOdd(z+1) / (sumEv(z+1) * (z+2)),
               0.0);
    return pi;
}
```

float of pi:

```
float sumEven(float f) {
    float d;
    for (int i=0; i<=f; i+=2) {
        d += kahan(1.0 / i, i+2, 0.0);
    }
    return d;
}

float sumOdd(float m) {
    float c;
    for (int j=1; j<=m; j+=2) {
        c += kahan(1.0 / j, j+2, 0.0);
    }
    return c;
}
```

product needed

Use the backside, if needed

Problem 1 of 4

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Problem 2: Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope k and the intercept b are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the y coordinates, $\overline{x^2}$ is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. You may assume and use the method `double mean(double[] a)`.

```

public static double[] lin(double[] data) {
    double x, y, k, b;
    double[] arr = new double[2];
    double x = mean(arrCr(data.length));
    double y = mean(data);
    double xy = mean(arrMul(data));
    double sqrx1 = mean(arrCr(data.length), 2);
    double sqrx2 = x * x;
    arr[0] double k = (xy - x * y) / (sqrx1 - sqrx2);
    arr[1] double b = y - k * x;
    return arr;
}

public static double[] arrCr(int c) {
    double[] arr1 = new double[c];
    for (int i = 0; i <= c; i++) {
        if (i == 1) {
            arr1[i] = i;
        } else if (i == 2) {
            arr1[i] = i * i;
        }
    }
    return arr1;
}

public static double[] arrMul(double[] s) {
    double arr2 = new double[s.length];
    for (int j = 0; j <= s.length; j++) {
        arr2[j] = arr2[j] * j;
    }
    return arr2;
}

```

Use the backside, if needed

Problem 2 of 4

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