

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA  
College of Science and Engineering  
CS 120 Introduction to Object-Oriented Programming  
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

**ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED**  
Write down your section, name and ID# at the top of all used pages

Participation:

**Problem 1:** Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value  $\pi$  by the following formula:

$$\pi = 16 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)5^{2k+1}} - 4 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)239^{2k+1}} = \left( \frac{16}{1 \cdot 5} - \frac{4}{1 \cdot 239} \right) - \left( \frac{16}{3 \cdot 5^3} - \frac{4}{3 \cdot 239^3} \right) + \left( \frac{16}{5 \cdot 5^5} - \frac{4}{5 \cdot 239^5} \right) - \dots$$

The initial value of `float compensation` is `0.0`.

```
float pi(int n)
{
    int sum, int m, int d;
    for(int k=0; k<n; k++)
    {
        m = 16 * (pow(-1,k) / (2k+1) * pow(5, 2k+1)) -
        - 4 * (pow(-1,k) / (2k+1) * pow(239, 2k+1))
        d = (16 * pow(-1,(k+1)) / (2(k+1)+1) * pow(5, 2(k+1)+1)) -
        - 4 * (pow(-1,(k+1)) / (2(k+1)+1) * pow(239, 2(k+1)+1))
        sum = sum + kahan(m, d, 0.0);
    }
    return sum;
}
```

Use the backside, if needed

Problem 1 of 4

OOP.MT.170317.MOB7

see HG

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**Problem 2:** Write a Java method `public static double[] expReg(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the exponent of an exponential regression and the second element being the amplitude. The exponential regression approximates the data points by a formula

$$y = a e^{mx},$$

where the exponent  $m$  and the amplitude  $a$  are computed as

$$m = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, a = \bar{y} - m\bar{x}$$

Here  $\bar{x}$  is the mean of the  $x$  coordinates,  $\bar{y}$  is the mean of the natural logarithm of  $y$  coordinates,  $\overline{x^2}$  is the mean of the squares of the  $x$  coordinates, and  $\overline{xy}$  is the mean of the products of the  $x$  and natural logarithm of  $y$  coordinates. Use the element indices of the array `double[] data` as  $x$  coordinates and the element values as  $y$  coordinates. For natural logarithm, use the method `double Math.log()`.

Both result elements are zeros, if at least one data element is non-positive.

```
public static double[] expReg(double[] data) {
```

```
    int x1, y1, x2, m, a, x2;
```

```
    for (int x=0; x<data.length; x++)
```

```
    { xy = xy + x * double Math.log(data[x]);
```

```
        x1 = x1 + x;
```

```
        y1 = y1 + double Math.log(data[x]);
```

```
        x2 = x2 + pow(x1, 2); }
```

```
    m = (xy / data.length) - (x1 / data.length) * (y1 / data.length)
```

```
        / ((x2 / data.length) - pow(x1 / data.length, 2))
```

```
    a = (y1 / data.length) - m * (x1 / data.length)
```

```
    double[] mek = new double[2];
```

```
    mek[0] = m;
```

```
    mek[1] = a;
```

```
    return mek;
```

Use the backside, if needed

OOP.MT.10317.M064

Problem 2 of 4

see HG



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**Problem 3:** Write a Java function `public static boolean isInside(double[][] vertex, double x, double y)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row, and `double x` and `double y` coordinates of a point. It checks, if the point is inside the polygon.

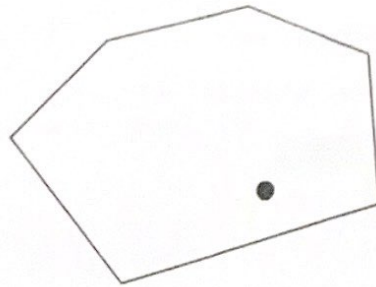
Assume and use a method `boolean toLeft(double x1, double y1, double x2, double y2, double x0, double y0)` that takes as its arguments coordinates of three points and returns `true`, if the third point  $(x_0, y_0)$  is in the left-hand side, when moving from the first point  $(x_1, y_1)$  to the second one  $(x_2, y_2)$ ; and `false`, if it is in the right-hand side.

```
public static boolean isInside  
(double[][] vertex, double x, double y)
```

```
{ for (int i=0; i<2, i++)
```

```
{ for (int j=0, j<vertex[i].length, j++)
```

we should have an if statement  
in order to state our conditions  
of returning false or true



OOP.MT.18031J.m067

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Problem 3 of 4

**Problem 4:** Write a Java method `public static void magicOdd(int[][] square)` that creates a magic square of an *odd* size using the following algorithm:

1. The number 1 goes in the middle of the top row;
2. All numbers are then placed one *column to the right* and *one row up* from the previous number;
3. Whenever the next number placement is above the top row, stay in the same column and place the number in the bottom row (note the place of 2 instead of the shaded location);
4. Whenever the next number placement is outside of the rightmost column, stay in the same row and place the number in the leftmost column (note the place of 3 instead of the shaded location);
5. When encountering an already filled-in square, place the next number directly below the previous number;
6. When the next number position is outside both a row and a column, place the number directly beneath the previous number (note the place of 7 instead of the shaded location).

	9	2	7
8	1	6	3
3	5	7	4
4	9	2	

```
public static void magicOdd(int[][] square)
```

```
{ int [][] magic = new int[n][n]
```

$n \% 2 = 1$

```
for (int j = 0; j < square.length; j++)
    for (int i = 0; i < square.length; i++)
```

we start the odd size

~~row[i+1][j+1]~~

~~square[i+1][j+1]~~ = 1

1st row 2nd column is equal to 1

OOP.MT. 170317.M067

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