

Section, Name and ID#:

OOP.MT.170318.HOYT

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1}{2} * \frac{2}{3} + \frac{1*3}{2*4} * \frac{2}{5} + \frac{1*3*5}{2*4*6} * \frac{2}{7} + \dots$$

Recall that $n!!$ is the product of odd numbers from 1 to n , if n is odd; and is the product of even numbers from 2 to n , if n is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

```
float pi (int n)
{
    float result = 0.0, float odd, even, pcomp;
    loop needed if (n % 2 != 0) { // n is odd
        for (int i = 1; i <= n; i += 2)
            odd *= i;
    }
    else {
        for (int i = 2; i <= n; i += 2)
            even *= i;
    }
    result = odd / even * (2 * n + 1);
    return 2 * result;
}
```

Use the backside, if needed

Problem 1 of 4

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Problem 2: Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope k and the intercept b are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\bar{x}^2 - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

$$\begin{pmatrix} k \\ b \end{pmatrix}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the y coordinates, \bar{x}^2 is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. You may assume and use the method `double mean(double[] a)`.

```

public static double[] lin(double[] data) {
    for (int i = 0; i < data.length; i++) {
        double[] xm = new double[data.length];
        xm[i] = i;
        double[] ym = new double[data.length];
        ym[i] = data[i];
    }
    int x = mean((double[]) xm);
    double[] ym = new double[data.length];
    for (int i = 0; i < data.length; i++) {
        ym[i] = data[i];
    }
    int y = mean((double[]) ym);
    double[] x2m = new double[data.length];
    for (int i = 0; i < data.length; i++) {
        x2m[i] = i^2;
    }
    int x2 = mean((double[]) x2m);
    double[] xym = new double[data.length];
    for (int i = 0; i < data.length; i++) {
        xym[i] = i * data[i];
    }
    int xy = mean((double[]) xym);
    result[0] = (xy - (x * y)) / (x2 - x * x);
    result[1] = y - result[0] * x;
    return result;
}

```

Use the backside, if needed

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```

public static int scalar( int[] mat1, int[] mat2 )
{
    int result = 0;
    for (int i=0; i < mat1.length; i++)
    {
        result += mat1[i] * mat2[i];
    }
    return result;
}

```

```

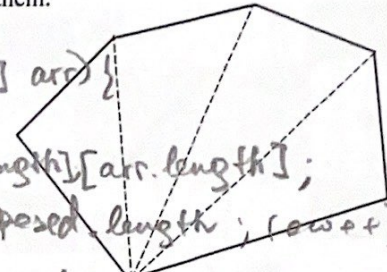
public static void printD ( int[] arr ) {
    for (int i=0; i < arr.length; i++) {
        System.out.print ( arr[i] + " ");
    }
}

```


Problem 3: Write a Java function `public static double area(double[][] vertex)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` - the x coordinates in the first row and y coordinates in the second row. It returns polygon's area as follows:

1. Divides the polygon into triangles by connecting the first vertex with the n^{th} and $(n+1)^{\text{st}}$ vertices;
2. Adds the areas of the constructed triangles using the formula $\text{area} = \sqrt{p(p-a)(p-b)(p-c)}$, where a , b and c are the sides and $p = (a + b + c) / 2$.

You may assume and use a method `double dist(double x1, double y1, double x2, double y2)` that takes as its arguments coordinates of two points and returns the distance between them.



```
public static void transpose (int[][] arr) {
    int [][] transposed = new int [arr[0].length][arr.length];
    for (int row = 0; row < transposed.length; row++) {
        for (int col = 0; col < transposed[0].length; col++) {
            transposed [ row ][ col ] = arr [ col ][ row ];
        }
    }
}
```

(already created) `print2d (transposed);` change to `arr` - ?

```
public static void shiftL (int[] arr) {
    int keeper = arr[0];
    for (int i = 0; i < arr.length / 2; i++) {
        arr [ i ] = arr [ i + 1 ];
    }
    arr [ arr.length - 1 ] = keeper;
    print1d ( arr ); not needed
}
```

```
public static int[][] multiply (int[][] mat1, int[][] mat2)
{
    int [][] result = new int [ mat1.length ][ mat1.length ];
    transpose ( mat2 );
    for ( int row = 0; row < result.length; row++ ) {
        for ( int col = 0; col < result.length; col++ ) {
            result [ row ][ col ] = scalar
            transpose ( mat2 );
            return result;
        }
    }
}
```

Use the backside, if needed

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Previous page.

$$\text{row} = \text{arr}[\text{row}].\text{length} + \text{col} + 1$$

for (int row = 0; row < arr.length; row++)

1 2 3 4 { for (int col = 0; col < arr[0].length; col++)

}

$$\text{arr}[\text{row}][\text{col}] = \text{row} \cdot \text{arr}[\text{row}].\text{length} + \text{col} + 1$$

row 0

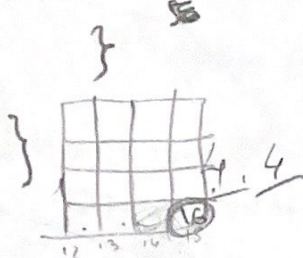
col 3

row 1

col 0

$$0 \cdot 4 + 0 + 1 = 1$$

$$1 \cdot 4 + 1 = 5$$



$$4 \cdot 4 + 4 - 4$$

$$\begin{aligned} 4 \cdot 4 - (4 \cdot 4 + 4 + 1) &= \\ &= 16 - (19) \\ 4 \cdot 4 + 3 + 4 &= 15 \\ 16 + 2 - 4 &= 14 \end{aligned}$$

$$\text{arr.length} \cdot \text{arr}[\text{row}].\text{length} - (\text{row} \cdot \text{arr}[\text{row}].\text{length} + \text{col} + 1)$$

for (int row = square.length; row > 0; row--)

for (int col = square[0].length; col > 0; col--)

$$\text{square}[\text{row}][\text{col}] = \text{arr.length} \cdot \text{arr}[\text{row}].\text{length} -$$

$$\frac{\text{arr.length} \cdot \text{row} + \text{col} - + \text{col} + \text{square}}{\text{arr.length}}$$

$$4 \cdot 3 + 4 - 4 = 12$$

Problem 4: Write a Java method `public static void magic4N(int[][] square)` that creates a magic square of a $4N$ -by- $4N$ size using the following algorithm:

1. Creates an array of the same size as `int[][] square` and fills it forward with successive integers assigning 1 to the top-left element;
2. Creates another array of the same size as `int[][] square` and fills it backward with successive integers assigning 1 to the bottom-right element;
3. Divides the original `int[][] square` into 16 blocks of the same size – 4 blocks per row and column. In the on-diagonal (shaded) blocks copies the elements from the first array, and in the off-diagonal blocks copies the elements from second array.

in main
Scanner input
= new Scanner
(System.in);

1	2					7	8
9	10					15	16
		19	20	21	22		
		27	28	29	30		
		35	36	37	38		
		43	44	45	46		
49	50					55	56
57	58					63	64

		62	61	60	59		
		54	53	52	51		
48	47					42	41
40	39					34	33
32	31					26	25
24	23					18	17
		14	13	12	11		
		6	5	4	3		

```

① public static void magic4N(int[][] square) {
    int[][] arr = new int[square.length][square.length];
    for (int row = 0; row < square.length; row++) {
        for (int col = 0; col < square[0].length; col++) {
            square[row][col] = row * square[0].length + col + 1;
        }
        System.out.println();
    }

    // int[][] arr2 = new int[square.length][square.length];
    // for (int row = arr2.length; row > 0; row--) {
    //     for (int col = arr2[0].length; col > 0; col--) {
    //         arr2[row][col] = arr2.length * row + col - arr.length;
    //     }
    //     System.out.println();
    // }
}

```

```

for (int row = 0; row < arr2.length; row++) {
    for (int col = 0; col < arr2[0].length; col++) {
        arr2.length * row + col - arr.length - arr[row][col];
    }
    System.out.println();
}

```

Use the backside, if needed

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