

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:
Duration:
Attention:

Friday, March 17 2017 at 17:30
2 hours

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED
Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 16 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)5^{2k+1}} - 4 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)239^{2k+1}} = \left(\frac{16}{1 \cdot 5} - \frac{4}{1 \cdot 239} \right) - \left(\frac{16}{3 \cdot 5^3} - \frac{4}{3 \cdot 239^3} \right) + \left(\frac{16}{5 \cdot 5^5} - \frac{4}{5 \cdot 239^5} \right) - \dots$$

The initial value of `float compensation` is `0.0`.

```
float pi(int n) {
    int length = n;
    for (int i = 0; i <= n; i++) {
        p = Math.Pow(-1, i) / ((i+1) * Math.Pow(5, 2*i+1))
        float num1 = 16 * Math.Pow(-1, i) / ((i+1) * Math.Pow(5, 2*i+1));
        float num2 = 4 * Math.Pow(-1, i) / ((i+1) * Math.Pow(239, 2*i+1));
        float p1 = 0;
        pi += kahan(num1, num2, comp 0);
    }

    return pi;
}
```

Use the backside, if needed

Problem 1 of 4

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