

Section, Name #

AMERICAN UNIVERSITY OF ARMENIA  
College of Science and Engineering  
CS 120 Introduction to Object-Oriented Programming  
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

**ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED**  
Write down your section, name and ID# at the top of all used pages

7 sec 15

Participation:

**Problem 1:** Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value  $\pi$  by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1}{2} * \frac{2}{3} + \frac{1*3}{2*4} * \frac{2}{5} + \frac{1*3*5}{2*4*6} * \frac{2}{7} + \dots$$

Recall that  $n!!$  is the product of odd numbers from 1 to  $n$ , if  $n$  is odd; and is the product of even numbers from 2 to  $n$ , if  $n$  is even. The double factorial of non-positive numbers equals to 1 by definition. The initial value of `float compensation` is 0.0.

```
float pi(int n) {
    float p = 0.0;
    float result = 0.0;
    for (int i = 0; i < n; i++) {
        p = kahan(result,  $\frac{(2i-1)!!}{(2i)!!(2i+1)}$ , 0.0);
    }
}
```

int division

3/2 = 1.5

See NS

```
return p;
}
```

Use the backside, if needed

Problem 1 of 4

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**Problem 2:** Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope  $k$  and the intercept  $b$  are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

Here  $\bar{x}$  is the mean of the  $x$  coordinates,  $\bar{y}$  is the mean of the  $y$  coordinates,  $\overline{x^2}$  is the mean of the squares of the  $x$  coordinates, and  $\overline{xy}$  is the mean of the products of the  $x$  and  $y$  coordinates. Use the element indices of the array `double[] data` as  $x$  coordinates and the element values as  $y$  coordinates. You may assume and use the method `double mean(double[] a)`.

```
public static double[] lin(double[] data) {
    double[] xy = new double[data.length];
    double[] x2 = new double[data.length];
    double[] x = new double[data.length];
    double[] result = new double[2];
    result[0] = double[] xc = new double[data.length];
    for (int i = 0; i < data.length - 1; i++) {
        xy[i] = i * x[i];
        x2[i] = i * i;
        xc[i] = i;
    }
    result[0] = (mean(xy) - mean(xc) * mean(x)) / (mean(x2) - (mean(xc) * mean(xc)));
    result[1] = mean(x) - result[0] * mean(xc);
    return result;
}
```

3/2 = 1.5  
see NS

one more problem, take array and fill with ones. "1"

```
int[][] one = new int[5][5];
for (int row = 0; row < one.length; row++) {
    for (int col = 0; col < one[row].length; col++) {
        one[row][col] = 1;
    }
}
```

Use the backside, if needed

Problem 2 of 4

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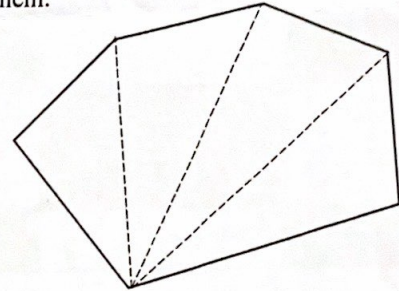


**Problem 3:** Write a Java function `public static double area(double[][] vertex)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row. It returns polygon's area as follows:

1. Divides the polygon into triangles by connecting the **first** vertex with the  $n^{th}$  and  $(n+1)^{st}$  vertices;
2. Adds the areas of the constructed triangles using the formula  $area = \sqrt{p(p-a)(p-b)(p-c)}$ , where  $a, b$  and  $c$  are the sides and  $p = (a + b + c) / 2$ .

You may assume and use a method `double dist(double x1, double y1, double x2, double y2)` that takes as its arguments coordinates of two points and returns the distance between them.

```
public static double area(double[][] vertex){
    double area;
```



another problem

```
public static int mat(int[][] arr){
    for(int row=0; row<arr.length; row++){
        for(int col=0; col<arr[0].length; col++){
            arr[row][col] = 0;
        }
    }
    return arr;
}
```

takes an  $n \times n$  array ~~arr~~ and fill each row from 1 to n;

eg.  $4 \times 4$  array is returned in this way.

```
1 2 3 4
1 2 3 4
1 2 3 4
1 2 3 4
```

```
return area;
}
```

factorial function, another problem.

```
int factorial(int n){
    if(n <= 0){
        return "error";
    }
    else{
        for(int i=n; i>1; i--){
            n = n * i;
        }
    }
    return n;
}
```

Use the backside, if needed



**Problem 4:** Write a Java method `public static void magic4N(int[][] square)` that creates a magic square of a  $4N$ -by- $4N$  size using the following algorithm:

1. Creates an array of the same size as `int[][] square` and fills it forward with successive integers assigning 1 to the top-left element;
2. Creates another array of the same size as `int[][] square` and fills it backward with successive integers assigning 1 to the bottom-right element;
3. Divides the original `int[][] square` into 16 blocks of the same size – 4 blocks per row and column. In the on-diagonal (shaded) blocks copies the elements from the first array, and in the off-diagonal blocks copies the elements from second array.

1	2					7	8
9	10					15	16
		19	20	21	22		
		27	28	29	30		
		35	36	37	38		
		43	44	45	46		
49	50					55	56
57	58					63	64

		62	61	60	59		
		54	53	52	51		
48	47					42	41
40	39					34	33
32	31					26	25
24	23					18	17
		14	13	12	11		
		6	5	4	3		

```

public static void magic4N(int[][] square) {
    int n, i, j, k, r, c = 1;
    Scanner input = new Scanner(System.in);
    n = input.nextInt();
    int[][] arr = new int[square.length][square.length];
    for (i = 0; i < arr.length; i++) {
        for (j = 0; j < arr[i].length; j++) {
            arr[i][j] = k;
            k++;
        }
    }
    int[][] arr2 = new int[square.length][square.length];
    for (row = 0; row < arr2.length; row++) {
        for (col = 0; col < arr2[row].length; col++) {
            arr2[row][col] = k;
            k--;
        }
    }
}

```

2/2 = 1  
see NS



... array, return the largest element,  
~~public static int[] big = new~~

```
public static int big(int[] b){
```

```
    int a = b[0];
```

```
    for (let i = 0; i < b.length; i++) {
```

```
        if (a < b[i]) {
```

```
            a = b[i]
```

```
        }
```

```
    }  
    return a;  
}
```

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