

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 16 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)5^{2k+1}} - 4 \sum_{k=0}^n \frac{(-1)^k}{(2k+1)239^{2k+1}} = \left(\frac{16}{1 \cdot 5} - \frac{4}{1 \cdot 239} \right) - \left(\frac{16}{3 \cdot 5^3} - \frac{4}{3 \cdot 239^3} \right) + \left(\frac{16}{5 \cdot 5^5} - \frac{4}{5 \cdot 239^5} \right) - \dots$$

The initial value of `float compensation` is 0.0.

```
float pi(int n) {
    int float sum1 = 0.0;    int pi1, pi2;    babken = ?
    float sum2 = 0.0;
    for (int k=0; k <= n; k++) {
        pi1 = (16 * pow(-1, k)) / ((2*k+1) * pow(5, 2*k+1));
        pi2 = (-4 * pow(-1, k)) / ((2*k+1) * pow(239, 2*k+1));
        sum1 += pi1;
        sum2 += pi2;
    }
    return kahan(sum1, sum2, babken);
}
```

Use the backside, if needed

Problem 1 of 4

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Problem 2: Write a Java method `public static double[] expReg(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the exponent of an exponential regression and the second element being the amplitude. The exponential regression approximates the data points by a formula

$$y = a e^{mx},$$

where the exponent m and the amplitude a are computed as

$$m = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, a = \bar{y} - m\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the natural logarithm of y coordinates, $\overline{x^2}$ is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and natural logarithm of y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. For natural logarithm, use the method `double Math.log()`.

Both result elements are zeros, if at least one data element is non-positive.

```
public static double[] expReg(double[] data) {  
    double me, a;  
    double (xm, xm2, ym, xm2) = 0;  
    for (int k = 0; k < data.length; k++)  
    {  
        xm += k;  
        ym += Math.log(data[k]);  
        xm2 += pow(k, 2);  
    }  
    xm /= data.length;  
    xm2 = pow(xm, 2) / data.length;  
    ym /= data.length;  
    me = (xm * ym - xm2) / (xm2 - xm);  
    a = ym - me * xm;  
    double[] z = {me, a};  
    return z;  
}
```

Use the backside, if needed

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Problem 2 of 4

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Problem 3: Write a Java function `public static boolean isInside(double[][] vertex, double x, double y)` that takes as its argument a 2-by- n array of a convex polygon's vertex coordinates `double[][] vertex` – the x coordinates in the first row and y coordinates in the second row, and `double x` and `double y` coordinates of a point. It checks, if the point is inside the polygon.

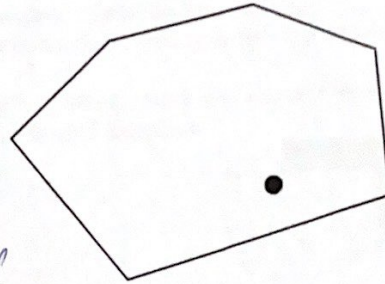
Assume and use a method `boolean toLeft(double x1, double y1, double x2, double y2, double x0, double y0)` that takes as its arguments coordinates of three points and returns `true`, if the third point (x_0, y_0) is in the left-hand side, when moving from the first point (x_1, y_1) to the second one (x_2, y_2) ; and `false`, if it is in the right-hand side.

```
public static boolean isInside ( ) {  
    double vertex.sort;
```

```
    for (int k=0; k < vertex.length/2; k++) {
```

```
        if (toLeft (vertex[k], vertex[k+1], x, y) == false) {  
            return false;  
        }  
    }
```

```
    return true;  
}
```



6 args needed

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Use the backside, if needed

Problem 3 of 4

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Problem 4: Write a Java method `public static void magicOdd(int[][] square)` that creates a magic square of an odd size using the following algorithm:

1. The number 1 goes in the middle of the top row; $\text{square}[0][1] = 1$;
2. All numbers are then placed one column to the right and one row up from the previous number;
3. Whenever the next number placement is above the top row, stay in the same column and place the number in the bottom row (note the place of 2 instead of the shaded location);
4. Whenever the next number placement is outside of the rightmost column, stay in the same row and place the number in the leftmost column (note the place of 3 instead of the shaded location);
5. When encountering an already filled-in square, place the next number directly below the previous number;
6. When the next number position is outside both a row and a column, place the number directly beneath the previous number (note the place of 7 instead of the shaded location).

	9	2	7
8	1	6	8
3	5	7	3
4	9	2	

```
public static void magicOdd(int[][] square) {
```

```
    square[0][1] = 1;
```

```
    int r = 0; int c = (square[0].length() / 2) + 1;
```

```
    row = square.length;
```

```
    square[0][(r/2)+1] = 1;
```

```
    for (int k=0; k < square.length; k++) {
```

```
        square[r-k][(r/2)+k] = 1+k;
```

```
        if (r-k < 0) {
```

```
            r = row - 1;
```

```
        }
```

```
        if (c > r/2) {
```

```
            c = 0;
```

```
        }
```

```
        if (r < 0 || c > r/2) {
```

```
            r += 2; c -= 1;
```

```
        }
```

```
    return square;
```

overwrite?

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Use the backside, if needed

Problem 4 of 4

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