

Section, Name and ID#:

AMERICAN UNIVERSITY OF ARMENIA
College of Science and Engineering
CS 120 Introduction to Object-Oriented Programming
MIDTERM EXAM

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED

Write down your section, name and ID# at the top of all used pages

Participation:

Problem 1: Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value π by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1}{2} * \frac{2}{3} + \frac{1*3}{2*4} * \frac{2}{5} + \frac{1*3*5}{2*4*6} * \frac{2}{7} + \dots \quad 1 + \frac{1}{6} + \frac{3}{40}$$

Recall that $n!!$ is the product of odd numbers from 1 to n , if n is odd; and is the product of even numbers from 2 to n , if n is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

```
float pi(int n) {
    float result = 1, result2 = 1, result3 = 1, result4 = 1;
    for (int k = 0; k <= n; k++) {
        if (k % 2 == 1) {
            result2 = result2 * k;
        }
        for (int i = 2; i <= k; i = i + 2) {
            result2 = result2 * i;
        }
        for (int j = 2; j <= k; j = j + 2) {
            result2 = result2 * j;
        }
        result = result * (result2 / (result2 * (2k+1)))
    } else if (k % 2 == 0) {
        result2 = 1 / (1 * (2k+1));
    }
    result = 2 * result;
    kahan(result, result2, compensation);
}
```

Use the backside, if needed

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Problem 2: Write a Java method `public static double[] lin(double[] data)` that takes as its argument an array of data points `double[] data`, and returns a two-element array – the first element being the slope of the linear regression and the second element being the intercept. The linear regression approximates the data points by the linear formula

$$y = kx + b,$$

where the slope k and the intercept b are computed as

$$k = \frac{\overline{xy} - \bar{x}\bar{y}}{\overline{x^2} - \bar{x}^2}, b = \bar{y} - k\bar{x}$$

Here \bar{x} is the mean of the x coordinates, \bar{y} is the mean of the y coordinates, $\overline{x^2}$ is the mean of the squares of the x coordinates, and \overline{xy} is the mean of the products of the x and y coordinates. Use the element indices of the array `double[] data` as x coordinates and the element values as y coordinates. You may assume and use the method `double mean(double[] a)`.

```

public static double[] lin(double[] data) {
    double[] xs = new double[data.length];
    for (int x = 0; x < data.length; x++) {
        int[] xs = new int[1];
        data[x] = x;
    }
    double meanofx = mean(xs);
    double meanofy = mean(data);
    double result = 0;
    for (int x = 0; x < data.length; x++) {
        result = result + (double[x] * x);
    }
    result = result / data.length;
    double meanofx2 = 0;
    for (int i = 0; i < xs.length; i++) {
        meanofx2 = meanofx2 + i;
    }
    meanofx2 = meanofx2 / xs.length;
    double slope = (result - (meanofx * meanofy)) / (meanofx2 - Math.pow(meanofx, 2));
    for (int i = 0; i < 2; i++) {
    lin[0] = (result - (meanofx * meanofy)) / (meanofx2 - Math.pow(meanofx, 2));
    slope = (result - (meanofx * meanofy)) / (meanofx2 - Math.pow(meanofx, 2));
    double b = meanofy - slope * meanofx;
    lin[0] = meanofy - lin[0] * meanofx;
    }
    return lin;
}

```

Use the backside, if needed

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Problem 3: Write a Java function `public static double area(double[][] vertex)` that takes as its argument a 2-by-n array of a convex polygon's vertex coordinates `double[][] vertex` - the x coordinates in the first row and y coordinates in the second row. It returns polygon's area as follows:

1. Divides the polygon into triangles by connecting the first vertex with the n^{th} and $(n+1)^{\text{st}}$ vertices;
2. Adds the areas of the constructed triangles using the formula $\text{area} = \sqrt{p(p-a)(p-b)(p-c)}$, where a, b and c are the sides and $p = (a + b + c) / 2$.

You may assume and use a method `double dist(double x1, double y1, double x2, double y2)` that takes as its arguments coordinates of two points and returns the distance between them.

```
public static double area(double[][] vertex) {
```

```
    for (int i = 0; i < 2; i++) {
```

```
        for (int j = 0; j < vertex[i].length; j++) {
```

$\begin{bmatrix} x_1 & x_2 & x_3 \\ y_1 & y_2 & y_3 \end{bmatrix}$

Let me explain how I will do it :)

So, we have 2 for's (I wrote it above), which read the elements of matrix.

We have x_0 and y_0 and other elements.

x_0 and y_0 are the first point.

So we have a function called `distance`. $\text{distance} = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$

We call this function and find all the distances from (x_0, y_0) to other points.

Then we also compute the distance from 2 successive points such as

(x_1, y_1) and (x_2, y_2) .

So, in case of 3 points we would have the first point with other two and the other two with each other.

Then, we simply compute p, p_1, p_2 $\text{first dist} + \text{sec} + \text{third}$

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Use the backside, if needed

and $\text{Area} = \sqrt{p(p - \text{first dist})(p - \text{sec})(p - \text{third})}$

For other triangles we have the same thing. First one is computed with the second successive points. So, $\text{Area} = \text{Area} + \text{the sum of areas of triangles}$.