

AMERICAN UNIVERSITY OF ARMENIA  
College of Science and Engineering  
CS 120 Introduction to Object-Oriented Programming  
**MIDTERM EXAM**

Date / Time:

Friday, March 17 2017 at 17:30

Duration:

2 hours

Attention:

**ANY TYPE OF COMMUNICATION IS STRICTLY PROHIBITED**

Write down your section, name and ID# at the top of all used pages

Participation:

**Problem 1:** Consider below a C++ function `float kahan(float num1, float num2, float& compensation)` that implements the *Kahan Summation Algorithm* for high-precision compensated summation of two float arguments `float num1` and `float num2`:

```
float kahan(float num1, float num2, float &compensation)
{
    float result;
    num2 -= compensation;
    result = num1 + num2;
    compensation = (result - num1) - num2;
    return result;
}
```

Using this function, write a C++ function `float pi(int n)` that computes the value  $\pi$  by the following formula:

$$\pi = 2 \sum_{k=0}^n \frac{(2k-1)!!}{(2k)!!(2k+1)} = \frac{2}{1*1} + \frac{1*2}{2*3} + \frac{1*3*2}{2*4*5} + \frac{1*3*5*2}{2*4*6*7} + \dots$$

Recall that  $n!!$  is the product of odd numbers from 1 to  $n$ , if  $n$  is odd; and is the product of even numbers from 2 to  $n$ , if  $n$  is even. The double factorial of non-positive numbers equals to 1 by definition.

The initial value of `float compensation` is 0.0.

```
float pi(int n) {
    result1 = 1; result2 = 1;
    for (i = 2; i <= n; i = i + 2)
        result1 = result1 * i;
    for (j = 1; j <= n; j = j + 2)
        result2 = result2 * j;
    pi = 2 * result1 / (result2 * (n+1));
    return pi;
}
```

for (k=1; k<=n; k++)

$$\pi = 2 * \frac{\text{odd}(2k-1)}{\text{even}(2k) * (2k+1)}$$

wrong logic

Kahan?

Use the backside, if needed

Problem 1 of 4

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