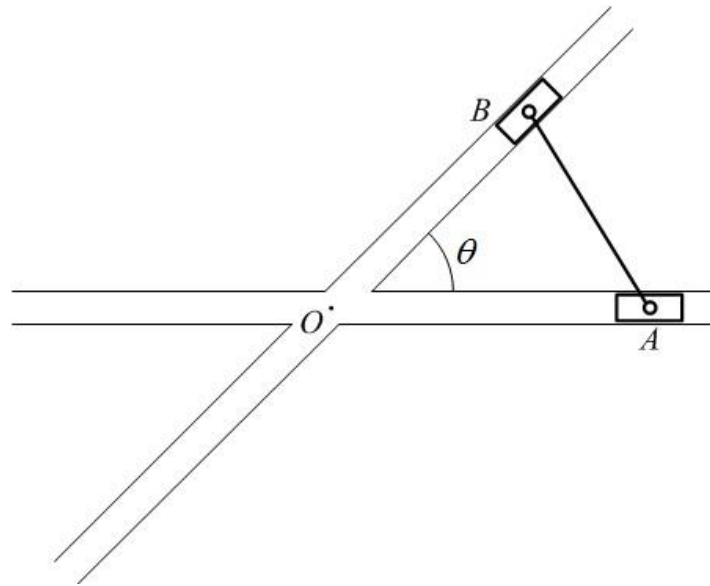


## AMSTR Course— Assignment 4

**Due date and time: Monday, 23 December 2019, 8:00AM**

**Question 1.** Points  $A$  and  $B$  are constrained to move in the plane on lines intersecting at angle  $\theta$ , Figure 1. Describe precisely the fixed and moving centrodes realizing the planar motion of body  $AB$  starting from a configuration like the one showed in the figure. Provide a rigorous mathematical proof that the instantaneous center traces the curves described by you.

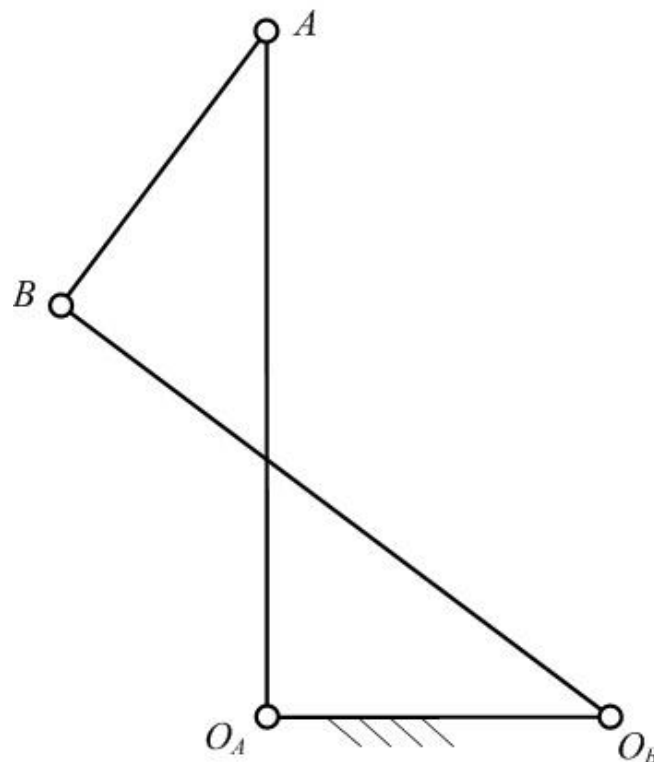


**Figure 1.**

**Question 2.** Points  $A$  and  $B$  are constrained to move in the plane on circles with centers  $O_A$  and  $O_B$  with  $|O_AA| = |O_BB|$ ,  $|O_AO_B| = |AB|$ , and  $|O_AA| > |AB|$ , Figure 2. Describe precisely the fixed and moving centrodes realizing the planar motion of body  $AB$  starting from a configuration like the one showed in the figure. Provide a rigorous mathematical proof that the instantaneous center traces the curves described by you. Plot the centrodes for the link-length parameters using a table of value given below.

**Question 3.** In the conditions of Question 2, let points  $O_A$  and  $A$  be fixed, while points  $O_B$  and  $B$  move on circles. Describe precisely the fixed and moving centrodes realizing the planar motion of the body  $O_BB$  starting from a configuration like the one showed in the figure. Provide a rigorous mathematical proof that the instantaneous center traces the curves described by you. Make a drawing (or a computer simulation) illustrating and explaining the rolling of the centrodes. Plot the centrodes for the

link-length parameters using a table of value given below.



**Figure 2.**

**Question 4 (bonus).** For each of Questions 1, 2 and 3: Does the rolling of the identified centrodes yield *all* possible configurations of the moving body allowed by the linkage? Prove your answer.

**Hint.** In all cases, the centrodes are relatively simple, familiar curves. The proofs required in Questions 1-3 can be made using simple planar geometry.

**Note.** You can get up to 100% of the mark for this homework by answering the first three questions, and up to 110% by answering all four.

Simulations can be performed in Matlab/Mathematica/Maple or CAD.

For **Question 2 and 3**,

$$|AB| = l_a$$

The value of  $l_a$  is given by first digit of your student ID/Matricola.

$$|OA_A| = l_b$$

$$k = 0.1 + (0.012)n$$

$$l_b = 1/k$$

Value of  $n$  is given below:

Nome	Cognome	n
Amrita	Suresh	1
Davide	Lanza	2
Ravi Kiran	Aggadi	3
Sai Santosh	Narra	4
Vignesh	Durai	5
Astha	Gupta	6
Ariel	Gjaci	7
Mugisha	Stanley	8