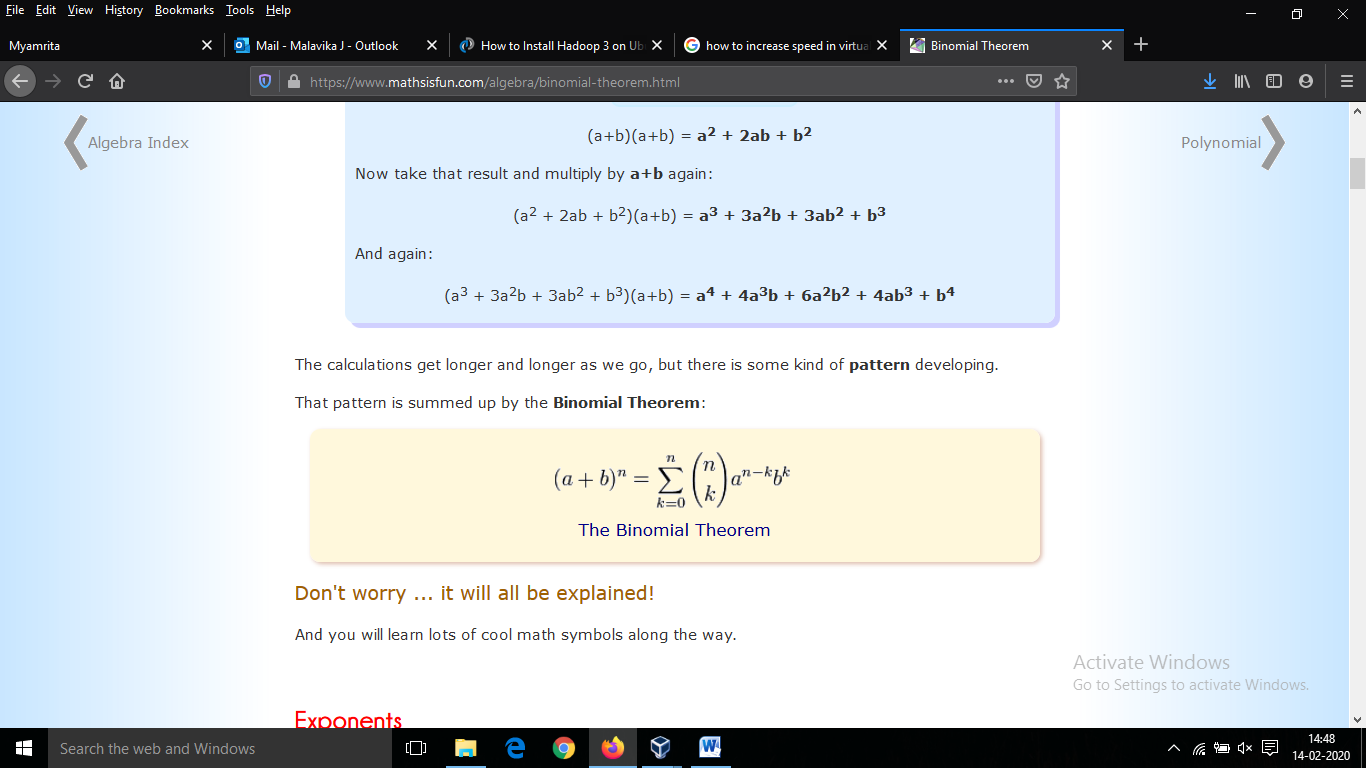
1. **a belongs to Zp. Prove that (a + p)n(mod p) =an(mod p)**

Using binomial theorem,



On applying this to (a + p)n(mod p)=an+pn  mod p

rest of the terms becomes 0 since(p mod p=0)

(a + p)n(mod p)=an+pn  mod p

=an mod p + pn mod p

=an  mod p + 0

=an  mod p

Hence proved.

2 ) Find the multiplicative inverse of all the elements in Z5 and Z11

Z5

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| 1 | 2 | 3 | 4 | 5 | 6 |
| 1 | 4 | 5 | 2 | 3 | 6 |

Z11

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 1 | 6 | 4 | 3 | 9 | 2 | 8 | 7 | 5 | 10 |

3) Determine the gcd of 56245 and 43159

Let a=56245 b=43159

56245=1\*43159+13086

43159=3\*13086+3901

13086=3\*3901+1383

3901=2\*1383+1135

1383=1\*1135+248

1135=4\*248+143

248=1\*143+105

143=1\*105+38

105=2\*38+29

38=1\*29+9

29=7\*9+2

9=4\*2+1

2=2\*1+0

ie; gcd=1,relatively prime

4) Compute phi(n) for 34 and 210

Based to Euler’s product formula

phi(34)=34\*(1-(1/3))

=81\*2/3

=54.

phi(210)=210\*(1-(1/2))

=1024\*1/2

=512.

5) Compute 3100 mod(31319)

e=100 =>26+25+22

30 mod 31319=3

32 mod 31319=9

34 mod 31319=81

38 mod 31319=6561

316 mod 31319=14418

332 mod 31319=21979

364 mod 31319=12185

3100 mod(31319)=12185\*21979\*81 mod 31319

=5346\*81 mod 31319

=25879.

PART B

1)Write a program to implement Extended Euclidean Algorithm and find multiplicative inverse for following values.

#include<iostream>

using namespace std;

int Exteuc(int a, int b, int \*x, int \*y)

{

if (a == 0)

{

\*x = 0, \*y = 1;

return b;

}

int x1, y1;

int gcd = Exteuc(b%a, a, &x1, &y1);

\*x = y1 - (b/a) \* x1;

\*y = x1;

return gcd;

}

int main()

{

int a, m;

cin>>a>>m;

int x, y;

int g = Exteuc(a, m, &x, &y);

if (g != 1)

cout << "\n Inverse does not exist. ";

else

{

int res = (x%m + m) % m;

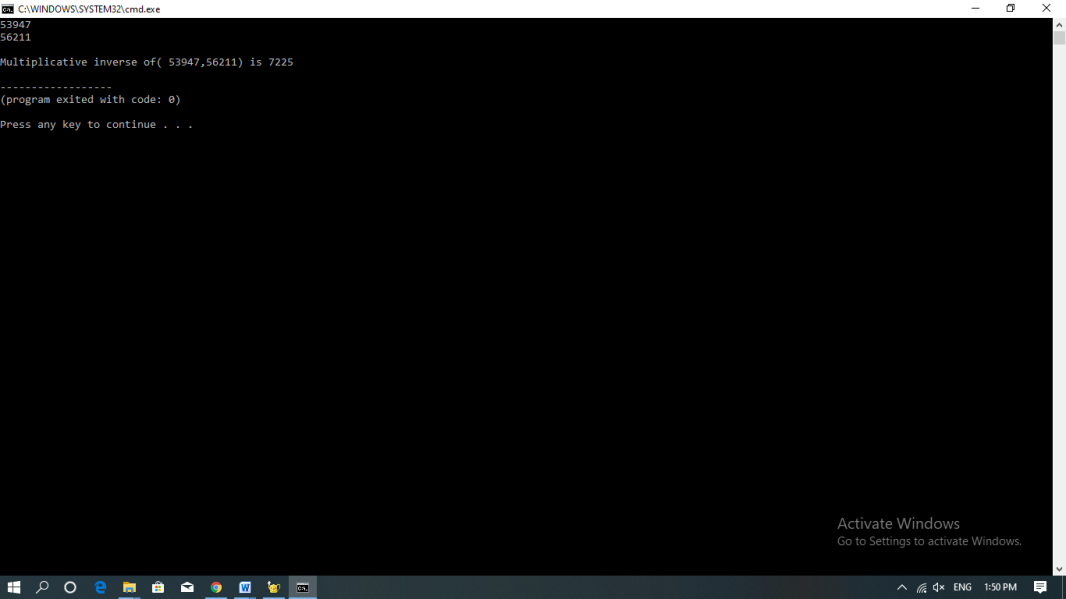
cout << "\nMultiplicative inverse of( "<<a<<","<<m<<") is "<< res;

}

return 0;

}

53947-1 mod 56211



19385-1 mod 431592.

