

Given Every human is mortal 1.  $\forall x \text{ human}(x) \rightarrow \text{mortal}(x)$   
 and Every mortal is alive 2.  $\forall y \text{ mortal}(y) \rightarrow \text{alive}(y)$   
 Formally Show Every human is alive  $\forall z \text{ human}(z) \rightarrow \text{alive}(z)$

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3. human(c)	ded method premise	} ded. method proof
4. human(c) $\rightarrow$ mortal(c)	1, ui	
5. mortal(c) $\rightarrow$ alive(c)	2, ui	
6. mortal(c)	3, 4, mp	
7. alive(c)	6, 5, mp	
8. human(c) $\rightarrow$ alive(c)	ded method 3-7	
9. $\forall z \text{ human}(z) \rightarrow \text{alive}(z)$	8, ug	

Premise 1.  $\forall x P(x) \rightarrow \forall y Q(x,y)$  premise

Show:  $\forall x \forall y P(x) \rightarrow Q(x,y)$

2.  $P(c) \rightarrow \forall y Q(c,y)$  1,  $\forall i$

3.  $P(c)$  Ded method premise

4.  $\forall y Q(c,y)$  2,3,  $\forall y$

5.  $Q(c,d)$  4,  $\forall i$

6.  $P(c) \rightarrow Q(c,d)$  Ded method 3-5

7.  $\forall y P(c) \rightarrow Q(c,y)$  6  $\forall y$

8.  $\forall x \forall y P(x) \rightarrow Q(x,y)$  7  $\forall x$

## Formal vs. (Informal) Proof

Deductive : proof that claims are entailed from our assumptions.

inductive reasoning

induction

Claim:  $n(n-1)+41$  is always prime. (yes if you generalize from a lot of natural examples)  
 $\hookrightarrow n^2 - n + 41 = 41^2$  when  $n=41$  not prime

1.

2.

3.

4.

5.

6.

all prime.

But not entailed.

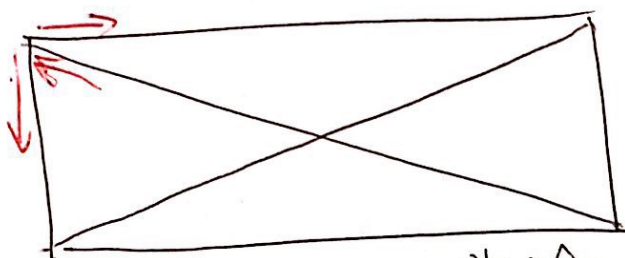
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\* Mathematical Induction is  
a deductive technique. \*

To prove or to refute?

Carl Witty

Claim : every odd natural number  $> 2$  is prime.



\* a complete tracing uses an even # of segments at every intersection except possibly the start and finish points



$\therefore$  traceable figures have at most 2 "odd intersections"

Trace in 1 line w/o re tracing?

No, by exhaustive consideration (hard to do)

