

$$T_H(n) = 2T_H(n-1) \quad \text{is homogeneous part}$$

$$r^n = 2r^{n-1}$$

$$r_1 = 2$$

$$r_2 = 1$$

(5 is not a root)

$$\text{so } T_H = c2^n$$

$$p(n) = n^2$$

Find $p(n)$

$$\text{Ans of } p(n) = n^m p'(n) s^n = n^2 (c_2 n^2 + c_1 n + c_0) 1^n = c_2 n^4 + c_1 n^3 + c_0 n^2$$

$$\text{Find } c_2, c_1, c_0 \text{ by plugging } p(n) \text{ into } T(n) = 2T(n-1) + n^2$$

$$c_2 n^4 + c_1 n^3 + c_0 n^2 = 2[c_2 (n-1)^2 + c_1 (n-1) + c_0] + n^2$$

$$\text{from } n^2: c_2 = 2c_2 + 1 \Rightarrow c_2 = -1$$

$$\text{from } n: c_1 = -4c_2 + 2c_1 = 4 + 2c_1 \Rightarrow c_1 = -4$$

$$\text{from } 1: \text{etc. find } c_0$$

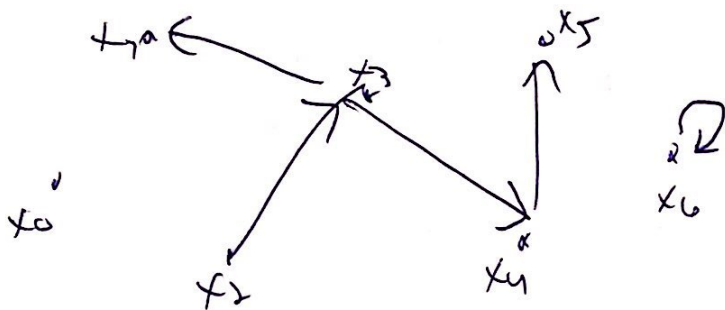
$$p(n) = -n^2 - 4n + c_0$$

$$T(n) = c2^n + (-n^2 - 4n + c_0)$$

then use base case to find c_0

Please read relevant textbook sections for relations & functions listed at top of hw6 assignment.

Relations A relation is a set of n -tuples, for arity n .
most common & useful case is $n=2$. (binary relation)
- easily drawn as a graph.



$\{(x_3, x_1), (x_2, x_3), (x_3, x_4),$
 $(x_4, x_5), (x_4, x_6)\}$

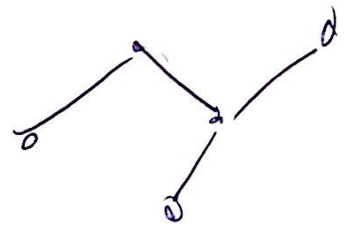
A binary relation $R(x,y)$ can be:

reflexive $\forall x \in D \quad R(x,x) \quad \leq$

irreflexive $\forall x \in D \quad \neg R(x,x) \quad <$

symmetric $\forall x \forall y \quad R(x,y) \rightarrow R(y,x)$

anti-symmetric $\forall x \forall y \quad R(x,y) \wedge R(y,x) \rightarrow x=y$
 "no faithful property"



transitive: $\forall x \forall y \forall z \quad R(x,y) \wedge R(y,z) \rightarrow R(x,z)$



A reflexive antisymmetric transitive relation is called a partial ordering.

A reflexive symmetric transitive relation (rst) is called an equivalence relation.