

# Equation of States of Nuclear Matter and Tidal deformation of Neutron Stars

by

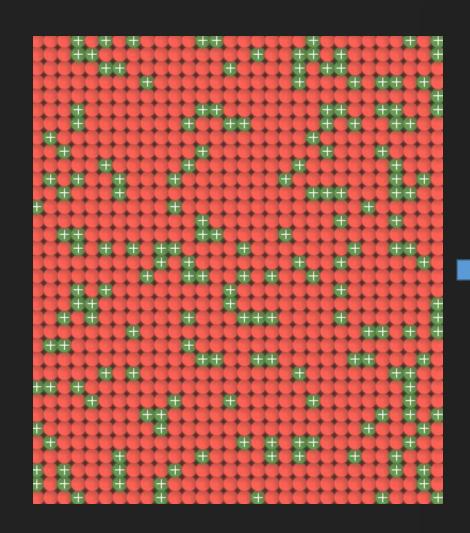
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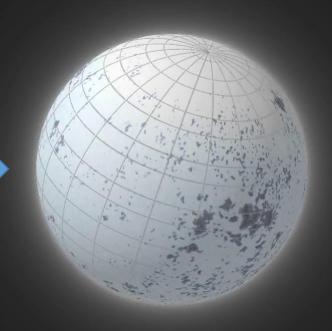
### **Equation of States of Nuclear Matter** *Nuclear Matter and Neutron Star?*



1993

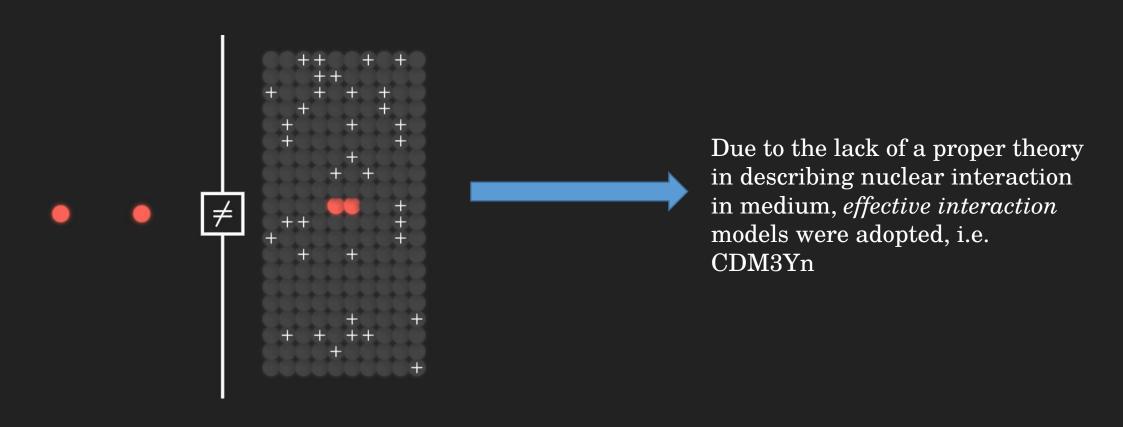


Tolman-Oppenheimer-Volkoff equation



# **Equation of States of Nuclear Matter** *Effective interactions*

• Two-body nucleon-nucleon interaction in medium is different with that for free NN

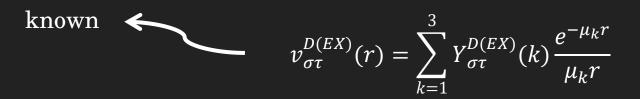


### Equation of States of Nuclear Matter CDM3Yn interactions

• CDM3Yn interaction has the form

$$v(n_b, r) = F_{00}(n_b)v_{00}(r) + F_{01}(n_b)v_{01}(r)(\sigma_1 \cdot \sigma_2) + F_{10}(n_b)v_{10}(r)(\tau_1 \cdot \tau_2) + F_{11}(n_b)v_{11}(r)(\sigma_1 \cdot \sigma_2)(\tau_1 \cdot \tau_2)$$

• The central terms are inherited from M3Y-Paris interaction



 $\underline{Asymmetry:} \ \delta = \frac{n_n - n_p}{n_b}$   $\underline{Polarization:} \Delta = \frac{n_{\uparrow \tau} - n_{\downarrow \tau}}{n_{\tau}}$ 

• The density-dependent form factors are

$$F_{\sigma\tau}(n_b) = C_{\sigma\tau}[1 + \alpha_{\sigma\tau}e^{-\beta_{\sigma\tau}n_b} + \gamma_{\sigma\tau}n_b]$$
 to be adjusted

### **Equation of States of Nuclear Matter** *Hartree-Fock energy*

• Total energy of system of nucleons

$$E_{HF} = \sum_{\boldsymbol{k}\sigma\tau} \frac{\hbar^{2}k^{2}}{2m_{\tau}} + \frac{1}{2} \sum_{\boldsymbol{k}\sigma\tau} \sum_{\boldsymbol{k}'\sigma'\tau'} \left[ \langle \boldsymbol{k}\sigma\tau, \boldsymbol{k}'\sigma'\tau' | v^{D} | \boldsymbol{k}\sigma\tau, \boldsymbol{k}'\sigma'\tau' \rangle + \langle \boldsymbol{k}\sigma\tau, \boldsymbol{k}'\sigma'\tau' | v^{EX} | \boldsymbol{k}'\sigma\tau, \boldsymbol{k}\sigma'\tau' \rangle \right]$$
Potential energy

• Baryonic pressure

Kinetic energy

$$P_b = n_b^2 \frac{\partial (E_{HF}/A)}{\partial n_b}$$

# Equation of States of Nuclear Matter $\beta$ -stable nuclear matter

• Aside from nucleons, leptons ( $e^-$  and  $\mu^-$ ) are also included, since

$$n \leftrightarrow p + e^- + \overline{\nu}_e$$

$$e^- \leftrightarrow \mu^- + \nu_e + \overline{\nu}_\mu$$

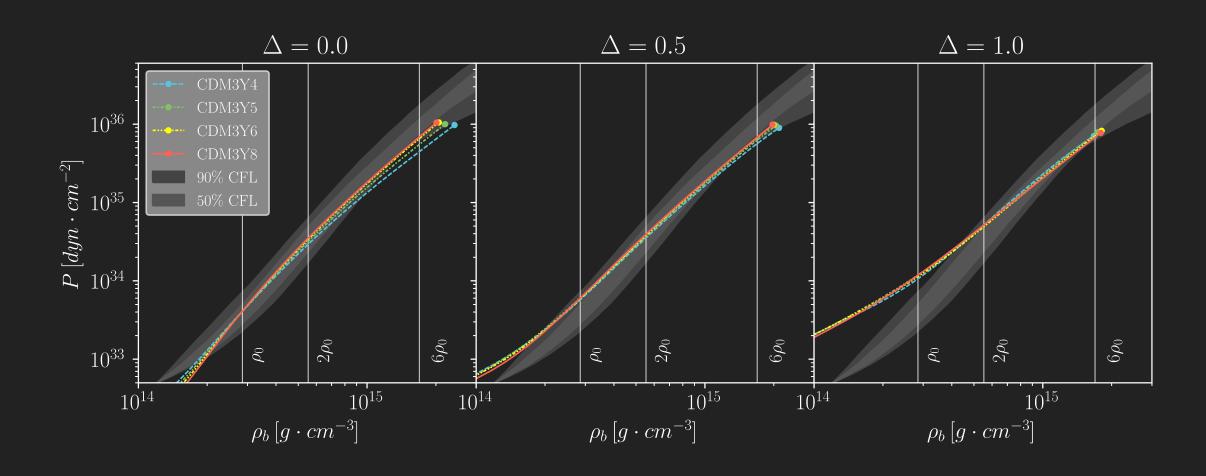
- **β-stable conditions** must be fulfilled
  - Charge balance

$$n_p = n_e + n_\mu$$

Energy balance

$$\mu_n - \mu_p = \mu_e = \mu_\mu$$

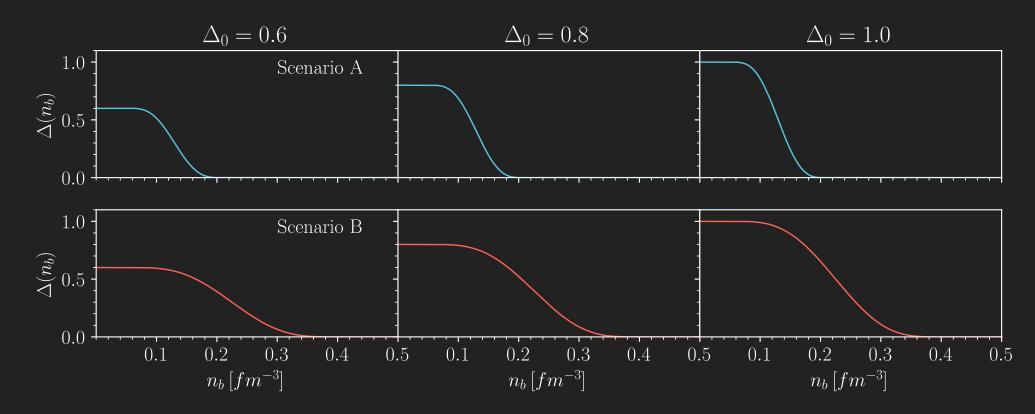
#### **Equation of States of Nuclear Matter** *Result*



### Tidal deformation of Neutron Star Neutron Star configuration

In a highly magnetized Neutron star (a magnetar), the polarization  $\Delta$  is expected to be

- high at lower density
- reduce to zero at high density



# Tidal deformation of Neutron Star Tolman-Oppenheimer-Volkoff equation

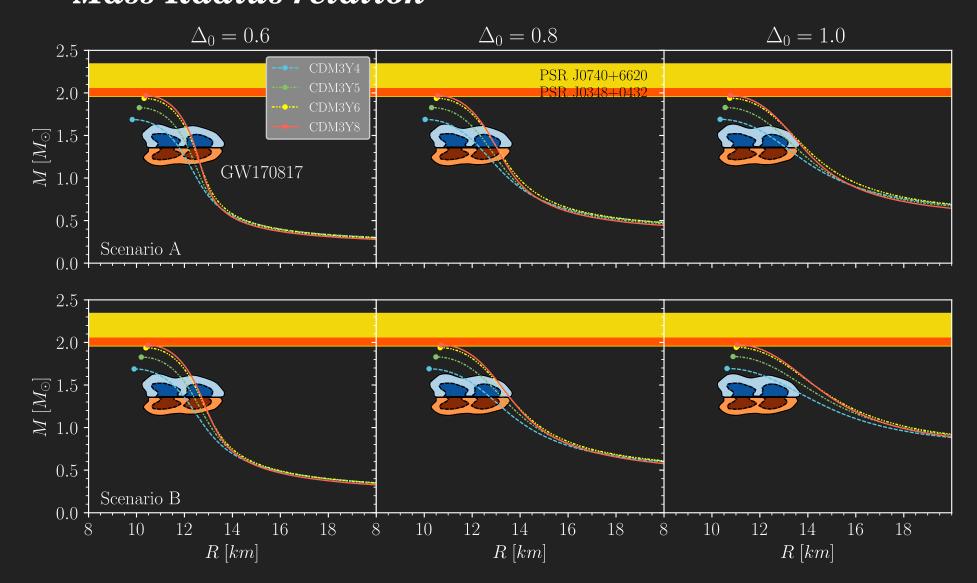
The macroscopic properties of neutron star are determined from the equation of states using the TOV equation

$$\frac{dP}{dr} = -\frac{G\rho\mathcal{M}}{r^2} \left(1 + \frac{P}{\rho c^2}\right) \left(1 + \frac{4\pi P r^3}{c^2 \mathcal{M}}\right) \left(1 - \frac{2G\mathcal{M}}{c^2 r}\right)^{-1}$$



Mass-Radius M(R)

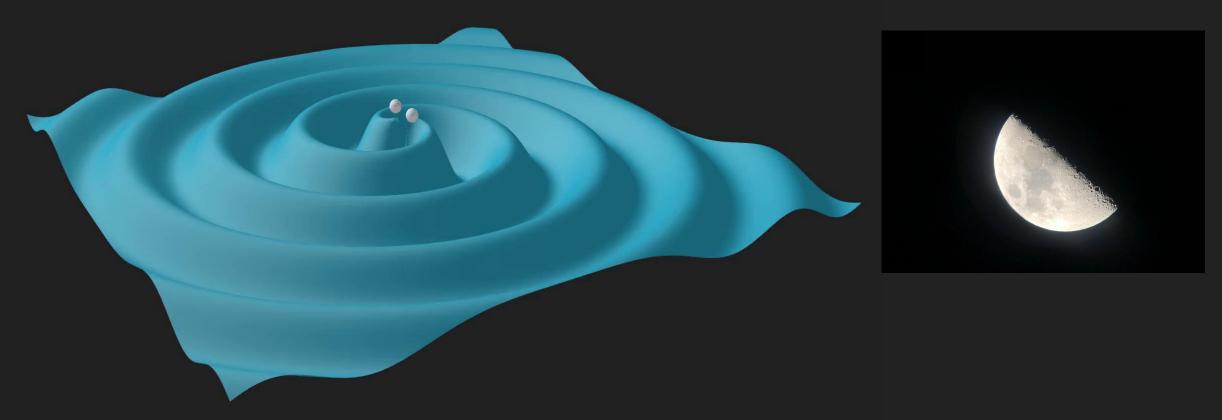
### Tidal deformation of Neutron Star Mass-Radius relation



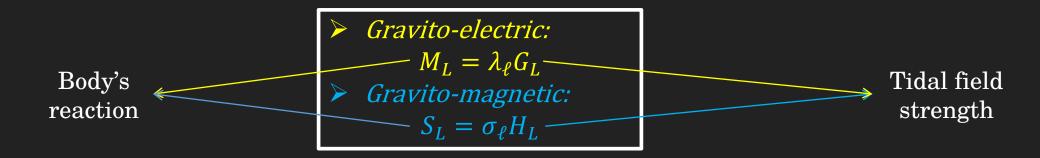
Only models with high values of K (CDM3Y6 and CDM3Y8) at partial polarization ( $\Delta$  < 1) are plausible

### Tidal deformation of Neutron Star Tidal effect in a binary system

In a binary system of neutron stars, one is subjected to strong tidal effect caused by the other

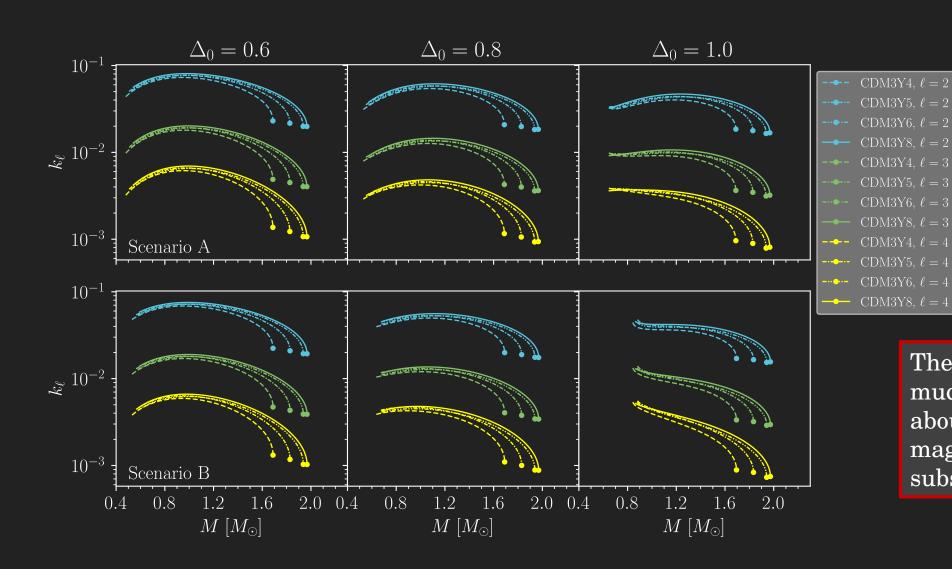


• The tidal properties of a neutron star are expressed in order  $\ell$  as



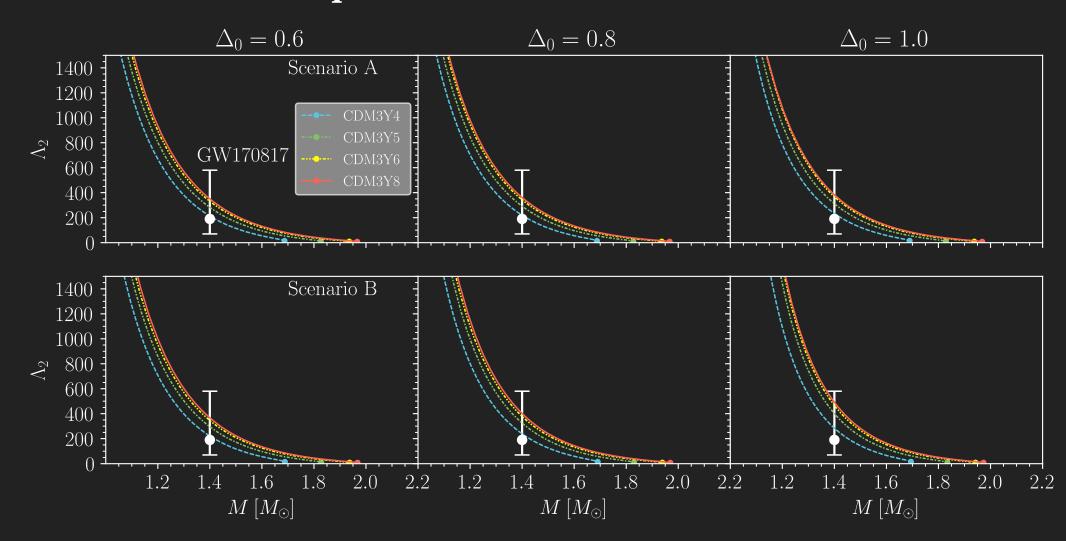
• Equivalently, they can also be described by the tidal Love numbers of order  $\ell$ 

$$k_{\ell} = \frac{1}{2} (2\ell - 1)!! \frac{G\lambda_{\ell}}{R^{2\ell+1}}$$
$$j_{\ell} = 4(2\ell - 1)!! \frac{G\sigma_{\ell}}{R^{2\ell+1}}$$

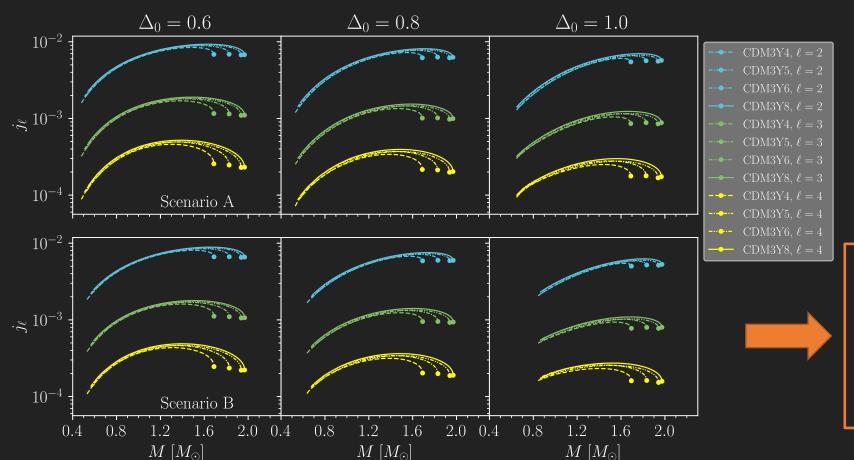


The second order  $(\ell = 2)$  is much more dominant, at about an order of magnitude larger than the subsequent order

### Tidal deformation of Neutron Star Dimensionless tidal parameter

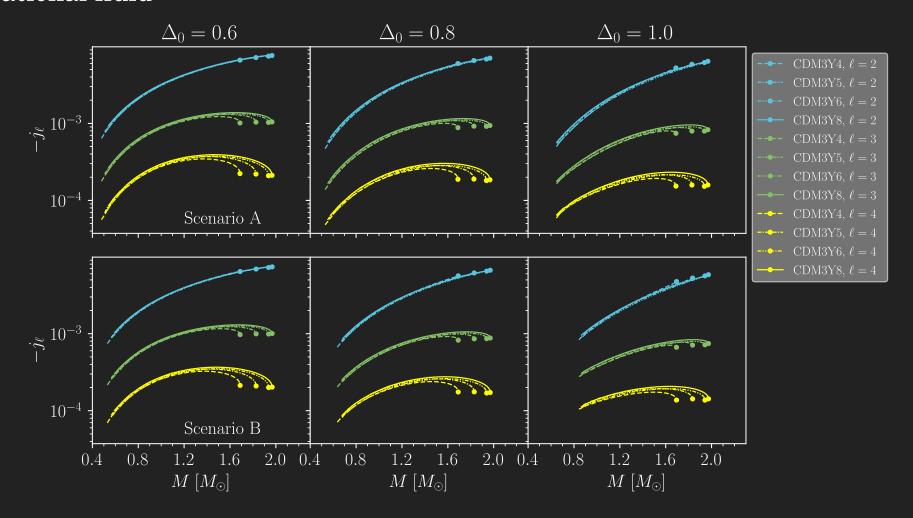


#### > Static fluid



The same trend is found in gravito-magnetic Love numbers. However, they appear to be 1 order of magnitude lower than their GE counterparts.

#### > Irrotational fluid



#### Conclusions

- The case of total polarization at the outer core and crust is ruled out as expected.
- Higher values of K are favored as only CDM3Y6 and CDM3Y8 come close to the lower mass limit of the heaviest pulsars observed.
- The tidal properties of the neutron star are also investigated with assumptions and up to fourth order in contribution, which returns a close result with those obtained in recent study.

### Thank you for your attention!