JIDT: An information-theoretic toolkit for studying the dynamics of complex systems

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Java Information Dynamics Toolkit (JIDT)

https://code.google.com/p/information-dynamics-toolkit/

JIDT provides a standalone, open-source (GPL v3 licensed) implementation of information-theoretic measures of information processing in complex systems, i.e. information storage, transfer and modification.

JIDT includes implementations:

- Principally for transfer entropy, mutual information, their conditional variants, active information storage etc;
- For both discrete and continuous-valued data;
- Using various types of estimators (e.g. Kraskov-Stögbauer-Grassberger, linear-Gaussian, etc.).

Java Information Dynamics Toolkit (JIDT)

JIDT is written in Java but directly usable in Matlab/Octave, Python, R, Julia, Clojure, etc.

JIDT requires almost zero installation.

JIDT is distributed with:

- A paper describing its design and usage;
 - J.T. Lizier, Frontiers in Robotics and AI 1:11, 2014; (arXiv:1408.3270)
- Full Javadocs;
- A suite of demonstrations, including in each of the languages listed above.

JIDT tutorial – Objectives

Participants will:

- Understand measures of information dynamics;
- Be able to obtain and install JIDT distribution;
- Understand and run sample scripts in their chosen environment;
- Be able to modify sample scripts for new analysis;
- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).

Introduction

Outline

- 2 Information dynamics
 - Information theory
 - The information dynamics framework
- Stimation techniques
- Overview of JIDT
- Demos
- 6 Exercise
- Wrap-up

Hi, I'm Joe ..

- My background.
- Why I developed an information-theoretic toolkit.

• Where are you from? Unis, other organisations?

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- Which languages/environments are you using, and how much coding experience do you have?

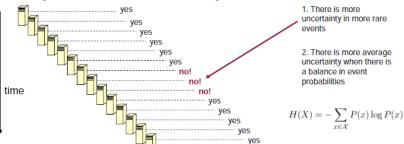
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- How familiar are you with information theory what measures do you know? Are you using it for analysis yet?

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- Which languages/environments are you using, and how much coding experience do you have?
- How familiar are you with information theory what measures do you know? Are you using it for analysis yet?
- What types of information-theoretic analysis do you have planned (perhaps with JIDT)?

Entropy

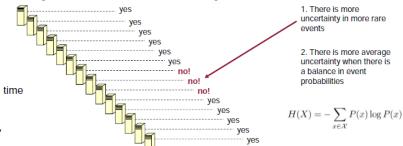
(Shannon) entropy is a measure of uncertainty. Intuitively: if we want to know the value of a variable, there is uncertainty in what that value is before we inspect it (measured in bits).

e.g. Is the web server cam.ac.uk running?



Sample entropy calculation

· e.g. Is the web server cam.ac.uk running?



Here we have p(yes) = 11/14, p(no) = 3/14 – what is H?

x = yes no	p(x)	$-\log_2 p(x)$	$-p(x)\log_2 p(x)$
yes	0.786	0.348	0.273
no	0.214	2.22	0.476
			H = 0.750 bits

Conditional entropy

Uncertainty in one variable X in the context of the known measurement of another variable Y.

Intuitively: how much uncertainty is there in X after we know the value of Y?

e.g. How uncertain are we about the web server is running if we know the IT guy is at lunch?

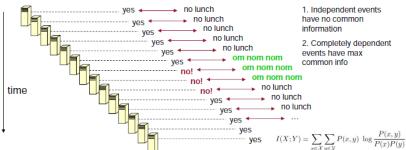
$$H(X|Y) = H(X,Y) - H(Y) = -\sum_{x \in X} \sum_{y \in Y} p(x,y) \log p(x|y)$$

Mutual information

Information is a measure of uncertainty reduction.

Intuitively: common information is the amount that knowing the value of one variable tells us about another.

· e.g. How much common info b/w if IT guy is at lunch and the web server running?



Information-theoretic quantities

Outline

Shannon entropy
$$H(X) = -\sum_{x} p(x) \log_2 p(x)$$

$$= \langle -\log_2 p(x) \rangle$$
Conditional entropy
$$H(X|Y) = -\sum_{x,y} p(x,y) \log_2 p(x|y)$$
Mutual information (MI)
$$I(X;Y) = H(X) + H(Y) - H(X,Y)$$

$$= \sum_{x,y} p(x,y) \log_2 \frac{p(x|y)}{p(x)}$$

$$= \left\langle \log_2 \frac{p(x|y)}{p(x)} \right\rangle$$
Conditional MI
$$I(X;Y|Z) = H(X|Z) + H(Y|Z) - H(X,Y|Z)$$

$$= \left\langle \log_2 \frac{p(x|y,z)}{p(x|z)} \right\rangle$$

Local measures

We can write local (or point-wise) information-theoretic measures for specific observations/configurations $\{x, y, z\}$:

$$h(x) = -\log_2 p(x),$$
 $i(x; y) = \log_2 \frac{p(x|y)}{p(x)}$
 $h(x|y) = -\log_2 p(x|y),$ $i(x; y|z) = \log_2 \frac{p(x|y, z)}{p(x|z)}$

- We have $H(X) = \langle h(x) \rangle$ and $I(X; Y) = \langle i(x; y) \rangle$, etc.
- If X, Y, Z are time-series, local values measure dynamics over time.

What can we do with these measures in ALife/CI?

- Measure the diversity in agent strategies (Miramontes, 1995; Prokopenko et al., 2005).
- Measure long-range correlations as we approach a phase-transition (Ribeiro et al., 2008).
- Feature selection for machine learning (Wang et al., 2014).
- Quantify the information held in a response about a stimulus, and indeed about specific stimuli (DeWeese and Meister, 1999).
- Measure the common information in the behaviour of two agents (Sperati et al., 2008).
- Guide self-organisation using these measures (Prokopenko et al., 2006).
- . . .
- \rightarrow Information theory is useful for answering specific questions about information content, shared information, and where and to what extent information about some variable is mirrored.

We talk about computation as:

- Memory
- Signalling
- Processing

Distributed computation is any process involving these features:

- Time evolution of cellular automata
- Information processing in the brain
- Gene regulatory networks computing cell behaviours
- Flocks computing their collective heading
- Ant colonies computing the most efficient routes to food
- The universe is computing its own future!

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Idea: quantify computation via:

- Information storage
- Information transfer
- Information modification

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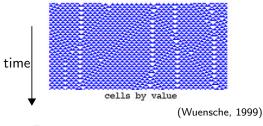
- Time evolution of cellular automata
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General idea: by quantifying intrinsic computation in the language it is normally described in, we can understand how nature computes and why it is complex.

Motivating example: cellular automata



CAs: simple dynamical systems; known causal structure and rules.



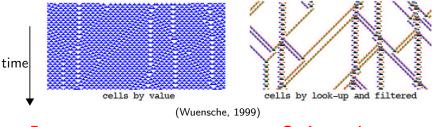
Emergent structure:

- Domain, blinkersParticles
- - Gliders, domain walls
- Collisions

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Emergent structure:

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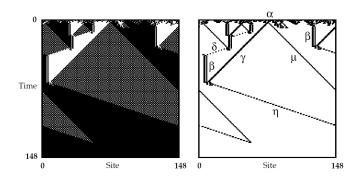
Conjectured to represent:

- Information storageInformation transfer
- Information modification

It's easy to identify which components store, transfer and modify information in a PC – it's not so easy in complex systems.



Motivating example: cellular automata



Mitchell et al. (1994, 1996) used GAs to evolve CAs to solve specific computational tasks.

In attempting the density classification task (above), the CA uses:

- ullet domains and blinkers eta to store information;
- gliders γ , η to transfer information;
- glider collisions e.g. $\gamma + \beta \rightarrow \eta$ to modify/process information.



We talk about computation as:

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Information dynamics

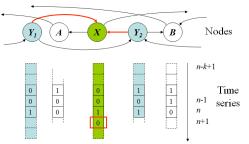
- Information storage
- Information transfer
- Information modification

Key properties of the information dynamics approach:

- A focus on individual operations of computation rather than overall complexity;
- Alignment with descriptions of dynamics in specific domains;
- A focus on the local scale of info dynamics in space-time;
- Information-theoretic basis directly measures computational quantities:
 - Captures non-linearities;
 - Is applicable to, and comparable between, any type of time-series.



Key question: how is the next state of a variable in a complex system **computed**?

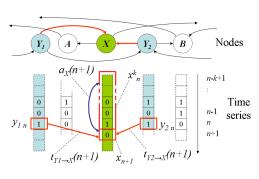


Q: Where does the information in x_{n+1} come from, and how can we measure it?

Q: How much was stored, how much was transferred, can we partition them or do they overlap?

Complex system as a multivariate time-series of states

Studies computation of the next state of a target variable in terms of information storage, transfer and modification: (Lizier et al., 2008, 2010, 2012)

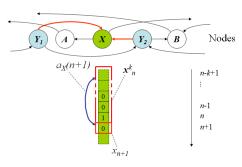


The measures examine:

- State updates of a target variable;
- Dynamics of the measures in space and time.

Active information storage (Lizier et al., 2012)

How much information about the next observation X_{n+1} of process X can be found in its past state $\mathbf{X}_{\mathbf{n}}^{(\mathbf{k})} = \{X_{n-k+1} \dots X_{n-1}, X_n\}$?



Active information storage:

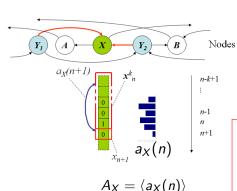
Nodes
$$A_X = I(X_{n+1}; \mathbf{X}_n^{(\mathbf{k})})$$

$$= \left\langle \log_2 \frac{p(x_{n+1}|\mathbf{x}_n^{(\mathbf{k})})}{p(x_{n+1})} \right\rangle$$

Average information from past state that is in use in predicting the next value.

Active information storage (Lizier et al., 2012)

How much information about the next observation X_{n+1} of process X can be found in its past state $\mathbf{X_n^{(k)}} = \{X_{n-k+1} \dots X_{n-1}, X_n\}$?



Local active information storage:

$$a_X(n) = \log_2 \frac{p(x_{n+1}|\mathbf{x}_n^{(k)})}{p(x_{n+1})}$$

Information from a specific past state that is in use in predicting the specific next value.

Active information storage:

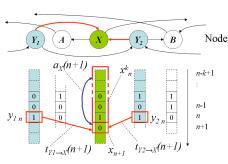
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Average information from past state that is in use in predicting the next value.

Information transfer

How much information about the state transition $\mathbf{X}_{\mathbf{n}}^{(\mathbf{k})} \to X_{n+1}$ of X can be found in the past state $\mathbf{Y}_{\mathbf{n}}^{(\mathbf{l})}$ of a source process Y?



Transfer entropy: (Schreiber, 2000)

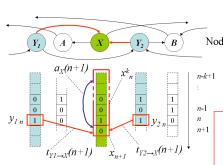
$$T_{Y \to X} = I(\mathbf{Y}_{\mathbf{n}}^{(1)}; X_{n+1} | \mathbf{X}_{\mathbf{n}}^{(k)})$$
$$= \left\langle \log_2 \frac{\rho(x_{n+1} | \mathbf{x}_{\mathbf{n}}^{(k)}, \mathbf{y}_{\mathbf{n}}^{(l)}))}{\rho(x_{n+1} | \mathbf{x}_{\mathbf{n}}^{(k)})} \right\rangle$$

Average info from source that helps predict next value in context of past.

Storage and transfer are complementary: $H_X = A_X + T_{Y \to X} + \text{higher order terms}$

Information transfer

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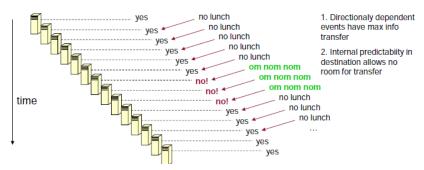
Local transfer entropy: (Lizier et al., 2008) $t_{Y \to X}(n) = \log_2 \frac{p(x_{n+1}|\mathbf{x}_n^{(k)}, \mathbf{y}_n^{(l)}))}{p(x_{n+1}|\mathbf{x}_n^{(k)}))}$

Information from a specific observation about the specific next value.

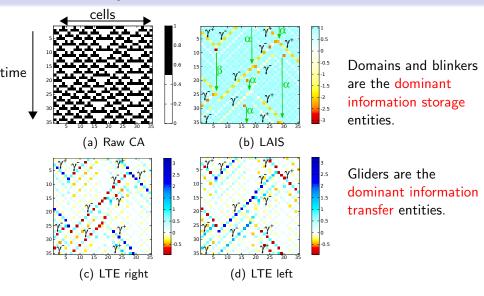
Information transfer

Transfer entropy measures directed coupling between time-series. Intuitively: the amount of information that a source variable tells us about a destination, in the context of the destination's current state.

e.g. How much does knowing the IT guy is at lunch tell us about the web server running, given its previous state?

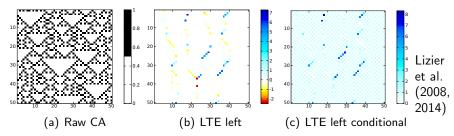


Information dynamics in CAs



Other transfer entropy characteristics

TE can be made conditional $T_{Y \to X|Z} = I(\mathbf{Y}_{\mathbf{n}}^{(\mathbf{l})}; X_{n+1} \mid \mathbf{X}_{\mathbf{n}}^{(\mathbf{k})}, \mathbf{Z}_{\mathbf{n}}^{(\mathbf{m})})$ or multivariate $T_{Y \to X|Z} = I(\{\mathbf{Y}_{\mathbf{n}}^{(\mathbf{l})}, \mathbf{Z}_{\mathbf{n}}^{(\mathbf{m})}\}; X_{n+1} \mid \mathbf{X}_{\mathbf{n}}^{(\mathbf{k})})$ (Lizier et al., 2008, 2010, 2011)



Computed over delay u as $T_{Y\to X|Z}=I(\mathbf{Y}_{\mathbf{n}-\mathbf{u}+\mathbf{1}}^{(\mathbf{l})};X_{n+1}\mid\mathbf{X}_{\mathbf{n}}^{(\mathbf{k})})$ (Wibral et al., 2013).

Discrete: plug-in estimator

For discrete variables x and y, to compute H(X, Y)

- **1** estimate: $p(x,y) = \frac{\text{count}(X=x,Y=y)}{N}$, where N is our sample size;
- ② plug-in each estimated PDF to H(X, Y) to get $\hat{H}(X, Y)$

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Bias: expected offset of estimated value from a finite sample set from the true underlying value of the measure. There are several available bias correction techniques.

Variance: variance in estimated values of the measure (from a finite sample set) around the expected value.

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A simple way to handle continuous variables is to discretise or bin them.

Continuous variables → Differential entropy

Differential entropy:

$$H_D(X) = -\int_{S_X} f(x) \log f(x) dx$$

for PDF f(x), where S_X is the set where f(x) > 0.

Evaluate all measures as sums and differences of $H_D(X)$ terms.

The properties of $H_D(X)$ are slightly odd ... however, the properties of $I_D(X;Y)$ are the same as for discrete variables.

JIDT includes 3 estimation methods for differential entropy based MIs (and conditional MIs) ...

Gaussian model

If a multivariate \mathbf{X} (of d dimensions) is Gaussian distributed (Cover and Thomas, 1991):

$$H(\mathbf{X}) = rac{1}{2} \ln \left[(2\pi e)^d \mid \Omega_{\mathbf{X}} \mid
ight]$$

(in *nats*) where $\mid \Omega_{\mathbf{X}} \mid$ is the determinant of the $d \times d$ covariance matrix $\Omega_{\mathbf{X}} = \overline{\mathbf{X}} \overline{\mathbf{X}}^T$.

Any measure is computed as sums and differences of these joint entropies.

Pros: fast $(O(Nd^2))$, parameter free Cons: subject to the linear-model assumption

Kernel estimation

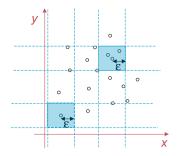
Estimate PDFs with a *kernel function* Θ , measuring "similarity" between pairs of samples $\{x_n, y_n\}$ and $\{x_{n'}, y_{n'}\}$ using a resolution or *kernel width* r.

E.g.:
$$\hat{p}_r(x_n, y_n) = \frac{1}{N} \sum_{n'=1}^N \Theta\left(\left|\begin{pmatrix} x_n - x_{n'} \\ y_n - y_{n'} \end{pmatrix}\right| - r\right).$$

By default Θ is the step kernel $(\Theta(x > 0) = 0, \ \Theta(x \le 0) = 1)$, and the norm $|\cdot|$ is the maximum distance.

Pros: model-free (captures non-linearities)
Cons: sensitive to r, is biased, less time-efficient (though can be reduced to $O(N \log N)$).

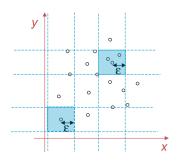
Estimating p(x, y), p(x) and p(y)



Kernel estimation

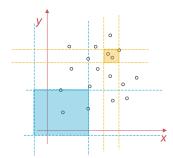
- Fixed width $r = \epsilon$
- MI: "How does knowing x within r help me predict y within r?"

Estimating p(x, y), p(x) and p(y)



Kernel estimation

- Fixed width $r = \epsilon$
- MI: "How does knowing x within r help me predict y within r?"



Kraskov (KSG) technique (Kraskov et al., 2004)

- Dynamic width r and bias correction
- MI: "How does knowing x within the K neasrest neighbours in the joint space help me predict y?"

KSG estimators (Kraskov et al., 2004)

Improve on box-kernel estimation with lower bias via:

- Harnessing Kozachenko-Leonenko entropy estimators;
- Using nearest-neighbour counting, with a fixed number K of neighbours in the full joint space.

KSG estimators (Kraskov et al., 2004)

Improve on box-kernel estimation with lower bias via:

- Harnessing Kozachenko-Leonenko entropy estimators;
- Using nearest-neighbour counting, with a fixed number K of neighbours in the full joint space.

There are two algorithms; algorithm 1 gives:

$$I^{(1)}(X;Y) = \psi(K) - \langle \psi(n_x+1) + \psi(n_y+1) \rangle + \psi(N),$$

(in *nats*) where ψ denotes the digamma function. Extensions to conditional MI are available (Frenzel and Pompe, 2007; Gomez-Herrero et al., 2010; Wibral et al., 2014).

Pros: model-free, bias corrected, best of breed in terms of data efficiency and accuracy, and is effectively parameter free (w.r.t K).

Cons: less time-efficient (though fast nearest neighbour searching reduces this to $O(KN \log N)$).

Why JIDT?

JIDT is unique in the combination of features it provides:

- Large array of measures, including all conditional/multivariate forms of the transfer entropy, and complementary measures such as active information storage.
- Wide variety of estimator types and applicability to both discrete and continuous data

Measure-estimator combinations

As of V1.2 distribution:

Measure		Discrete	Continuous estimators			
Name	Notation	estimator	Gaussian	Box-Kernel	Kraskov et al.(KSG)	Permutation
Entropy	H(X)	√	√	√	*	
Entropy rate	$H_{\mu X}$	√	Use two multivariate entropy calculators			
Mutual information (MI)	I(X;Y)	√	√	√	✓	
Conditional MI	$I(X; Y \mid Z)$	√	√		✓	
Multi-information	I(X)	√		√"	√"	
Transfer entropy (TE)	$T_{Y \to X}$	√	√	√	✓	√ "
Conditional TE	$T_{Y \to X Z}$	√	√ u		√"	
Active information storage	A_X	√	√ u	√ u	√"	
Predictive information	EX	√	√ u	√ u	√ "	
Separable information	S_X	✓				

Why JIDT?

JIDT is unique in the combination of features it provides:

- Large array of measures, including all conditional/multivariate forms of the transfer entropy, and complementary measures such as active information storage.
- Wide variety of estimator types and applicability to both discrete and continuous data
- Local measurement for all estimators;
- Statistical significance calculations for MI, TE;
- No dependencies on other installations (except Java);
- Lots of demos and information on website/wiki:
 - https://code.google.com/p/information-dynamics-toolkit/

Why implement in Java?

The Java implementation of JIDT gives us several fundamental features:

- Platform agnostic, requiring only a JVM;
- Object-oriented code, with a hierachical design to interfaces for each measure, allowing dynamic swapping of estimators for the same measure;
- JIDT can be directly called from Matlab/Octave, Python, R,
 Julia, Clojure, etc, adding efficiency for higher level code;
- Automatic generation of Javadocs.

Installation

- Download the latest full distribution from https://code.google.com/p/information-dynamics-toolkit/wiki/Downloads or http://bit.ly/jidt-download
- ② Unzip it to your prefered location for the distribution
- To be able to use it, you will need the infodynamics.jar on your classpath.

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That's it!

Installation – caveats

- You'll need a JRE installed (Version ≥ 6)
 - Should come automatically with Matlab/Octave/Python-JPype installation
- You need ant if you want to rebuild the project using build.xml
- You need junit if you want to run the unit tests
- Additional preparation may be required to use JIDT in GNU Octave or Python ...

Check that your environment works

Java:

• Run demos/java/example1TeBinaryData.sh or .bat

Matlab/Octave:

- For Octave version < 3.8, first follow steps on the wiki, including installing octave-java from octave-forge.
- Q Run demos/octave/example1TeBinaryData.m

Python:

- Install jPype to connect Python to Java
- ② Run demos/python/example1TeBinaryData.py

In case of issues, see the wiki pages on Non-Java environments or the Instructor.

Contents of distribution

- license-gplv3.txt GNU GPL v3 license;
- infodynamics.jar library file;
- Documentation
- Source code in java/source folder
- Unit tests in java/unittests folder
- build.xml ant build script
- Demonstrations of the code in demos folder.

Documentation

Included in the distribution:

- readme.txt;
- InfoDynamicsToolkit.pdf a pre-print of the publication introducing JIDT;
- javadocs folder documents the methods and various options for each estimator class;
- PDFs describing each demo in the demos folder;

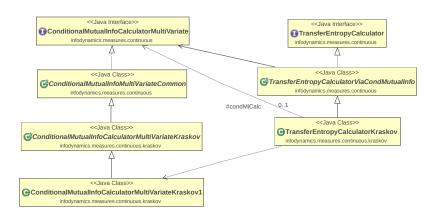
Also see:

- The wiki pages on the JIDT website
- This presentation! (via JIDT wiki)
- Our email discussion list jidt-discuss on Google groups.

Source code structure

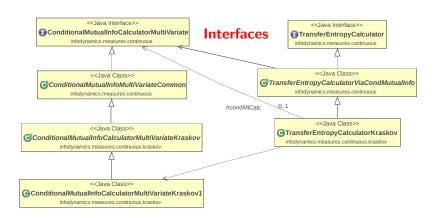
Source code at java/source is organised into the following Java packages (mapping directly to subdirectories):

- infodynamics.measures
 - infodynamics.measures.discrete for discrete data;
 - infodynamics.measures.continuous for continuous data
 - top level: Java interfaces for each measure, then
 - a set of sub-packages (gaussian, kernel, kozachenko, kraskov and symbolic) containing implementations of such estimators for these interfaces.
 - infodynamics.measures.mixed experimental discrete-to-continuous MI calculators
- infodynamics.utils utility functions
- infodynamics.networkinference higher-level algorithms



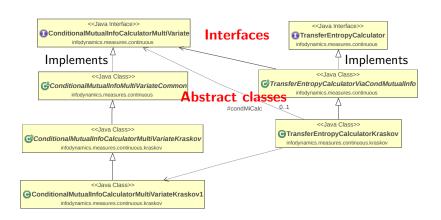
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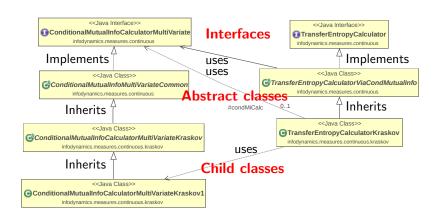
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▶ Return to JIDT contents

Demos

JIDT is ditributed with the following demos:

- Simple Java Demos
 - Mirrored in Matlab/Octave, Python, R, Julia, Clojure.
- Recreation of Schreiber's original transfer entropy examples;
- Information dynamics in Cellular Automata;
- Detecting interaction lags;
- Interregional coupling;
- Behaviour of null/surrogate distributions;

All have documentation provided to help run them.

Simple Java Demos

There are 8 demo scripts here highlighting different data types and estimation techniques.

We'll walk through:

- Example 1 a typical calling pattern on discrete data; and
- Example 4 a typical calling pattern on continuous data.

These examples use transfer entropy calculators, but note that the general paradigm for all calculators is the same.

Simple Demo 1 - Discrete Data

Open:
demos/java/infodynamics/demos/Example1TeBinaryData.java
OR
demos/octave/Example1TeBinaryData.m
OR
demos/python/Example1TeBinaryData.py
that you ran earlier

Simple Demo 1 - Discrete Data

Open:

demos/java/infodynamics/demos/Example1TeBinaryData.java
OR
demos/octave/Example1TeBinaryData.m
OR
demos/python/Example1TeBinaryData.py
that you ran earlier

1. Run it again

Simple Demo 1 - Discrete Data

Open:

demos/java/infodynamics/demos/Example1TeBinaryData.java
OR
demos/octave/Example1TeBinaryData.m

OR demos/python

demos/python/Example1TeBinaryData.py
that you ran earlier

- 1. Run it again
- 2. Observe how the classpath is pointed to infodynamics.jar:
 - Java: java command line in .sh/.bat (or in IDE);
 - Matlab/Octave: javaaddpath() statement;
 - Python: startJVM() statement.



Simple Java Demo 1 – Discrete Data

3. Examine the code (excerpt from .java file below)

```
int arrayLengths = 100;
  RandomGenerator rg = new RandomGenerator();
  // Generate some random binary data:
  int[] sourceArray = rg.generateRandomInts(
      arrayLengths, 2);
  int[] destArray = new int[arrayLengths];
  destArray[0] = 0;
  System.arraycopy(sourceArray, 0, destArray, 1,
      arrayLengths - 1);
  // Create a TE calculator and run it:
  TransferEntropyCalculatorDiscrete teCalc = new
      TransferEntropyCalculatorDiscrete(2, 1);
  teCalc.initialise();
10
  teCalc.addObservations(sourceArray, destArray);
11
  double result = teCalc.
12
      computeAverageLocalOfObservations();
```

Simple Java Demo 1 – Discrete Data

```
int arrayLengths = 100;
    RandomGenerator rg = new RandomGenerator();
    // Generate some random binary data:
    int[] sourceArray = rg.generateRandomInts(arrayLengths, 2);
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    destArray[0] = 0;
    System.arraycopy(sourceArray, 0, destArray, 1, arrayLengths - 1);
       Create a TE calculator and run it:
    TransferEntropyCalculatorDiscrete teCalc = new TransferEntropyCalculatorDiscrete
          (2, 1);
10
    teCalc.initialise():
    teCalc.addObservations(sourceArray, destArray);
11
12
    double result = teCalc.computeAverageLocalOfObservations();
```

- 4. Note: Discrete data represented as int[] arrays:
 - with values in the range 0...base 1, where e.g. base=2 for binary.
 - ② for time-series measures, the array is indexed by time.
 - for multivariate time-series, we use int[][] arrays, indexed first by time then variable number.

```
int arrayLengths = 100;
    RandomGenerator rg = new RandomGenerator();
    // Generate some random binary data:
    int[] sourceArray = rg.generateRandomInts(arrayLengths, 2);
    int[] destArray = new int[arrayLengths];
6
    destArray[0] = 0;
    System.arraycopy(sourceArray, 0, destArray, 1, arrayLengths - 1);
       Create a TE calculator and run it:
    TransferEntropyCalculatorDiscrete teCalc = new TransferEntropyCalculatorDiscrete
          (2, 1);
    teCalc.initialise():
10
11
    teCalc.addObservations(sourceArray, destArray);
12
    double result = teCalc.computeAverageLocalOfObservations();
```

- Construct the calculator, providing parameters
 - Always check Javadocs for which parameters are required.
 - **9** Here the parameters are the number of possible discrete symbols per sample (2, binary), and history length for TE (k = 1).
 - **3** Constructor syntax is different for Matlab/Octave/Python.

```
int arrayLengths = 100;
    RandomGenerator rg = new RandomGenerator();
    // Generate some random binary data:
    int[] sourceArray = rg.generateRandomInts(arrayLengths, 2);
    int[] destArray = new int[arrayLengths];
    destArray[0] = 0;
    System.arraycopy(sourceArray, 0, destArray, 1, arrayLengths - 1);
    // Create a TE calculator and run it:
    TransferEntropyCalculatorDiscrete teCalc = new TransferEntropyCalculatorDiscrete
         (2.1):
    teCalc.initialise():
10
    teCalc.addObservations(sourceArray, destArray);
11
12
    double result = teCalc.computeAverageLocalOfObservations();
```

- Initialise the calculator prior to:
 - use, or
 - **2** re-use (e.g. looping back from line 12 back to line 10 to examine different data).
 - 3 This clears PDFs ready for new samples.

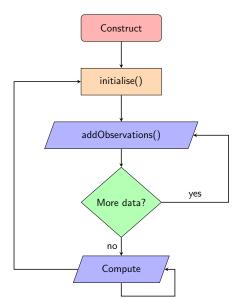
```
int arrayLengths = 100:
    RandomGenerator rg = new RandomGenerator();
    // Generate some random binary data:
    int[] sourceArray = rg.generateRandomInts(arrayLengths, 2);
    int[] destArray = new int[arrayLengths];
    destArray[0] = 0;
    System.arraycopy(sourceArray, 0, destArray, 1, arrayLengths - 1);
    // Create a TE calculator and run it:
    TransferEntropyCalculatorDiscrete teCalc = new TransferEntropyCalculatorDiscrete
          (2, 1);
    teCalc.initialise():
10
11
    teCalc.addObservations(sourceArray, destArray);
12
    double result = teCalc.computeAverageLocalOfObservations();
```

- Supply the data to the calculator to construct PDFs:
 - addObservations() may be called multiple times;
 - Onvert arrays into Java format:
 - From Matlab/Octave using our octaveToJavaIntArray(array), etc., scripts.
 - From Python using JArray(JInt, numDims)(array), etc.

```
int arrayLengths = 100;
    RandomGenerator rg = new RandomGenerator();
    // Generate some random binary data:
    int[] sourceArray = rg.generateRandomInts(arrayLengths, 2);
    int[] destArray = new int[arrayLengths];
    destArrav[0] = 0:
    System.arraycopy(sourceArray, 0, destArray, 1, arrayLengths - 1);
    // Create a TE calculator and run it:
    TransferEntropyCalculatorDiscrete teCalc = new TransferEntropyCalculatorDiscrete
          (2.1):
10
    teCalc.initialise():
11
    teCalc.addObservations(sourceArray, destArray);
12
    double result = teCalc.computeAverageLocalOfObservations();
```

- Compute the measure:
 - Value is always returned in bits for discrete calculators.
 - Result here approaches 1 bit since destination copies the (random) source.
 - Other computations include:
 - computeLocalOfPreviousObservations() for local values
 - computeSignificance() to compute p-values of measures of predictability (see Appendix A5 of paper for description).

Discrete Data - Usage Paradigm



Simple Demo 4 – Continuous Data

```
Open:
```

demos/java/infodynamics/demos/Example4TeContinuousDataKraslOR

 ${\tt demos/octave/Example4TeContinuousDataKraskov.m}$

OR

demos/python/Example4TeContinuousDataKraskov.py

Simple Demo 4 – Continuous Data

Open:

demos/java/infodynamics/demos/Example4TeContinuousDataKraslOR
demos/octave/Example4TeContinuousDataKraskov.m

OR

demos/python/Example4TeContinuousDataKraskov.py

1. Run it as you did for example 1.

Simple Java Demo 4 - Continuous Data

3. Examine the code (excerpt from . java file below) – can you notice anything different to the discrete case?

```
double[] sourceArray, destArray;
// Import values into sourceArray and destArray
TransferEntropyCalculatorKraskov teCalc = new
    TransferEntropyCalculatorKraskov();
teCalc.setProperty("k", "4");
teCalc.initialise(1);
teCalc.setObservations(sourceArray, destArray);
double result = teCalc.
    computeAverageLocalOfObservations();
```

Simple Java Demo 4 – Continuous Data

```
double[] sourceArray, destArray;
// ...
// Import values into sourceArray and destArray
// ...
TransferEntropyCalculatorKraskov teCalc = new TransferEntropyCalculatorKraskov()
;
teCalc.setProperty("k", "4");
teCalc.initialise(1);
teCalc.setDbservations(sourceArray, destArray);
double result = teCalc.computeAverageLocalOfObservations();
```

- 4. Note: Continuous data represented as double[] arrays:
 - for time-series measures, the array is indexed by time.
 - ② for multivariate time-series, we use double[][] arrays, indexed first by time then variable number.

```
double[] sourceArray, destArray;
// ...
3  // Import values into sourceArray and destArray
4  // ...
5  TransferEntropyCalculatorKraskov teCalc = new TransferEntropyCalculatorKraskov()
;
teCalc.setProperty("k", "4");
teCalc.initialise(1);
teCalc.setObservations(sourceArray, destArray);
double result = teCalc.computeAverageLocalOfObservations();
```

- Construct the calculator, possibly providing parameters
 - Always check Javadocs for which parameters are required.
 - 2 For continuous calculators, parameters may always be provided later (see next slide) to allow dynamic instantiation.
 - **3** Constructor syntax is different for Matlab/Octave/Python.

```
double[] sourceArray, destArray;
// ...
// Import values into sourceArray and destArray
// ...
TransferEntropyCalculatorKraskov teCalc = new TransferEntropyCalculatorKraskov()
;
teCalc.setProperty("k", "4");
teCalc.initialise(1);
teCalc.setObservations(sourceArray, destArray);
double result = teCalc.computeAverageLocalOfObservations();
```

- Set properties for the calculator (new method for continuous):
 - Check the Javadocs for available properties for each calculator;
 - **Q** E.g. here we set the number k of nearest neighbours for the KSG calculation.
 - Property names and values are always key-value pairs of String objects;
 - Only guaranteed to hold after the next intialise() call.
 - Properties can easily be extracted and set from a file (see Simple Demo 6).

```
double[] sourceArray, destArray;
// ...
// Import values into sourceArray and destArray
// ...
TransferEntropyCalculatorKraskov teCalc = new TransferEntropyCalculatorKraskov();
teCalc.setProperty("k", "4");
teCalc.initialise(1);
teCalc.setObservations(sourceArray, destArray);
double result = teCalc.computeAverageLocalOfObservations();
```

- Initialise the calculator prior to:
 - use or re-use, as for Discrete.
 - This clears PDFs ready for new samples, and finalises any new property settings.
 - There may be several overloaded forms taking different arguments. In the above, teCalc.initialise(1) sets history length k = 1. We could also call teCalc.initialise(k, tau_k, 1, 1_tau, delay) here to specify embedding dimensions and source-target delay. Check Javadocs for options here.

```
double[] sourceArray, destArray;
// ...

// Import values into sourceArray and destArray
// ...

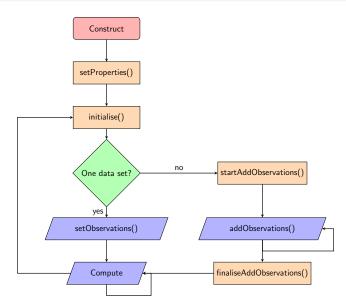
TransferEntropyCalculatorKraskov teCalc = new TransferEntropyCalculatorKraskov()
;
teCalc.setProperty("k", "4");
teCalc.setObservations(sourceArray, destArray);
double result = teCalc.computeAverageLocalOfObservations();
```

- Supply the data to the calculator to construct PDFs:
 - setObservations() may be called once, OR
 - ② call addObservations() multiple times, in between startAddObservations() and finaliseAddObservations() calls.
 - Onvert arrays into Java format:
 - From Matlab/Octave using our octaveToJavaDoubleArray(array), etc., scripts.
 - From Python using JArray(JDouble, numDims)(array),
 etc

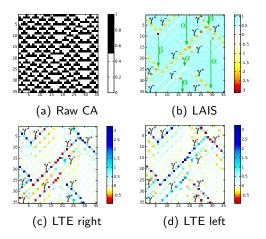
```
double[] sourceArray, destArray;
// ...
// Import values into sourceArray and destArray
// ...
TransferEntropyCalculatorKraskov teCalc = new TransferEntropyCalculatorKraskov()
;
teCalc.setProperty("k", "4");
teCalc.initialise(1);
teCalc.setObservations(sourceArray, destArray);
double result = teCalc.computeAverageLocalOfObservations();
```

- Compute the measure:
 - Value may be in bits (kernel) OR in nats (LSG, Gaussian) calculators.
 - Result here approaches 0.17 nats since destination is correlated with the (random) source.
 - Other computations include:
 - omputeLocalOfPreviousObservations() for local values
 - computeSignificance() to compute p-values of measures of predictability (see Appendix A5 of paper for description).

Continuous Data – Usage Paradigm



Many other demos – e.g. local dynamics in CAs

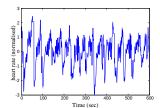


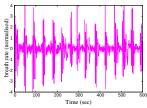
See PDF documentation for demos/octave/CellularAutomata/to recreate, e.g. run GsoChapterDemo2013.m.



Read & understand the calculation of transfer entropy between heart rate & breath rate measurements (data from Rigney et al. (1993) in demos/data/SFI-heartRate_breathVol_bloodOx.txt) in:

- demos/java/infodynamics/java/schreiberTransferEntropyExamples/-HeartBreathRateKraskovRunner.java
- @ demos/octave/SchreiberTransferEntropyExamples/runHeartBreathRateKraskov.m
- demos/python/SchreiberTransferEntropyExamples/runHeartBreathRateKraskov.py (available here in SVN, not in V1.2 distribution)







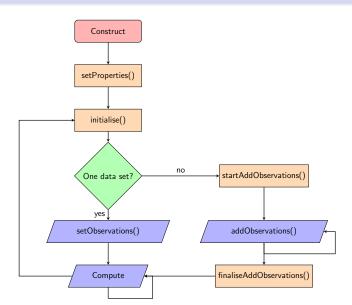
- Task:
 - Compute Mutual Information between the heart and breath rate time-series data in that example (samples 2350 to 3550, inclusive),
 - Using a Kraskov (KSG) estimator, algorithm 2, with 4 nearest neighbours.
 - You can start from the Transfer Entropy demo on this data set, in your preferred environment, and modify it to compute MI..

- Task:
 - Compute Mutual Information between the heart and breath rate time-series data in that example (samples 2350 to 3550, inclusive),
 - Using a Kraskov (KSG) estimator, algorithm 2, with 4 nearest neighbours.
 - You can start from the Transfer Entropy demo on this data set, in your preferred environment, and modify it to compute MI.

Answer: 0.123 nats.

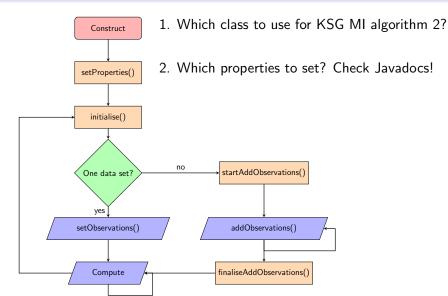
- Task:
 - Compute Mutual Information between the heart and breath rate time-series data in that example (samples 2350 to 3550, inclusive),
 - Using a Kraskov (KSG) estimator, algorithm 2, with 4 nearest neighbours.
 - You can start from the Transfer Entropy demo on this data set, in your preferred environment, and modify it to compute MI..
 - Hint: You can see how a Kraskov MI calculator is used in Simple Demo 6 in the distribution.

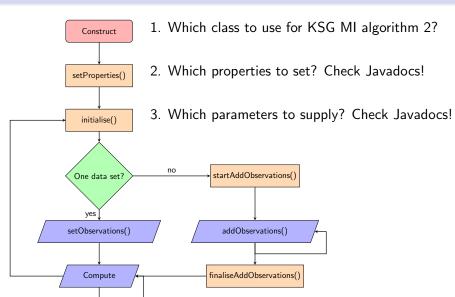
Answer: 0.123 nats.

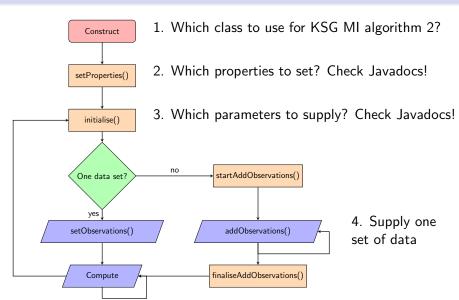


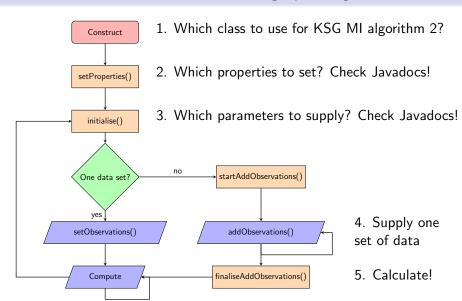
1. Which class to use for KSG MI algorithm 2? Construct setProperties() initialise() no startAddObservations() One data set? yes addObservations() setObservations() Compute finaliseAddObservations()











Exercise – sample answer

```
import infodynamics.measures.continuous.kraskov.
     MutualInfoCalculatorMultiVariateKraskov2;
3 // New KSG MI (algorithm 2) calculator:
  miCalc = new
     MutualInfoCalculatorMultiVariateKraskov2();
  miCalc.initialise(1,1); // univariate
     calculation
  miCalc.setProperty("k", "4"); // 4 nearest
     neighbours
  miCalc.setObservations(heart, chestVol);
  double miHeartToBreath = miCalc.
     computeAverageLocalOfObservations();
```

Debrief

How did you find the exercise?

Was it difficult? Which parts?

Did you know where to find the information you needed?

Any questions arising from the exercise?

Exercise - Challenge task 1

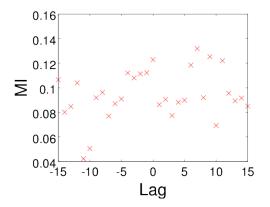
Extend to compute MI(heart;breath), for a variety of **lags** between the two time-series. E.g., investigate lags of [0, 1, ..., 14, 15].

HINT: You could either:

- shift the time-series with respect to eachother to affect the lag, or
- (cleaner) check out the available properties for this MI calculator in the Javadocs. (Challenge: what to do if you want to use negative lags, i.e. a positive lag from breath to heart, with this property?)

Exercise - Challenge task 1

Extend to compute MI(heart;breath), for a variety of **lags** between the two time-series. E.g., investigate lags of [0, 1, ..., 14, 15].



What would you interpret from the results? Can you think of some logical further investigations here?

What I wanted you to take away today:

- Understand measures of information dynamics;
- Be able to obtain and install JIDT distribution;
- Understand and run sample scripts in their chosen environment;
- Be able to modify sample scripts for new analysis;
- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).

What I wanted you to take away today:

- Understand measures of information dynamics;
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- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).

Did we get there?

What I wanted you to take away today:

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- Be able to modify sample scripts for new analysis;
- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).

Did we get there?
Did you get what you came here for?

What I wanted you to take away today:

- Understand measures of information dynamics;
- Be able to obtain and install JIDT distribution;
- Understand and run sample scripts in their chosen environment;
- Be able to modify sample scripts for new analysis;
- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).

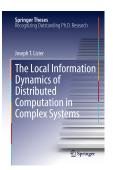
Did we get there? Did you get what you came here for? Any other questions?

Final messages

We're seeking a Postdoc and PhD students for our Complex Systems group at University of Sydney – talk to me if interested

Final messages

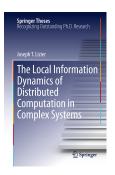
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"The local information dynamics of distributed computation in complex systems", J. T. Lizier, Springer, Berlin (2013).

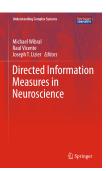
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We're seeking a Postdoc and PhD students for our Complex Systems group at University of Sydney – talk to me if interested



"The local information dynamics of distributed computation in complex systems", J. T. Lizier, Springer, Berlin (2013).

"Directed information measures in neuroscience", edited by M. Wibral, R. Vicente and J. T. Lizier, Springer, Berlin (2014). In Press



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