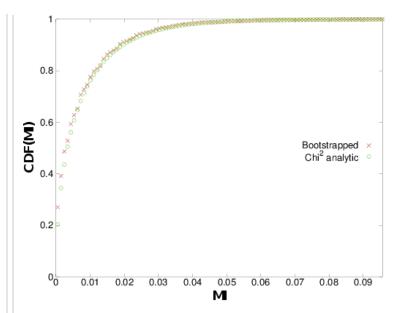
joseph.lizier@gmail.com ▼ | My favorites ▼ | Profile | Sign out

informationdynamics-toolkit JIDT: Java Information Dynamics Toolkit for studying information-theoretic measures of computation in complex Search projects systems **Project Home Downloads** Wiki Issues Source Administer Current pages New page | Search Search for Edit Delete NullDistributions Demonstration of analytic and null distributions of surrogates under null hypothesis for Mutual Information examples, octave, matlab Updated Jan 11, 2015 by joseph.lizier Demos > Null distributions **Null distributions** This demonstration set shows how to generate resampled distributions of MI and TE under null hypotheses of no source-destination relationship, and also investigates the correspondence between analytic and resampled distributions. As detailed in section II.E of the paper describing the toolkit (see InfoDynamicsToolkit.pdf in the distribution), MI, conditional MI and TE will have non-zero bias even for unrelated data when they are estimated from a finite number of samples. Knowing the distribution of this bias is crucial for interpreting whether a sample value of TE, say, indicates a significant directed relationship between the variables, or is just an artifact of random fluctuations. One can compare a sample measurement to the distribution in order to make this judgement. There are some known analytic forms for the distribution of these biases (see refs. 1-4 in the References section below), but otherwise the distribution must be formed by resampling methods, see: Example 3 of the Simple Java Demos, section II.E of the toolkit paper, and refs. 5-10 below. Resampling means creating surrogate source time-series, and taking a population of surrogate measurements from these surrogate source time-series to the destination (in particular we use permutations rather than bootstrapping in JIDT). This demo compares the analytic forms (for the estimators they apply to) to those generated by resampling (which is more computationally intensive, but represents the ground The demo is run under Octave or Matlab. If run in Matlab, it requires the statistics toolbox for access to the chi2cdf function. The demo is available in the distribution at demos/octave/NullDistributions. MI - discrete variables We compare the analytic null distribution for MI for discrete variables against that obtained by resampling in checkMiDiscreteNullDistribution.m. Run this for example as: [mis] = checkMiDiscreteNullDistribution(10000, 100, 0.5, 0.5); to examine the distribution (resampled 10000 times) of MI obtained from sets of 100 samples of unrelated binary variables, each with p=0.5 probability of being a 0 or 1. A sample plot obtained from these parameters is:

28/01/15 16:07 1 of 3

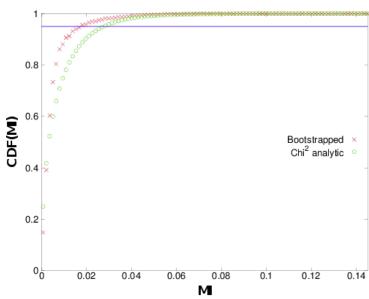


We can see the agreement between the analytic and resampled versions here is very good.

The agreement is not so good for skewed variables however. If we run:

```
[\texttt{mis}] = \mathsf{checkMiDiscreteNullDistribution}(100000,\ 100,\ 0.05,\ 0.05);
```

i.e. with binary variables each with only p=0.05 of being a 1, then we get the following sample plot:



In fact, the analytic distribution does not take the skewing of the variables into account (see the code), only number of samples. We know however that for skewed variables in general the MI will be lower. This is borne out in the plot above where the analytic and resampled distributions do not match as well.

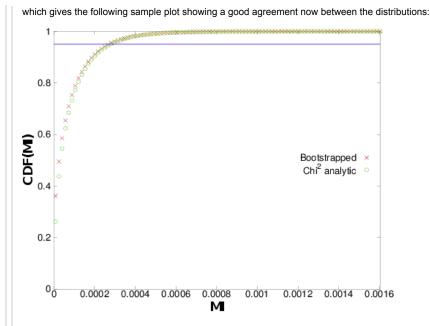
This can be a problem where for example we wish to use the distribution to confirm whether the sample measurement indicates a significant relationship or not. If we use an α =0.05 cutoff (i.e. CDF=0.95), represented by the blue line on the plot, we see that the analytic distribution would result in an MI threshold being around double that determined by the resampling.

>> This would make a big difference to our conclusions, so for a small number of samples (which is usually what we are dealing with) it is more accurate to stick with resampling. <<

The analytic distributions are asymptotically correct though as our number of samples gets larger. We can see this if we run our function again for the same skewed variables but for 100x more samples:

[mis] = checkMiDiscreteNullDistribution(100000, 10000, 0.05, 0.05);

2 of 3 28/01/15 16:07



References

- 1. J. Geweke, Journal of the American Statistical Association 77, 304 (1982).
- 2. D. R. Brillinger, Brazilian Journal of Probability and Statistics 18, 163 (2004).
- 3. P. E. Cheng, J. W. Liou, M. Liou, and J. A. D. Aston, Journal of Data Science 4, 387 (2006).
- 4. L. Barnett and T. Bossomaier, Physical Review Letters 109, 138105+ (2012).
- 5. M. Wibral, R. Vicente, and M. Lindner, in "Directed Information Measures in Neuroscience", Understanding Complex Systems, edited by M. Wibral, R. Vicente, and J. T. Lizier (Springer, Berlin/Heidelberg, 2014) pp. 3-36.
- 6. J. T. Lizier, J. Heinzle, A. Horstmann, J.-D. Haynes, and M. Prokopenko, Journal of Computational Neuroscience 30, 85 (2011).
- 7. R. Vicente, M. Wibral, M. Lindner, and G. Pipa, Journal of Computational Neuroscience 30, 45 (2011).
- 8. M. Lindner, R. Vicente, V. Priesemann, and M. Wibral, BMC Neuroscience 12, 119+ (2011).
- 9. M. Chávez, J. Martinerie, and M. Le Van Quyen, Journal of Neuroscience Methods 124, 113 (2003).
- 10. P. F. Verdes, Physical Review E 72, 026222+ (2005).

Thanks also to Lionel Barnett for discussions on the relationship between resampled and analytic results, and pointing out the asymptotically correct nature of the analytic forms.

Terms - Privacy - Project Hosting Help

Powered by Google Project Hosting

3 of 3 28/01/15 16:07