# The Influence of Metallicity on the Leavitt Law from Geometrical Distances of Milky Way and Magellanic Cloud Cepheids

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#### Abstract

The Cepheid period–luminosity (PL) relation is the key tool for measuring astronomical distances and for establishing the extragalactic distance scale. In particular, the local value of the Hubble constant ( $H_0$ ) strongly depends on Cepheid distance measurements. The recent Gaia Data Releases and other parallax measurements from the Hubble Space Telescope (HST) already enabled us to improve the accuracy of the slope ( $\alpha$ ) and intercept ( $\beta$ ) of the PL relation. However, the dependence of this law on metallicity is still largely debated. In this paper, we combine three samples of Cepheids in the Milky Way (MW), the Large Magellanic Cloud (LMC), and the Small Magellanic Cloud (SMC) in order to derive the metallicity term (hereafter  $\gamma$ ) of the PL relation. The recent publication of extremely precise LMC and SMC distances based on late-type detached eclipsing binary systems provides a solid anchor for the Magellanic Clouds. In the MW, we adopt Cepheid parallaxes from the early third Gaia Data Release. We derive the metallicity effect in V, I, J, H,  $K_S$ ,  $W_{VI}$ , and  $W_{JK}$ . In the  $K_S$  band we report a metallicity effect of  $-0.221 \pm 0.051$  mag dex $^{-1}$ , the negative sign meaning that more metal-rich Cepheids are intrinsically brighter than their more metal-poor counterparts of the same pulsation period.

Unified Astronomy Thesaurus concepts: Cepheid distance (217); Parallax (1197); Metallicity (1031); Magellanic Clouds (990); Milky Way Galaxy (1054)

Supporting material: machine-readable tables

#### 1. Introduction

The Cepheid period–luminosity (PL) relation, discovered by Henrietta Leavitt (Leavitt & Pickering 1912) about a century ago, is an essential tool for measuring astronomical distances since it represents the first rung of the extragalactic distance ladder. This law is used to measure distances to Type Ia supernovae (SNe Ia) host galaxies and thus plays a key role in the determination of the Hubble constant ( $H_0$ ). This parameter currently exhibits a tension of at least  $\sim 4\sigma$  between its measurement in the early universe by Planck Collaboration et al. (2020) assuming a  $\Lambda$ CDM cosmology and the local estimate based on Cepheid distances (Riess et al. 2021). The precise calibration of the PL relation is therefore of paramount importance to reach a 1% determination of the Hubble constant.

While the slope  $(\alpha)$  and intercept  $(\beta)$  of the Leavitt law are generally consistent between various studies, the value and even the sign of the metallicity term  $(\gamma)$ , defined as  $M = \alpha \log P + \beta + \gamma$  [Fe/H]) are still debated and constitute 0.5% of the error budget of  $H_0$  (Riess et al. 2016). Some empirical studies report a metallicity dependence consistent with  $\gamma \sim 0$  mag dex<sup>-1</sup>: Udalski et al. (2001) conclude with a null effect from the study of a metal-poor galaxy in optical bands, Storm et al. (2011b) find a null effect in all bands except in  $W_{VI}$ , and Wielgórski et al. (2017) derive a gamma value consistent with zero in optical and near-IR (NIR) bands. Still, a large majority of the analysis investigating the metallicity effect derived a negative sign, with values ranging between -0.2 and

-0.5 mag dex<sup>-1</sup> (Freedman & Madore 1990; Macri et al. 2006; Saha et al. 2006; Gieren et al. 2018; Groenewegen 2018). This trend would indicate that metal-rich Cepheids are brighter than metal-poor ones. However, the study by Romaniello et al. (2008) yielded a metallicity effect of the opposite sign, confirming the theoretical predictions (Caputo et al. 2000; Bono et al. 2008; Fiorentino et al. 2013).

In this paper, we aim at determining the effect of metallicity on the PL relation by combining samples of Cepheids in the Milky Way (MW) and in the Magellanic Clouds (MCs), taking advantage of the large range of metallicity covered by the Cepheids in these three galaxies (from +0.08 to -0.75 dex). Most of the Cepheids located in distant galaxies hosting SNe Ia have metallicities within this range; therefore, our results are directly applicable to extragalactic studies of the distance scale (e.g., Javanmardi et al. 2021).

Recently, Pietrzyński et al. (2019) and Graczyk et al. (2020) measured the most precise distances to date for the Large Magellanic Cloud (LMC) and Small Magellanic Cloud (SMC), respectively, based on enhanced samples of late-type detached eclipsing binaries (DEBs). These distances allow us to obtain a precise calibration of the PL relation in the LMC and SMC. For MW Cepheids, we use the early third Gaia Data Release (EDR3), which recently provided parallaxes of unprecedented precision for hundreds of galactic Cepheids.

In Section 2 we present our samples of Cepheids in the three galaxies, and in Section 3 we provide the distances we adopted for each sample. Then, in Section 4 we estimate the metallicity effect by fitting the period–luminosity–metallicity (PLZ)

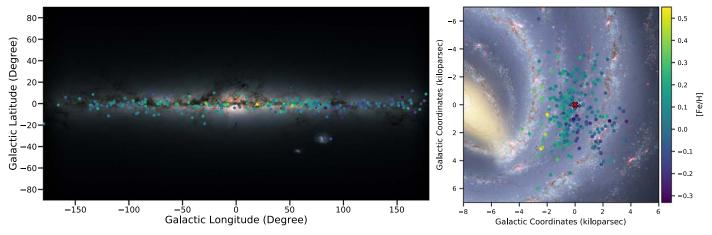


Figure 1. Galactic maps projected on the sky (left) and on the galactic plane (right) showing the distribution of the MW Cepheid sample. The color scale represents the metallicity [Fe/H], and the red cross is the position of the solar system.

relation in the three galaxies. We discuss the results in Section 5.

#### 2. Samples of Cepheids

#### 2.1. MW Cepheids

We gather a sample of MW Cepheids for which wellcovered light curves are available. In the NIR J, H, and K bands, we combine the catalogs by Welch et al. (1984), Laney & Stobie (1992), Barnes et al. (1997), and Monson & Pierce (2011). The data from these four studies are found to be in close agreement, with residuals of 0.013, 0.010, and 0.002 mag in *J*, *H*, and *K*, respectively (Monson & Pierce 2011). We adopt these values as photometric zero-point (ZP) uncertainties for the NIR photometry. Additional NIR data were also found in Feast et al. (2008); we consider that including this source of data does not impact the homogeneity and the dispersion of the data since it only affects four stars of the sample. In the optical V and I bands, we use the catalog from Berdnikov (2008) that provides photometry in the Johnson–Cousins system for a large number of Cepheids. Since it is a compilation of data from various catalogs by the same author, we adopt a photometric ZP uncertainty of 0.010 mag.

For each star and in each filter, we phase the data at the date of maximum luminosity and obtain intensity-averaged mean apparent magnitudes by performing light-curve fitting using Fourier series. Depending on the properties of the different light curves (such as the presence of bumps, steep variations, or to prevent the introduction of unphysical oscillations when the data are too dispersed or not dense enough), we adapt the number of Fourier modes, and thus of free parameters, in order to obtain a satisfactory representation of the light curve. A Fourier decomposition of order 3 is generally sufficient for an usual Cepheid light curve such as  $\delta$  Cep and is up to order 6 for a more complex star such as RS Pup. We derived the statistical uncertainties on the mean magnitudes from the scatter of each light curve. In a few cases, a very large number of data points are available (>300) and result in unrealistic small errors; in these cases we adopt a minimum error of 0.006 mag.

For long-period Cepheids, large phase shifts may degrade the quality of the fit, the photometry being spread over four decades. Therefore, period changes were taken into account for

the phasing of long-period stars such as SV Vul, GY Sge, or RS Pup (Kervella et al. 2017). We adopted a polynomial model of up to degree 5 for the pulsation period.

We carefully analyze the light curves: we exclude Cepheids for which fewer than eight data points are available (MW Cepheids have on average 35 data points in NIR and 160 in optical) and Cepheids that have poor-quality photometry or insufficient phase coverage. Finally, we convert all the NIR data in the Two Micron All Sky Survey (2MASS) system using the transformations from Monson & Pierce (2011). The systematics related to these transformations are negligible. Examples of a well-covered light curve and of a poor-quality light curve are provided in Figures 8 and 9 in Appendix A.

We select Cepheids pulsating in the fundamental mode according to the reclassification by Ripepi et al. (2019). For stars that were not available in this catalog, we adopted by order of priority the pulsation modes from Groenewegen (2018), from the Variable Star indeX (VSX; Watson et al. 2006), and from Luck (2018).

We adopt reddening values from Fernie et al. (1995) with a 0.94 scaling factor as suggested by Groenewegen (2018), and from Acharova et al. (2012) if not available in the latter. We adopt an uncertainty of 0.05 if it is not provided.

For MW Cepheids, we search for individual metallicities in Genovali et al. (2015). This catalog provides mean abundances based on high-resolution spectra for 75 Cepheids. For stars that are not available in this catalog, we adopt the values from Genovali et al. (2014); they provide homogeneous Cepheid metallicities from their group and compiled from the literature, rescaled to their solar abundance. The individual metallicities are represented in Figure 1 by colored points; they range from -0.33 to +0.55 dex. The gradient of metallicity in the MW is particularly visible, with metal-rich Cepheids located closer to the galactic center than metal-poor ones. These individual metallicities have a weighted mean value of  $0.083 \pm 0.019 \, dex$ with a scatter of 0.14 dex. In the following, we adopt this weighted mean value for all MW Cepheids for consistency and homogeneity with the LMC and SMC samples that only have a mean metallicity, but also because the current precision of the individual metallicities is not sufficient for a thorough calibration of the metallicity effect.

The Cepheids of our MW sample are represented in Figure 1, and their main parameters are listed in Tables 3 and 4 in Appendix B.

#### 2.2. LMC Cepheids

We build a sample of LMC Cepheids by combining the OGLE-IV photometry in V and I bands (Soszyński et al. 2015) with the multiepoch observations from the LMC Near-Infrared Synoptic Survey by Macri et al. (2015) taken with the CPAPIR camera on the 1.5 m CTIO telescope. We update their NIR mean magnitudes to bring them into better agreement with the 2MASS system using the following relations (L. Macri 2021, private communication). These were derived by matching  $\sim$ 34,000 stars in common between their Table 1 and the 2MASS Point Source Catalog (Cutri et al. 2003), with 12 mag < H <13.5 mag, K >11.5 mag, and -0.5 mag < J - K <1.4 mag:

$$\begin{split} J_{\text{2MASS}} &= J_{\text{M15}} - 0.0167 + 0.0205 \, (J_{\text{M15}} - K_{\text{M15}} - 0.4) \\ &+ 0.0101 \, (J_{\text{M15}} - K_{\text{M15}} - 0.4)^2 \\ H_{\text{2MASS}} &= H_{\text{M15}} + 0.0116 - 0.0054 \, (J_{\text{M15}} - K_{\text{M15}} - 0.4) \\ &- 0.0189 \, (J_{\text{M15}} - K_{\text{M15}} - 0.4)^2 \\ K_{\text{2MASS}} &= K_{\text{M15}} + 0.0162 + 0.0227 \, (J_{\text{M15}} - K_{\text{M15}} - 0.4) \\ &- 0.0595 \, (J_{\text{M15}} - K_{\text{M15}} - 0.4)^2. \end{split}$$

We adopt a photometric ZP uncertainty of 0.02 mag in all bands. Since some Cepheids exhibit large brightness variations during a pulsation cycle, we consider that single-epoch photometry is not precise enough to derive reliable mean magnitudes; therefore, we discarded the mean magnitudes derived by Inno et al. (2016) from template fitting on 2MASS single-point data and IRSF measurements.

We perform a quality check on this initial sample: we reject stars with magnitude uncertainties larger than 1% and with fewer than five data points (LMC Cepheids have on average 43 data points in NIR and 147 in optical), and we only consider fundamental mode Cepheids. We reject Cepheids located outside a radius of 3° around the LMC center in order to avoid outliers such as stars that do not belong to the LMC or that are strongly affected by its geometrical effects (see Section 3.2). We adopt reddening values from the Górski et al. (2020) reddening map. The final sample of LMC Cepheids contains 1446 stars in the V band and 807 stars in  $K_S$ ; it is listed in Table 5 in Appendix C and provided as supplementary material online. A map of the final sample of LMC Cepheids is represented in Figure 2. For LMC Cepheids, we adopt the mean metallicity used by Gieren et al. (2018), which compiles several estimates from various studies:  $[Fe/H]_{LMC} = -0.34 \pm$ 0.06 dex. The uncertainties take into account the homogenization of the different measurements.

#### 2.3. SMC Cepheids

We assemble a sample of SMC Cepheids by taking the mean magnitudes from the VISTA survey of the Magellanic Clouds (VMC; Ripepi et al. 2016) cross-matched with OGLE-IV photometry by Soszyński et al. (2015). Unfortunately, we do not have H-band photometry for SMC Cepheids because we rejected data from single-epoch photometry and template fitting. Results in the H band are therefore derived from the

combination of MW and LMC Cepheids only. Magnitudes in the VISTA system were converted into the 2MASS system using the equations from Ripepi et al. (2016):

$$J' = J_{VMC} + 0.070 (J_{VMC} - K_{VMC})$$
  
 $K' = K_{VMC} - 0.011 (J_{VMC} - K_{VMC}).$ 

We perform an additional correction (L. Macri 2021, private communication) derived by matching  $\sim$ 7000 stars in common between the VMC DR4 and the 2MASS Point Source Catalog, with J>12.25 mag, K>11.5 mag, and -0.5 mag < J-K < 1.4 mag:

$$J_{2\text{MASS}} = J' - 0.0087 - 0.0010 (J' - K' - 0.4)$$
  
 $K_{2\text{MASS}} = K' + 0.0011 - 0.0087 (J' - K' - 0.4).$ 

We adopt a photometric ZP uncertainty of 0.02 mag for all bands. As we did for the LMC sample, we also reject SMC Cepheids with magnitude uncertainties larger than 1%, with fewer than five data points (SMC Cepheids have on average 17 data points in NIR and 46 in optical), and we only keep Cepheids pulsating in the fundamental mode. As for the LMC sample, we adopt reddening values from the Górski et al. (2020) reddening map.

While the LMC has a rather simple geometry, the SMC is very elongated along the line of sight: we select Cepheids located in a region of  $0.6^{\circ}$  around the SMC center, which covers an area of 1.3 kpc width. Since the SMC distance is derived from DEBs, this selection ensures that the Cepheids are located in the same region as these DEBs. The final SMC sample has 284 stars in the V band and 295 stars in  $K_S$ ; it is listed in Table 6 in Appendix D and provided as supplementary material. A map of our final sample of SMC Cepheids is presented in Figure 3.

For SMC Cepheids, we adopt the mean metallicity used by Gieren et al. (2018), which compiles several estimates from various studies:  $[Fe/H]_{SMC} = -0.75 \pm 0.05$  dex. Similar to the LMC value, the uncertainty takes into account the homogenization of the different measurements.

#### 3. Distances

In order to calibrate the Leavitt law, one needs to derive the absolute magnitude of each Cepheid from its apparent luminosity and from its distance.

#### 3.1. Distances to Milky Way Cepheids

Recently, the early third Gaia Data Release provided new parallaxes for MW Cepheids (Gaia Collaboration 2020). We perform a first quality check of Gaia EDR3 parallaxes based on the renormalized unit weight error (RUWE) provided in the catalog. This parameter reflects the quality of the parallax of a star compared to other stars of the same color and brightness. Its value is expected to be close to 1 for well-behaved sources (Lindegren et al. 2021b). In particular, the RUWE is sensitive to the photocentric motion of unresolved objects; therefore, it can be used to detect possible astrometric binaries. We discard the Cepheids of our sample that have an RUWE > 1.4; this selection corresponds to approximately 13% of our MW sample and removes the stars that are possibly affected by saturation or contamination by a bright neighbor companion. In particular, all the outliers noticed by eye on the PL relation are

affected by a large RUWE; therefore, the quality check based on this parameter appears to be relevant for our purposes.

Riess et al. (2021) use a different indicator: they identify stars with a goodness of fit (GOF) larger than 12.5 as having a compromised parallax. We find the GOF and the RUWE selections to have a very similar effect on our sample: adopting this GOF criterion for the quality check instead of the RUWE leads to rejecting exactly the same stars, except T Mon, V0496 Aql, and VW Pup, which have an RUWE of 1.72, 1.56, and 1.41 and a GOF of 12.11, 10.90, and 11.36, respectively. The RUWE criterion seems slightly more selective than the GOF limit adopted by Riess et al. (2021). Adopting a threshold of RUWE < 1.4 corresponds to a limit GOF of 10.

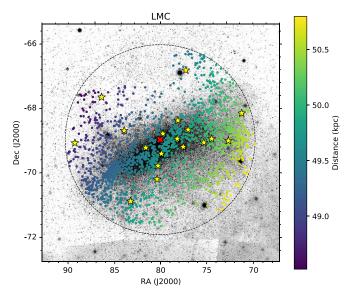
One method to check whether a Cepheid is an astrometric binary is to look for proper-motion anomalies between the observations by Hipparcos and Gaia. Using the approach described in Kervella et al. (2019), we find 20 Cepheids with a high-proper-motion anomaly signal. However, none of them were identified by their high RUWE or GOF, and they do not appear as outliers; therefore, we do not exclude them.

Cepheids are variable stars, and therefore their brightness and color can change significantly during a pulsation cycle. This effect was not taken into account in the processing of Gaia DR2 astrometry and resulted in additional systematics, noise, and dispersion for variable star parallaxes (Breuval et al. 2020). The correction for this chromatic effect on Cepheid parallaxes is still absent from Gaia EDR3 (Lindegren et al. 2021b). However, the number of observations obtained for each star increased consequently between Gaia DR2 (~22 months) and Gaia EDR3 (~34 months). We assume in this paper that the noise induced by this effect is negligible for Gaia EDR3 parallaxes.

For each Cepheid we correct for the parallax ZP by using the Python tool<sup>6</sup> described in Lindegren et al. (2021b). This ZP correction takes into account the ecliptic latitude, magnitude, and color of each star. Our MW Cepheids cover a range of magnitudes from G = 3 to 12 mag. For our sample of MW Cepheids, we find the ZP to vary between -4 and  $-54 \mu as$ with a median value of  $-27 \mu as$  ( $\sigma = 10 \mu as$ ), which is very similar to the median parallax offset derived by Riess et al. (2021). Following Lindegren et al. (2021b), who recommend to include an uncertainty of a few microarcseconds in the ZP, we adopt a systematic error of 5  $\mu$ as on this quantity. Considering our sample of Cepheids, this error is equivalent to an average systematic uncertainty of 0.020 mag in distance modulus. In Section 5.1, we discuss the influence of adopting this individual ZP correction compared with the uniform ZP of  $-17 \mu as$ derived from quasars.

We find 13 Cepheids to fall in the range between G = 10.8 and 11.2 mag, where a transition of window classes occurs (Figure 1 in Lindegren et al. 2021a). In this particular range, the value of the parallax ZP can possibly be affected, so we quadratically add 10  $\mu$ as to the parallax uncertainty.

Finally, we increase all Gaia EDR3 parallax uncertainties by 10%, following Riess et al. (2021) to account for potential excess uncertainty. This correction has significantly reduced since Gaia DR2, where it was recommended to increase parallax uncertainties by 30%.



**Figure 2.** Map of the LMC Cepheids considered in our study. Yellow stars are the eclipsing binaries from Pietrzyński et al. (2019), and the red cross is the center of the LMC. The dashed circle represents a radius of 3° around the LMC center.

#### 3.2. Distances to LMC Cepheids

Recently, Pietrzyński et al. (2019) estimated the distance to the LMC with a 1% precision based on DEBs:  $d_{\rm LMC} = 49.59 \pm 0.09$  (stat.)  $\pm 0.54$  (syst.) kpc. This method for measuring distances is independent from Cepheids and relies on surface brightness relations, established by precise interferometric measurements. We use this value as the initial distance to our Cepheids, and we add a corrective term depending on the position of each Cepheid in the LMC, assuming the disk geometry derived by OGLE from Cepheids by Jacyszyn-Dobrzeniecka et al. (2016). First, we compute the Cartesian coordinates ( $x_i$ ,  $y_i$ ,  $z_i$ ) of each Cepheid from their equatorial coordinates ( $\alpha_i$ ,  $\delta_i$ ) using the transformations

$$\begin{cases} x_i = -d_{\text{LMC}}\cos\delta_i\sin(\alpha_i - \alpha_{\text{LMC}}) \\ y_i = d_{\text{LMC}}\left[\sin\delta_i\cos\delta_{\text{LMC}} \\ -\cos\delta_i\sin\delta_{\text{LMC}}\cos(\alpha_i - \alpha_{\text{LMC}})\right]' \\ z_i = c_1x_i + c_2y_i + d_{\text{LMC}} \end{cases}$$

where  $(\alpha_{\rm LMC}, \delta_{\rm LMC}) = (80.05^{\circ}, -69.30^{\circ})$  are the coordinates of the LMC center and the coefficients  $(c_1, c_2) = (0.395 \pm 0.014, -0.215 \pm 0.013)$  are from Jacyszyn-Dobrzeniecka et al. (2016). The corrected distance of each LMC Cepheid is

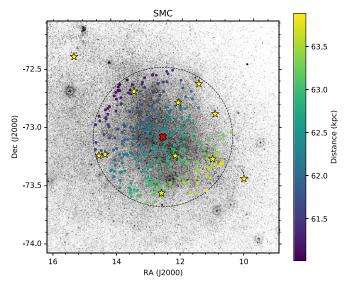
$$d_i = \sqrt{x_i^2 + y_i^2 + z_i^2}.$$

The distances of each LMC Cepheid derived with this correction are located in a range of  $\pm$  1.5 kpc around the mean LMC distance from Pietrzyński et al. (2019). They are represented by the colors in Figure 2.

#### 3.3. Distances to SMC Cepheids

The distance to the SMC was recently measured by Graczyk et al. (2020) with a precision of 1.5% using the same method as used in Pietrzyński et al. (2019) for the LMC: from a sample of 15 DEBs, a distance of  $d_{\rm SMC}=62.44\pm0.47$  (stat.)  $\pm$  0.81 (syst.) kpc is derived. However, the SMC has a large

<sup>6</sup> https://www.cosmos.esa.int/web/gaia/edr3-code



**Figure 3.** Map of the SMC Cepheids considered in our study. Yellow stars are the eclipsing binaries from Graczyk et al. (2020), and the red cross is the center of the SMC. The dashed circle represents a radius of  $0.6^{\circ}$  around the SMC center.

extension along the line of sight (Subramanian & Subramaniam 2012; Jacyszyn-Dobrzeniecka et al. 2016; Ripepi et al. 2017), which makes the distance to its core region particularly difficult to measure, contrary to the LMC, which has a rather simple geometry. In this section, we take into account the SMC elongated shape in order to derive corrected distances to each of its Cepheids. For each SMC Cepheid of coordinates ( $\alpha_i$ ,  $\delta_i$ ), we compute the Cartesian coordinates ( $x_i$ ,  $y_i$ ) such that

$$\begin{cases} x_i = -d_{\rm SMC}\cos\delta_i\sin(\alpha_i - \alpha_{\rm SMC}) \\ y_i = d_{\rm SMC}\left[\sin\delta_i\cos\delta_{\rm SMC} \\ -\cos\delta_i\sin\delta_{\rm SMC}\cos(\alpha_i - \alpha_{\rm SMC})\right] \end{cases},$$

where  $(\alpha_{\rm SMC}, \delta_{\rm SMC}) = (12^{\circ}54, -73^{\circ}.11)$  (Ripepi et al. 2017). Then, we used the equations corresponding to the blue lines in Figure 4 of Graczyk et al. (2020):

$$\begin{cases} d_i(x) = (3.086 \pm 0.066) x_i + d_{SMC} \\ d_i(y) = (-3.248 \pm 0.118) y_i + d_{SMC}. \end{cases}$$

We adopt the mean value of  $d_i(x)$  and  $d_i(y)$  as the final distance of each Cepheid. The elongated shape of the SMC is highlighted by the dispersion of the derived distances between +5 and -6 kpc around the mean value  $d_{\rm SMC}$ , which represents almost 10% of the mean value. The distances of our sample of SMC Cepheids are represented on the map in Figure 3. A discussion about the elongated shape of the SMC and its impact on our results is provided in Section 5.2.

## 4. The Metallicity Effect from Milky Way and Magellanic Cloud Cepheids

In this section, we aim at estimating the metallicity term  $\gamma$  of the Leavitt law. In Section 4.1, we start by fitting the  $\alpha$  and  $\beta$  coefficients of the PL relation in each of the three galaxies, without considering the metallicity term. In Section 4.2, we include the metallicity for each galaxy and derive the third term of the PLZ relation by combining the three galaxies.

#### 4.1. The Period-Luminosity Relation

We adopt the Cepheid samples described in Section 2. In the first place, we correct apparent magnitudes for the extinction by adopting the reddening law from Cardelli et al. (1989) and O'Donnell (1994) assuming  $R_V = 3.135$ , which yields  $A_{\lambda} = R_{\lambda} E(B-V)$  with  $R_I = 1.894$ ,  $R_J = 0.892$ ,  $R_H = 0.553$ , and  $R_{K_S} = 0.363$ . We also derive optical and NIR Wesenheit indices (Madore 1982) as defined by  $W_{VI} = I - 1.526 (V - I)$  and  $W_{JK} = K_S - 0.686 (J - K_S)$ . Wesenheit magnitudes are particularly convenient for calibrating the PL relation since they are independent of reddening.

We account for the width of the instability strip by adding quadratically to the photometry uncertainties the intrinsic scatter in each band: this quantity is obtained by subtracting quadratically the measurement errors (photometric inhomogeneities, differential extinction, geometrical effects, phase corrections, etc.) from the scatter of the PL relation: we adopt a width of the instability strip of 0.07 mag in NIR bands (J, H,  $K_S$ , and  $W_{JK}$ ) from Persson et al. (2004), 0.15 mag in V and 0.09 mag in I from Macri et al. (2006), and finally 0.08 mag in  $W_{VI}$  from Madore et al. (2017). We derive the absolute magnitude  $M_{\lambda}$  of each Cepheid from their distance d (in kpc) and dereddened apparent magnitude  $m_{\lambda}$ :

$$M_{\lambda} = m_{\lambda} - 5\log d - 10. \tag{1}$$

In the MW, the distance is obtained at the first order by taking the inverse of the parallax. In order to avoid biases due to this inversion, we adopt the approach introduced by Feast & Catchpole (1997) and Arenou & Luri (1999), consisting in fitting the astrometric-based luminosity (ABL) function instead of absolute magnitudes:

ABL = 
$$\pi_{\text{(mas)}} 10^{0.2m_{\lambda}-2} = 10^{M_{\lambda}/5}$$
 (2)

where:

$$M_{\lambda} = \alpha_{\lambda} (\log P - \log P_0) + \beta_{\lambda}. \tag{3}$$

We adopt a pivot period of  $\log P_0 = 0.7$ , which represents the median period of our Cepheid sample. This approach ensures minimum correlations between the fitted coefficients. We perform a  $3\sigma$  clipping procedure on the PL relation to remove possible outliers.

A nonlinearity in the SMC PL relation was highlighted at the short-period end ( $\log P < 0.4$ ; EROS Collaboration et al. 1999). For LMC and SMC Cepheids, Chown et al. (2021) detect a break in the PL relation at log P = 0.29 and also at very long periods ( $\log P = 1.72$ ). Cepheids beyond these limits are found to deviate from the global PL fit and can affect both the slope and the ZP. Additionally, the short-period edge of the PL relation is potentially affected by first-overtone contamination. In the following, we exclude all Cepheids with periods shorter than 2.5 days ( $\log P = 0.4$ ) and longer than 52 days  $(\log P = 1.72)$ . Finally, we include the systematics on the LMC and SMC distance moduli (0.026 and 0.032 mag, respectively) and the photometric ZPs provided in Section 2 on the intercept error. We use the curve\_fit function from the scipy Python library in a Monte Carlo algorithm to derive the PL coefficients and the 16th and 84th percentiles of the distribution to derive the uncertainties. The PL relations derived for each galaxy are provided in Table 1, where both the slope and intercept are fitted.

In each band, the intercept increases with decreasing metallicity, i.e., it becomes less negative from the MW to the

Band	$\alpha$	β	σ	Nª
		$MW^b$		
$\overline{V}$	$-2.443 \pm 0.031$	$-3.296 \pm 0.024$	0.25	178
I	$-2.780 \pm 0.028$	$-3.981 \pm 0.024$	0.23	150
$W_{VI}$	$-3.289 \pm 0.026$	$-5.030 \pm 0.025$	0.21	149
J	$-3.050 \pm 0.029$	$-4.498 \pm 0.026$	0.18	97
H	$-3.160 \pm 0.028$	$-4.762 \pm 0.024$	0.17	97
$K_S$	$-3.207 \pm 0.028$	$-4.848 \pm 0.022$	0.17	97
$W_{JK}$	$-3.317 \pm 0.028$	$-5.086 \pm 0.026$	0.17	97
		LMC <sup>c</sup>		
$\overline{V}$	$-2.704 \pm 0.007$	$-3.284 \pm 0.033$	0.23	1446
I	$-2.916 \pm 0.005$	$-3.910 \pm 0.033$	0.15	1460
$W_{VI}$	$-3.281 \pm 0.008$	$-4.877 \pm 0.038$	0.08	1432
J	$-3.127 \pm 0.005$	$-4.385 \pm 0.033$	0.12	805
H	$-3.160 \pm 0.005$	$-4.696 \pm 0.033$	0.11	808
$K_S$	$-3.217 \pm 0.005$	$-4.737 \pm 0.033$	0.10	807
$W_{JK}$	$-3.272 \pm 0.008$	$-4.974 \pm 0.039$	0.10	806
		SMC <sup>d</sup>		
$\overline{V}$	$-2.594 \pm 0.012$	$-3.196 \pm 0.038$	0.28	284
I	$-2.871 \pm 0.008$	$-3.841 \pm 0.038$	0.22	297
$W_{VI}$	$-3.334 \pm 0.014$	$-4.834 \pm 0.043$	0.12	283
J	$-2.956 \pm 0.004$	$-4.317 \pm 0.038$	0.17	294
H			•••	
$K_S$	$-3.163 \pm 0.002$	$-4.670 \pm 0.038$	0.15	295
$W_{JK}$	$-3.326 \pm 0.002$	$-4.916 \pm 0.043$	0.14	295

#### Notes.

LMC and in turn to the SMC. In the NIR, the intercept changes by  $\sim 0.18$  mag between the MW and the SMC, possibly indicating a strong dependence with metallicity. We note that our  $K_S$ -band calibration in the MW is in good agreement with the result by Breuval et al. (2020) based on Gaia DR2 parallaxes. The fit of the PL relation in the  $K_S$  band performed in each of the three galaxies is represented in Figure 4.

#### 4.2. The Period-Luminosity-Metallicity Relation

In this section, we now calibrate the dependence of the PL intercept  $\beta$  with metallicity. First, we fit the PL relation of the form  $M=\alpha(\log P-0.7)+\beta$  in each of the three galaxies separately with a common slope fixed to the LMC value. As in the previous section, the systematics due to the LMC and SMC distance and to the photometric ZP are included in quadrature to the intercept random error. The intercept  $\beta$  contains the metallicity term such that

$$\beta = \gamma [\text{Fe/H}] + \delta. \tag{4}$$

In Figure 5 are represented the intercepts of the PL relations in the MW, LMC, and SMC as a function of metallicity. We fit Equation (4) with a Monte Carlo algorithm to derive the  $\gamma$  and  $\delta$  coefficients, and we adopt the 16th and 84th percentiles of the distribution to derive the random errors. A histogram

representing the distribution of the  $\gamma$  values obtained with the Monte Carlo algorithm is represented in Figure 6.

The results of the fit are listed in Table 2. In the NIR, we report a strong metallicity effect of  $-0.208 \pm 0.051$  mag dex<sup>-1</sup> in J,  $-0.152 \pm 0.092$  mag dex<sup>-1</sup> in H, and  $-0.221 \pm 0.050$ mag dex<sup>-1</sup> in  $K_S$ . The NIR Wesenheit index  $W_{JK}$  shows a similar dependence with  $-0.214 \pm 0.057$  mag dex<sup>-1</sup>. These results agree by  $1\sigma$  with Gieren et al. (2018), who used the Infrared Surface Brightness Technique (Fouqué & Gieren 1997; Storm et al. 2011a) to derive the distances to the Cepheids in their MW, LMC, and SMC samples, an approach different and independent from the one used in the present study. In the NIR Wesenheit index  $W_H$ , Riess et al. (2019) find an effect of  $-0.170 \pm 0.060$  mag dex<sup>-1</sup>, which is also close to our results in the NIR. In optical bands, we derive a weaker effect than in the NIR with  $-0.048 \pm 0.051$  mag dex<sup>-1</sup> in V and  $-0.138 \pm$  $0.051~{\rm mag~dex^{-1}}$  in I. These values also agree at  $1\sigma$  with Gieren et al. (2018), and the value in V is also consistent at  $1\sigma$ with the differential study of LMC and SMC PL relations by Wielgórski et al. (2017). On average, our results are located between the values by Wielgórski et al. (2017), consistent with a null metallicity effect, and the work by Gieren et al. (2018), who derive a strong negative effect. In the H band, we derive a metallicity effect weaker than in other NIR bands, likely because it is derived from the MW and LMC samples only (due to the lack of H-band photometry for SMC Cepheids). We conclude with the general trend being that the sensitivity to metallicity increases in the absolute sense and becomes more negative from optical to NIR wavelengths. This trend is particularly visible in Figure 7.

We note that the PL slope was fixed to the LMC value because this sample contains significantly more stars than the two other ones. However, if the slope is fixed to the value found in the MW or in the SMC, the intercepts agree by 0.2% in NIR and by 1.4% in optical. Similarly, the  $\gamma$  values agree at  $0.2\sigma$  and  $0.8\sigma$  in NIR and optical, respectively.

#### 5. Discussion

The metallicity term of the PL relation can be sensitive to many different effects. In this section we study the stability  $\gamma$  after varying some parameters.

#### 5.1. Influence of Gaia EDR3 Parallax ZP

In Section 3.1, we corrected each Gaia EDR3 parallax for their individual ZP by using the Python tool described in Lindegren et al. (2021b). However, in Lindegren et al. (2021a), a uniform parallax ZP of  $-17~\mu$ as is derived from quasars. The results of the PLZ fit obtained after adopting this uniform ZP are provided in the second part of Table 7 in Appendix E. They are consistent at the  $1\sigma$  level with the values derived using the individual ZP, although it gives a slightly more negative metallicity effect in each band. For example, in  $K_S$  we obtain  $\gamma = -0.271 \pm 0.051$  mag dex $^{-1}$ , compared with  $\gamma = -0.221 \pm 0.050$  mag dex $^{-1}$  with individual ZPs. This effect can be explained by the individual ZPs being on average more negative than  $-17~\mu$ as for our sample of MW Cepheids.

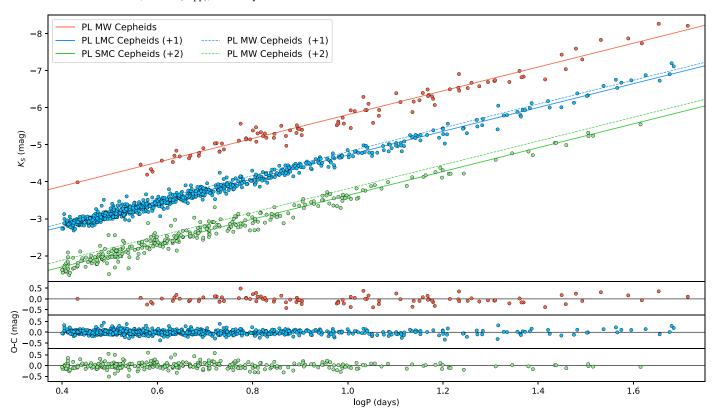
We also investigate whether the individual ZP correction by Lindegren et al. (2021b) is adapted to the most distant Cepheids: we remove from our sample the Cepheids with a parallax smaller than 0.3 mas and derive the PL relation in  $K_S$  without these stars. Using this PL relation, we compute

<sup>&</sup>lt;sup>a</sup> The number of stars is given after the sigma clipping procedure and the period cuts.

<sup>&</sup>lt;sup>b</sup> Mean [Fe/H] =  $+0.083 \pm 0.019$  dex.

<sup>&</sup>lt;sup>c</sup> Mean  $[Fe/H] = -0.34 \pm 0.06$  dex.

<sup>&</sup>lt;sup>d</sup> Mean  $[Fe/H] = -0.75 \pm 0.05 \text{ dex.}$ 



**Figure 4.** Fit of the PL relation in  $K_S$  for MW, LMC, and SMC Cepheids. The bottom panel shows the residual between the Cepheid absolute magnitudes and the corresponding PL fit for each of the three galaxies. The LMC and SMC relations were offset by +1 and +2 mag, respectively, for visualization purposes.

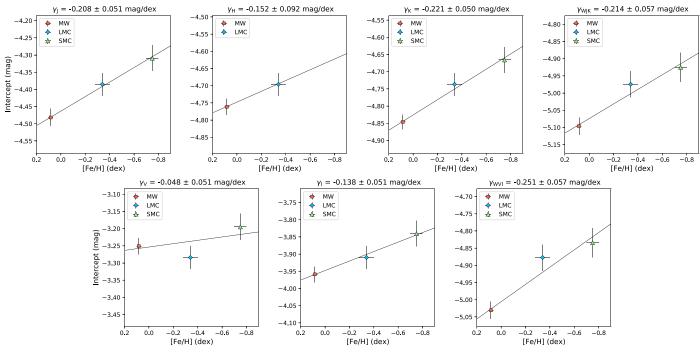


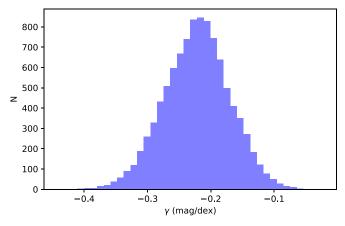
Figure 5. Intercept of the PL relation represented as a function of metallicity in J, H, K, V, I, and Wesenheit bands.

the expected parallax of the most distant Cepheids and compare it with the Gaia EDR3 parallax corrected by the individual ZP. We find a good agreement between the predicted parallaxes and the values from Gaia EDR3 with the Lindegren et al. (2021b) individual correction. From this study, we confirm that the individual ZP correction from

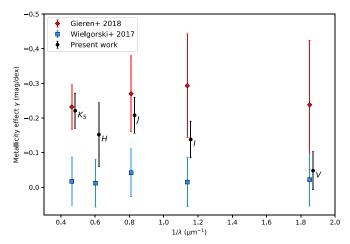
Lindegren et al. (2021b) is adapted to the most distant MW Cepheids of our sample.

#### 5.2. Influence of the SMC Sample

As mentioned in Sections 2.3 and 3.3, the distance to the core region of the SMC is particularly difficult to measure.



**Figure 6.** Histogram of the  $\gamma$  values obtained in the  $K_S$  band by the Monte Carlo algorithm iterated 10,000 times.



**Figure 7.** Metallicity effect as a function of wavelength, compared with values from the literature. The error bars include the systematics discussed in Section 5.2. For visualization purposes, the *X*-axis was slightly shifted for our values so that the error bars do not overlap, but they correspond to the same wavelength as the literature values.

Table 2 Final Results of the PLZ Fit of the Form  $M = \alpha(\log P - 0.7) + \delta + \gamma \text{ [Fe/H] and Associated Uncertainties}$ 

Band	$\alpha$	$\sigma$	$\delta$	$\sigma$	$\gamma$	$\sigma$
$\overline{V}$	-2.704	0.007	-3.252	0.020	-0.048	0.055
I	-2.916	0.005	-3.948	0.020	-0.138	0.053
$W_{VI}$	-3.281	0.008	-5.005	0.022	-0.251	0.057
J	-3.127	0.005	-4.463	0.022	-0.208	0.052
H	-3.160	0.005	-4.748	0.020	-0.152	0.092
$K_S$	-3.217	0.004	-4.826	0.019	-0.221	0.051
$W_{JK}$	-3.273	0.008	-5.075	0.022	-0.214	0.057

Note. The uncertainties include the systematics discussed in Section 5.2.

From their sample of DEBs, Graczyk et al. (2020) derive an uncertainty of about 2% for the distance to the SMC core region. These DEB systems are unevenly distributed in the central region of the galaxy, and their individual distances show a large dispersion around the mean value, ranging from 57 to 67 kpc (see their Figure 3), which corresponds to  $\sim 16\%$  of the SMC distance. In order to avoid including Cepheids

located too far away from the SMC center, we restricted our sample to a region of radius  $0.6^{\circ}$  around the SMC center. With a smaller radius, the contribution of the SMC sample in the PLZ fit becomes smaller than the MW contribution; therefore, we consider that the number of retained SMC Cepheids is insufficient. On the other hand, if we assume a radius larger than  $0.6^{\circ}$  around the SMC center, the number of outlier stars increases and the distance of some Cepheids may not correspond to the distance of the SMC core region. In order to test the validity of our hypothesis, we perform the same PLZ fit with a radius of  $0.5^{\circ}$  and  $0.7^{\circ}$  around the SMC center and report the coefficients in Table 7 in Appendix E.

After extending the SMC sample to a radius of  $0.7^{\circ}$  around the galaxy center, we find  $\gamma$  values in very good agreement (better than  $1\sigma$ ) with the values derived in the initial conditions. When the radius is reduced to  $0.5^{\circ}$ , the metallicity effect still agrees at  $1\sigma$  with the initial conditions in all bands. Considering a smaller region around the SMC center results in a slightly stronger (i.e., more negative) metallicity effect. These results highlight the sensitivity of the metallicity effect with respect to the adopted SMC sample, and in particular to the spatial distribution of the Cepheids considered. Moreover, it emphasizes the necessity to correct each Cepheid distance according to their position in the SMC plane, as we did in Section 3.3.

We consider the variation of  $\gamma$  within a region of  $0.5^{\circ} < R < 0.7^{\circ}$  around the SMC center as an additional source of systematic uncertainties: this source of error is at the level of  $0.02~{\rm mag~dex^{-1}}$  in optical bands and of  $0.01~{\rm mag~dex^{-1}}$  in NIR (see Table 7 in Appendix E). We adopt the same additional source of uncertainty for the intercept  $\delta$ , although the latter coefficient is particularly stable when the radius around the SMC center is changed. These systematics are included in the results presented in Table 2.

#### 6. Conclusions

We build large samples of Cepheids in the MW and in the MCs and make use of the most recent and precise distances available to estimate the metallicity effect on the Cepheid PL relation. In the  $K_S$  band we derive an effect of  $\gamma = -0.221 \pm 0.051$  mag dex $^{-1}$ , in agreement with the value found by Gieren et al. (2018) but more precise. In the V band we derive a weaker effect of  $\gamma = -0.048 \pm 0.055$  mag dex $^{-1}$ , which is consistent with both Wielgórski et al. (2017) and Gieren et al. (2018) within the error bars. We conclude with a nonzero dependence of Cepheid magnitude with metallicity, and we confirm its negative sign: metal-rich Cepheids are brighter than metalpoor ones.

The improved precision reached in this work was made possible thanks to the high quality of Gaia EDR3 parallaxes and the new distances of the two MCs obtained by the Araucaria Project. Combining MW and MC Cepheids also allows us to reach a better precision than previous studies based on MCs only, by the larger range of metallicities they cover. A refined analysis of each light curve ensures the use of accurate mean magnitudes. However, the elongated shape of the SMC in the line of sight remains a source of systematic uncertainty in our study, despite continuous efforts to improve our knowledge of its structure. In this study, we assumed a linear dependence of the PL relation with metallicity, but it might as well be nonlinear (Gieren et al. 2018). Additional high-resolution spectroscopic metallicity measurements of both MW and MC

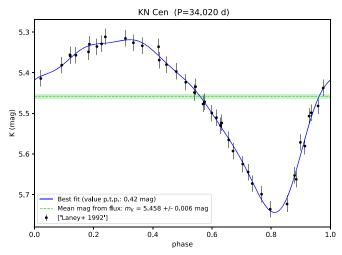
Cepheids should be carried out in the future to even better constrain the metallicity effect, particularly in the NIR, in our effort to further reduce the systematic uncertainty on the determination of the Hubble constant from the Cepheid-SN Ia method.

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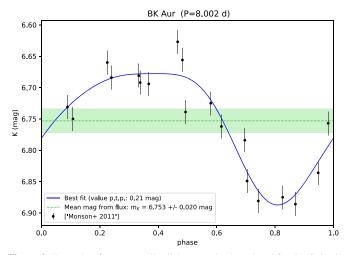
#### Appendix A

Examples of Light Curves of Milky Way Cepheids

Here we present examples of a well-covered light curve (Figure 8) and of a poor-quality light curve (Figure 9). The solid blue line represents the best fit of the light curve, the dashed green line is the mean magnitude derived from the best fit, and the green region is the uncertainty on the intensity-averaged mean magnitude. The method used to fit the light curves is described in Section 2.1.



**Figure 8.** Example of a well-covered light curve in the K band for the Galactic Cepheid KN Cen. The solid blue line represents the best fit of the light curve, the dashed green line is the mean magnitude derived from the best fit, and the green region is the uncertainty on the intensity-averaged mean magnitude.



**Figure 9.** Example of a poor-quality light curve in the K band for the Galactic Cepheid BK Aur. The solid blue line represents the best fit of the light curve, the dashed green line is the mean magnitude derived from the best fit, and the green region is the uncertainty on the intensity-averaged mean magnitude.

#### Appendix B

Data for the Sample of Milky Way Cepheids

Here we detail the sample of Milky Way Cepheids. In Table 3, we provide the period, parallax, and RUWE from Gaia EDR3, reddening, and metallicity for each Cepheid. In Table 4 are listed the apparent magnitudes in *V*, *I*, *J*, *H*, and *K* for each Milky Way Cepheid, along with the references.

 Table 3

 Sample of Milky Way Cepheids and Main Parameters

Star	Period (days)	$\pi_{\mathrm{EDR3}}$ (mas)	RUWE	E(B-V) (mag)	Reference	[Fe/H] (dex)	Reference
AA Gem	11.302	$0.311 \pm 0.018$	1.25	$0.345 \pm 0.036$	F95	$-0.08 \pm 0.05$	G15
AC Mon	8.014	$0.383 \pm 0.019$	1.38	$0.507 \pm 0.033$	F95	$-0.03\pm0.06$	G14b
AD Gem	3.788	$0.370 \pm 0.020$	0.97	$0.206 \pm 0.048$	F95	$-0.14 \pm 0.06$	G15
AD Pup	13.596	$0.254 \pm 0.017$	1.36	$0.363 \pm 0.020$	F95	$-0.20 \pm 0.15$	G14b
AE Vel	7.134	$0.369 \pm 0.012$	0.97	$0.691 \pm 0.055$	F95	$0.14 \pm 0.06$	G14b
AG Cru	3.837	$0.758 \pm 0.020$	1.02	$0.242 \pm 0.020$	F95	$0.08 \pm 0.06$	G14b
AP Pup AP Sgr	5.084	$0.924 \pm 0.020$	1.05	$0.250 \pm 0.034$	F95 F95	$-0.16 \pm 0.15$	G14b
AP Sgr AQ Car	5.058 9.769	$\begin{array}{c} 1.217 \pm 0.024 \\ 0.361 \pm 0.016 \end{array}$	0.88 1.07	$0.184 \pm 0.015$ $0.168 \pm 0.013$	F95 F95	$0.10 \pm 0.08$ $-0.30 \pm 0.15$	G14b G14b
AQ Car AQ Pup	30.149	$0.361 \pm 0.016$ $0.294 \pm 0.023$	1.18	$0.108 \pm 0.013$ $0.531 \pm 0.017$	F95	$-0.30 \pm 0.13$ $0.06 \pm 0.05$	G146 G15
AS Per	4.973	$0.650 \pm 0.016$	1.08	$0.684 \pm 0.041$	F95	$0.00 \pm 0.05$ $0.14 \pm 0.06$	G14b
AT Pup	6.665	$0.604 \pm 0.016$	1.04	$0.166 \pm 0.011$	F95	$-0.22 \pm 0.15$	G14b
AV Sgr	15.415	$0.404 \pm 0.025$	0.84	$1.238 \pm 0.027$	F95	$0.22 \pm 0.13$ $0.35 \pm 0.17$	G15
AW Per	6.464	$1.093 \pm 0.029$	1.16	$0.479 \pm 0.016$	F95	$0.04 \pm 0.06$	G14b
AY Cas	2.872	$0.414 \pm 0.019$	1.07	$0.760 \pm 0.049$	F95	$0.02 \pm 0.06$	G14b
AY Cen	5.310	$0.574 \pm 0.014$	0.95	$0.357 \pm 0.066$	F95	$0.08 \pm 0.06$	G14b
AY Sgr	6.570	$0.546 \pm 0.019$	0.85	$0.840 \pm 0.009$	F95	$0.11 \pm 0.06$	G15
BB Her	7.508	$0.280 \pm 0.015$	1.06	$0.392 \pm 0.039$	A12	$0.26\pm0.06$	G14b
BB Sgr	6.637	$1.188 \pm 0.024$	0.82	$0.285 \pm 0.011$	F95	$0.08 \pm 0.08$	G14b
BE Mon	2.706	$0.504 \pm 0.017$	1.17	$0.549 \pm 0.036$	F95	$0.05 \pm 0.09$	G15
BF Oph	4.068	$1.189 \pm 0.024$	0.84	$0.261 \pm 0.016$	F95	$0.14 \pm 0.06$	G14b
BG Vel	6.924	$1.045 \pm 0.017$	0.99	$0.434 \pm 0.011$	F95	$-0.10 \pm 0.15$	G14b
BK Aur	8.002	$0.426 \pm 0.015$	1.01	$0.393 \pm 0.026$	F95	$-0.07 \pm 0.15$	G14b
BM Per	22.952	$0.334 \pm 0.022$	0.99	$0.919 \pm 0.059$	F95	$0.23 \pm 0.06$	G14b
BM Pup	7.199	$0.302 \pm 0.013$	1.18	$0.575 \pm 0.058$	F95	$-0.07 \pm 0.08$	G15
BN Pup BP Cas	13.673 6.273	$0.301 \pm 0.015$	1.25 1.02	$0.422 \pm 0.017$ $0.864 \pm 0.014$	F95 F95	$0.03 \pm 0.05$ $0.09 \pm 0.06$	G15 G14b
BZ Cyg	10.142	$0.442 \pm 0.013$ $0.500 \pm 0.014$	1.02	$0.832 \pm 0.014$	F95	$0.09 \pm 0.06$ $0.19 \pm 0.08$	G14b
CD Cas	7.801	$0.412 \pm 0.014$	1.06	$0.745 \pm 0.012$	F95	$0.13 \pm 0.06$ $0.13 \pm 0.06$	G14b
CD Cyg	17.074	$0.394 \pm 0.016$	1.01	$0.512 \pm 0.021$	F95	$0.15 \pm 0.06$ $0.15 \pm 0.06$	G14b
CE Pup	49.326	$0.114 \pm 0.014$	0.82	$0.740 \pm 0.074$	A12	$-0.04 \pm 0.09$	G14
CF Cas	4.875	$0.316 \pm 0.012$	1.04	$0.556 \pm 0.021$	F95	$0.02 \pm 0.06$	G14b
CG Cas	4.366	$0.296 \pm 0.017$	1.03	$0.667 \pm 0.009$	F95	$0.09 \pm 0.06$	G14b
CK Sct	7.415	$0.490 \pm 0.020$	0.97	$0.816 \pm 0.024$	F95	$0.21 \pm 0.06$	G14b
CN Car	4.933	$0.342 \pm 0.014$	0.96	$0.438 \pm 0.049$	F95	$0.21\pm0.06$	G14b
CP Cep	17.859	$0.279 \pm 0.021$	1.01	$0.681 \pm 0.045$	F95	$-0.01 \pm 0.08$	G14b
CR Cep	6.233	$0.699 \pm 0.013$	1.06	$0.704 \pm 0.009$	F95	$-0.06 \pm 0.08$	G14b
CR Ser	5.301	$0.578 \pm 0.020$	1.19	$0.974 \pm 0.017$	F95	$0.12 \pm 0.08$	G15
CS Mon	6.732	$0.324 \pm 0.014$	1.04	$0.528 \pm 0.032$	F95	$-0.08 \pm 0.06$	G14b
CS Ori	3.889	$0.257 \pm 0.022$	1.33	$0.373 \pm 0.030$	F95	$-0.25 \pm 0.06$	G15
CS Vel	5.905	$0.272 \pm 0.016$	0.91	$0.716 \pm 0.027$	F95	$0.12 \pm 0.06$	G14b
CV Mon	5.379	$0.601 \pm 0.015$	1.10	$0.705 \pm 0.018$ $0.409 \pm 0.043$	F95	$0.09 \pm 0.09$	G15
CY Car CY Cas	4.266 14.377	$0.427 \pm 0.011$ $0.255 \pm 0.019$	0.93 1.07	$0.409 \pm 0.043$ $0.952 \pm 0.008$	F95 F95	$0.11 \pm 0.06$ $0.06 \pm 0.08$	G14b G14b
CZ Cas	5.664	$0.292 \pm 0.019$	0.96	$0.761 \pm 0.030$	F95	$0.00 \pm 0.08$ $0.07 \pm 0.06$	G14b
DD Cas	9.812	$0.346 \pm 0.013$	1.05	$0.486 \pm 0.016$	F95	$0.07 \pm 0.08$ $0.10 \pm 0.08$	G14b
DF Cas	3.832	$0.374 \pm 0.014$	1.05	$0.564 \pm 0.049$	F95	$0.13 \pm 0.08$	G14b
DW Per	3.650	$0.296 \pm 0.019$	1.31	$0.620 \pm 0.033$	F95	$-0.05 \pm 0.06$	G14b
EK Mon	3.958	$0.376 \pm 0.021$	1.16	$0.547 \pm 0.003$	F95	$-0.05 \pm 0.15$	G14b
ER Car	7.719	$0.869 \pm 0.015$	0.82	$0.111 \pm 0.016$	F95	$0.15 \pm 0.06$	G14b
EX Vel	13.234	$0.204 \pm 0.015$	0.94	$0.728 \pm 0.052$	F95	$0.07 \pm 0.06$	G14b
FI Car	13.458	$0.242 \pm 0.019$	0.99	$0.694 \pm 0.007$	F95	$0.31\pm0.06$	G14b
FM Aql	6.114	$1.014 \pm 0.026$	1.26	$0.635 \pm 0.019$	F95	$0.24 \pm 0.06$	G14b
FN Aql	9.482	$0.736 \pm 0.025$	1.12	$0.486 \pm 0.008$	F95	$-0.06 \pm 0.06$	G14b
GH Cyg	7.818	$0.417 \pm 0.014$	1.07	$0.608 \pm 0.023$	F95	$0.21 \pm 0.06$	G14b
GI Cyg	5.783	$0.273 \pm 0.017$	1.01	$0.734 \pm 0.073$	F95	$0.27 \pm 0.06$	G14b
GQ Ori	8.616	$0.408 \pm 0.021$	0.87	$0.224 \pm 0.013$	F95	$0.20 \pm 0.08$	G15
GU Nor	3.453	$0.565 \pm 0.015$	0.87	$0.683 \pm 0.029$	F95	$0.08 \pm 0.06$	G15
GX Car	7.197	$0.459 \pm 0.013$	1.02	$0.380 \pm 0.008$	F95	$0.14 \pm 0.06$	G14b
GY Sge	51.790	$0.342 \pm 0.023$	0.95	$1.183 \pm 0.111$	F95	$0.29 \pm 0.06$	G14b
HW Car	9.199	$0.397 \pm 0.012$	0.94	$0.181 \pm 0.018$	F95	$0.09 \pm 0.06$	G14b
IQ Nor	8.220	$0.535 \pm 0.018$	0.97	$0.676 \pm 0.044$	F95	$0.22 \pm 0.07$	G15

Table 3 (Continued)

			((	Continued)			
Star	Period (days)	$\pi_{\text{EDR3}}$ (mas)	RUWE	E(B-V) (mag)	Reference	[Fe/H] (dex)	Reference
IT Car	7.533	$0.702 \pm 0.020$	1.08	$0.212 \pm 0.016$	F95	$0.14 \pm 0.06$	G14b
KK Cen	12.180	$0.152 \pm 0.018$	1.03	$0.555 \pm 0.033$	F95	$0.24 \pm 0.06$	G14b
KN Cen	34.020	$0.251 \pm 0.018$	1.03	$0.728 \pm 0.040$	F95	$0.55\pm0.12$	G15
KQ Sco	28.705	$0.472 \pm 0.021$	0.91	$0.852 \pm 0.041$	F95	$0.52 \pm 0.08$	G15
LS Pup	14.147	$0.214 \pm 0.016$	1.25	$0.452 \pm 0.009$	F95	$-0.12 \pm 0.11$	G15
MW Cyg	5.955	$0.542 \pm 0.019$	1.21	$0.651 \pm 0.039$	F95	$0.09 \pm 0.08$	G14b
MZ Cen	10.354	$0.221 \pm 0.017$	0.84	$0.782 \pm 0.077$	F95	$0.27 \pm 0.10$	G15
QY Cen	17.752	$0.293 \pm 0.021$	1.02	$1.213 \pm 0.216$	F95	$0.24 \pm 0.06$	G14b
R Cru	5.826	$1.078 \pm 0.028$	1.16	$0.156 \pm 0.012$	F95	$0.13 \pm 0.06$	G14b
R Mus	7.510	$1.076 \pm 0.018$	1.07	$0.149 \pm 0.030$	F95	$-0.08 \pm 0.06$	G14b
R TrA RR Lac	3.389 6.416	$1.560 \pm 0.016$	0.89 1.10	$0.167 \pm 0.025$ $0.267 \pm 0.023$	F95 F95	$0.19 \pm 0.06$ $0.04 \pm 0.06$	G14b G14b
RS Nor	6.198	$0.424 \pm 0.015 \\ 0.472 \pm 0.017$	0.94	$0.267 \pm 0.023$ $0.577 \pm 0.036$	F95 F95	$0.04 \pm 0.06$ $0.18 \pm 0.08$	G146 G15
RS Ori	7.567	$0.472 \pm 0.017$ $0.589 \pm 0.030$	1.12	$0.377 \pm 0.030$ $0.332 \pm 0.010$	F95	$0.18 \pm 0.08$ $0.11 \pm 0.09$	G15
RS Pup	41.480	$0.589 \pm 0.030$ $0.581 \pm 0.017$	1.12	$0.352 \pm 0.010$ $0.451 \pm 0.010$	F95	$0.07 \pm 0.09$ $0.07 \pm 0.15$	G14b
RU Sct	19.704	$0.526 \pm 0.024$	0.87	$0.914 \pm 0.017$	F95	$0.07 \pm 0.13$ $0.14 \pm 0.04$	G146
RV Sco	6.061	$1.257 \pm 0.021$	0.81	$0.343 \pm 0.007$	F95	$0.14 \pm 0.04$ $0.11 \pm 0.06$	G14b
RW Cas	14.795	$0.335 \pm 0.019$	1.26	$0.440 \pm 0.032$	F95	$0.22 \pm 0.08$	G14b
RX Aur	11.624	$0.654 \pm 0.021$	0.98	$0.254 \pm 0.020$	F95	$0.10 \pm 0.06$	G14b
RY CMa	4.678	$0.825 \pm 0.029$	1.29	$0.238 \pm 0.016$	F95	$0.00 \pm 0.15$	G14b
RY Sco	20.323	$0.764 \pm 0.032$	0.73	$0.654 \pm 0.044$	F95	$0.01 \pm 0.06$	G15
RY Vel	28.136	$0.376 \pm 0.021$	1.07	$0.539 \pm 0.012$	F95	$-0.05 \pm 0.15$	G14b
RZ Vel	20.398	$0.661 \pm 0.017$	1.24	$0.301 \pm 0.011$	F95	$0.05 \pm 0.15$	G14b
S Cru	4.690	$1.342 \pm 0.024$	0.94	$0.172 \pm 0.014$	F95	$0.11 \pm 0.06$	G14b
S Nor	9.754	$1.099 \pm 0.022$	0.88	$0.182 \pm 0.008$	F95	$0.02 \pm 0.09$	G14b
S TrA	6.324	$1.120 \pm 0.022$	1.04	$0.086 \pm 0.010$	F95	$0.21 \pm 0.06$	G14b
SS CMa	12.361	$0.307 \pm 0.013$	1.11	$0.551 \pm 0.012$	F95	$0.06 \pm 0.04$	G15
SS Sct	3.671	$0.934 \pm 0.023$	0.84	$0.340 \pm 0.022$	F95	$0.14 \pm 0.06$	G14b
ST Tau	4.034	$0.916 \pm 0.034$	1.35	$0.328 \pm 0.006$	F95	$-0.14 \pm 0.15$	G14b
ST Vel	5.858	$0.384 \pm 0.015$	1.19	$0.530 \pm 0.024$	F95	$-0.14 \pm 0.15$	G14b
SV Mon	15.233	$0.464 \pm 0.032$	1.01	$0.264 \pm 0.021$	F95	$0.12 \pm 0.08$	G15
SV Vel	14.097	$0.434 \pm 0.018$	1.02	$0.376 \pm 0.024$	F95	$0.12 \pm 0.06$	G14b
SV Vul	44.993	$0.402 \pm 0.021$	1.20	$0.474 \pm 0.024$	F95	$0.05 \pm 0.08$	G14b
SW Cas SW Vel	5.441 23.407	$0.461 \pm 0.012$	1.12 1.05	$0.475 \pm 0.027$	F95 F95	$-0.03 \pm 0.08$	G14b G14b
SW Vei	4.860	$0.413 \pm 0.018$ $0.515 \pm 0.022$	1.05	$0.338 \pm 0.009$ $0.323 \pm 0.026$	F95	$-0.15 \pm 0.15$ $0.05 \pm 0.06$	G14b
SX Cai	4.290	$0.313 \pm 0.022$ $0.313 \pm 0.019$	1.19	$0.523 \pm 0.020$ $0.537 \pm 0.046$	F95	$-0.03 \pm 0.06$ $-0.03 \pm 0.06$	G14b
SX Vel	9.550	$0.513 \pm 0.019$ $0.501 \pm 0.019$	1.02	$0.237 \pm 0.040$ $0.237 \pm 0.014$	F95	$-0.03 \pm 0.00$ $-0.18 \pm 0.15$	G14b
SY Aur	10.145	$0.462 \pm 0.020$	1.08	$0.386 \pm 0.040$	F95	$-0.07 \pm 0.15$	G14b
SZ Aql	17.141	$0.525 \pm 0.020$	0.94	$0.553 \pm 0.022$	F95	$0.07 \pm 0.13$ $0.18 \pm 0.08$	G14b
SZ Cas	13.639	$0.407 \pm 0.017$	1.01	$0.713 \pm 0.060$	F95	$0.07 \pm 0.06$	G14b
SZ Cyg	15.110	$0.445 \pm 0.012$	0.96	$0.594 \pm 0.004$	F95	$0.09 \pm 0.08$	G14b
T Ant	5.898	$0.312 \pm 0.014$	1.18	$0.300 \pm 0.030$	A12	$-0.20 \pm 0.06$	G14b
T Cru	6.733	$1.222 \pm 0.014$	0.82	$0.191 \pm 0.022$	F95	$0.14 \pm 0.06$	G14b
T Vel	4.640	$0.940 \pm 0.016$	0.93	$0.282 \pm 0.018$	F95	$-0.02 \pm 0.15$	G14b
T Vul	4.435	$1.719 \pm 0.058$	1.20	$0.092 \pm 0.017$	F95	$0.01 \pm 0.08$	G14b
TT Aql	13.755	$0.997 \pm 0.023$	1.08	$0.487 \pm 0.024$	F95	$0.22\pm0.06$	G14b
TV CMa	4.670	$0.420 \pm 0.015$	1.20	$0.574 \pm 0.029$	F95	$0.01 \pm 0.07$	G15
TV Cam	5.295	$0.237 \pm 0.018$	1.11	$0.560 \pm 0.023$	F95	$0.04 \pm 0.06$	G14b
TW CMa	6.995	$0.384 \pm 0.019$	1.15	$0.374 \pm 0.033$	F95	$0.04 \pm 0.09$	G15
TW Nor	10.786	$0.360 \pm 0.020$	0.89	$1.190 \pm 0.023$	F95	$0.27 \pm 0.10$	G15
TX Cen	17.098	$0.332 \pm 0.018$	0.94	$0.941 \pm 0.038$	F95	$0.44 \pm 0.12$	G15
TX Cyg	14.710	$0.829 \pm 0.019$	0.95	$1.123 \pm 0.005$	F95	$0.20 \pm 0.08$	G14b
TY Sct	11.053	$0.371 \pm 0.016$	0.91	$0.930 \pm 0.017$	F95	$0.37 \pm 0.06$	G14b
TZ Mon	7.428	$0.298 \pm 0.015$	1.24	$0.434 \pm 0.023$	F95	$-0.02 \pm 0.07$	G15
TZ Mus	4.945	$0.266 \pm 0.020$	1.00	$0.676 \pm 0.020$	F95	$0.10 \pm 0.06$	G14b
U Car	38.829	$0.561 \pm 0.023$	1.23	$0.276 \pm 0.013$	F95	$0.17 \pm 0.09$	G14b
U Nor	12.644	$0.625 \pm 0.019$	0.98	$0.868 \pm 0.038$	F95	$0.07 \pm 0.09$	G14b
U Sgr	6.745	$1.605 \pm 0.023$	0.85	$0.408 \pm 0.007$	F95	$0.08 \pm 0.08$	G14b
UU Mus	11.636	$0.306 \pm 0.012$	1.01	$0.431 \pm 0.041$	F95	$0.11 \pm 0.09$	G14b
UX Car	3.682	$0.653 \pm 0.019$	1.02	$0.102 \pm 0.023$	F95	$-0.10 \pm 0.15$	G14b
UX Per	4.566	$0.162 \pm 0.020$	1.17	$0.462 \pm 0.024$	F95	$-0.05 \pm 0.06$	G14b

Table 3 (Continued)

			((	Continued)			
Star	Period (days)	$\pi_{\text{EDR3}}$ (mas)	RUWE	E(B-V) (mag)	Reference	[Fe/H] (dex)	Reference
UY Car	5.544	$0.455 \pm 0.014$	0.94	$0.188 \pm 0.017$	F95	$0.13 \pm 0.06$	G14b
UY Per	5.365	$0.415 \pm 0.015$	1.17	$0.888\pm0.013$	F95	$0.18\pm0.06$	G14b
UZ Car	5.205	$0.401 \pm 0.013$	0.95	$0.213 \pm 0.034$	F95	$0.13 \pm 0.06$	G14b
UZ Cas	4.259	$0.251 \pm 0.020$	1.23	$0.469 \pm 0.034$	F95	$-0.05 \pm 0.06$	G14b
UZ Sct	14.744	$0.324 \pm 0.025$	0.91	$0.959 \pm 0.023$	F95	$0.33 \pm 0.08$	G15
V Car	6.697	$0.797 \pm 0.014$	1.04	$0.164 \pm 0.013$	F95	$-0.06 \pm 0.15$	G14b
V Cen	5.494	$1.409 \pm 0.022$	1.06	$0.265 \pm 0.016$	F95	$0.04 \pm 0.09$	G14b
V Lac	4.983	$0.496 \pm 0.016$	1.09	$0.293 \pm 0.034$	F95	$0.06 \pm 0.06$	G14b
V Vel V0339 Cen	4.371	$0.953 \pm 0.017$	1.03	$0.225 \pm 0.021$	F95	$-0.30 \pm 0.15$	G14b
V0339 Cen V0340 Ara	9.466 20.814	$\begin{array}{c} 0.568 \pm 0.021 \\ 0.239 \pm 0.020 \end{array}$	0.89 0.93	$0.426 \pm 0.016$ $0.548 \pm 0.008$	F95 F95	$0.06 \pm 0.03$ $0.33 \pm 0.09$	G15 G15
V0340 Ara V0340 Nor	11.289	$0.239 \pm 0.020$ $0.491 \pm 0.025$	0.93	$0.348 \pm 0.008$ $0.312 \pm 0.050$	F95	$0.07 \pm 0.07$	G15
V0340 Nor V0378 Cen	6.460	$0.491 \pm 0.023$ $0.524 \pm 0.019$	0.92	$0.372 \pm 0.030$ $0.374 \pm 0.049$	F95	$0.07 \pm 0.07$ $0.08 \pm 0.06$	G14b
V0370 Cen V0381 Cen	5.079	$0.818 \pm 0.020$	1.06	$0.206 \pm 0.013$	F95	$0.00 \pm 0.00$ $0.02 \pm 0.06$	G14b
V0386 Cyg	5.258	$0.894 \pm 0.013$	0.95	$0.907 \pm 0.033$	F95	$0.02 \pm 0.00$ $0.11 \pm 0.08$	G14b
V0402 Cyg	4.365	$0.410 \pm 0.011$	0.92	$0.455 \pm 0.062$	F95	$0.02 \pm 0.08$	G14b
V0459 Cyg	7.251	$0.382 \pm 0.014$	1.09	$0.775 \pm 0.024$	F95	$0.09 \pm 0.06$	G14b
V0470 Sco	16.261	$0.534 \pm 0.029$	0.97	$1.550 \pm 0.124$	F95	$0.16 \pm 0.06$	G15
V0493 Aql	2.988	$0.472 \pm 0.017$	1.12	$0.730 \pm 0.087$	F95	$0.03 \pm 0.06$	G14b
V0496 Cen	4.424	$0.563 \pm 0.013$	0.94	$0.579 \pm 0.031$	F95	$0.09 \pm 0.06$	G14b
V0520 Cyg	4.049	$0.437 \pm 0.012$	1.03	$0.754 \pm 0.075$	F95	$0.08 \pm 0.06$	G14b
V0538 Cyg	6.119	$0.394 \pm 0.017$	0.99	$0.656 \pm 0.021$	F95	$0.05 \pm 0.06$	G14b
V0600 Aql	7.239	$0.523 \pm 0.019$	1.13	$0.812 \pm 0.007$	F95	$0.03 \pm 0.08$	G14b
V0609 Cyg	31.088	$0.295 \pm 0.017$	1.12	$1.243 \pm 0.124$	F95	$0.22\pm0.06$	G14b
V0636 Cas	8.377	$1.372 \pm 0.018$	1.02	$0.593 \pm 0.065$	F95	$0.07 \pm 0.08$	G14b
V0636 Sco	6.797	$1.180 \pm 0.034$	1.15	$0.227 \pm 0.017$	F95	$0.10 \pm 0.06$	G14b
V0733 Aql	6.179	$0.244 \pm 0.015$	0.98	$0.106 \pm 0.011$	A12	$0.08 \pm 0.08$	G14b
V0737 Cen	7.066	$1.213 \pm 0.019$	0.92	$0.227 \pm 0.022$	F95	$0.14 \pm 0.06$	G14b
V1154 Cyg	4.925	$0.442 \pm 0.012$	1.04	$0.315 \pm 0.031$	F95	$-0.10 \pm 0.08$	G14b
V1162 Aql	5.376	$0.823 \pm 0.023$	0.95	$0.184 \pm 0.011$	F95	$0.01 \pm 0.08$	G14b
VW Cen	15.036	$0.260 \pm 0.016$	1.06	$0.424 \pm 0.022$	F95	$0.41 \pm 0.08$	G15
VW Cru	5.265	$0.738 \pm 0.016$	0.85	$0.640 \pm 0.046$	F95	$0.19 \pm 0.06$	G14b
VY Car	18.890 7.857	$0.565 \pm 0.017$ $0.485 \pm 0.012$	0.92 1.07	$0.270 \pm 0.019$ $0.596 \pm 0.021$	F95 F95	$-0.06 \pm 0.15$ $0.00 \pm 0.08$	G14b G14b
VY Cyg VY Per	5.532	$0.485 \pm 0.012$ $0.485 \pm 0.017$	1.15	$0.948 \pm 0.021$ $0.948 \pm 0.018$	F95	$0.00 \pm 0.08$ $0.04 \pm 0.06$	G14b
VY Sgr	13.557	$0.483 \pm 0.017$ $0.412 \pm 0.025$	0.81	$0.948 \pm 0.018$ $0.903 \pm 0.243$	F95	$0.34 \pm 0.00$ $0.33 \pm 0.12$	G140
VZ Cyg	4.864	$0.545 \pm 0.016$	1.31	$0.291 \pm 0.015$	F95	$0.05 \pm 0.12$ $0.05 \pm 0.08$	G14b
VZ Pup	23.175	$0.220 \pm 0.015$	1.24	$0.433 \pm 0.018$	F95	$-0.01 \pm 0.04$	G146
W Gem	7.914	$1.006 \pm 0.028$	1.23	$0.264 \pm 0.011$	F95	$0.01 \pm 0.01$ $0.02 \pm 0.06$	G14b
WW Pup	5.517	$0.212 \pm 0.016$	1.14	$0.334 \pm 0.017$	F95	$0.13 \pm 0.16$	G15
WX Pup	8.937	$0.387 \pm 0.015$	1.06	$0.306 \pm 0.018$	F95	$-0.15 \pm 0.15$	G14b
WY Pup	5.251	$0.258 \pm 0.013$	1.02	$0.259 \pm 0.031$	F95	$-0.10 \pm 0.08$	G15
WZ Pup	5.027	$0.281 \pm 0.017$	1.35	$0.196 \pm 0.022$	F95	$-0.07 \pm 0.06$	G15
WZ Sgr	21.851	$0.612 \pm 0.028$	0.94	$0.457 \pm 0.025$	F95	$0.28 \pm 0.08$	G15
X Cru	6.220	$0.654 \pm 0.019$	0.95	$0.294 \pm 0.019$	F95	$0.15 \pm 0.06$	G14b
X Cyg	16.386	$0.910 \pm 0.020$	1.28	$0.251 \pm 0.010$	F95	$0.10 \pm 0.08$	G14b
X Pup	25.973	$0.397 \pm 0.020$	1.04	$0.396 \pm 0.015$	F95	$0.02 \pm 0.08$	G15
X Sct	4.198	$0.634 \pm 0.019$	0.80	$0.581 \pm 0.030$	F95	$0.12\pm0.09$	G15
X Sgr	7.013	$2.843 \pm 0.141$	1.22	$0.189 \pm 0.020$	F95	$-0.21 \pm 0.30$	G14b
X Vul	6.320	$0.864 \pm 0.022$	1.06	$0.775 \pm 0.021$	F95	$0.07 \pm 0.08$	G14b
XX Cen	10.953	$0.570 \pm 0.026$	1.24	$0.245 \pm 0.012$	F95	$0.04 \pm 0.09$	G14b
XX Mon	5.456	$0.242 \pm 0.013$	0.86	$0.586 \pm 0.014$	F95	$0.01 \pm 0.08$	G15
XX Sgr	6.424	$0.724 \pm 0.027$	1.10	$0.493 \pm 0.016$	F95	$-0.01 \pm 0.06$	G15
XX Vel	6.985	$0.308 \pm 0.013$	0.88	$0.530 \pm 0.007$	F95	$0.11 \pm 0.06$	G14b
XZ Car	16.651	$0.473 \pm 0.018$	1.05	$0.372 \pm 0.026$	F95	$0.19 \pm 0.06$	G14b
Y Aur	3.859	$0.541 \pm 0.017$	1.12	$0.384 \pm 0.031$	F95	$-0.26 \pm 0.15$	G14b
Y Lac	4.324	$0.431 \pm 0.013$	1.05	$0.212 \pm 0.020$	F95	$0.03 \pm 0.06$	G14b
Y Oph V Sot	17.125	$1.348 \pm 0.036$	1.03	$0.606 \pm 0.030$	F95	$0.06 \pm 0.08$	G14b
Y Sct	10.342	$0.558 \pm 0.020$	0.94 0.99	$0.792 \pm 0.021$	F95 F95	$0.23 \pm 0.06$	G14b
YZ Aur YZ Car	18.193 18.168	$0.233 \pm 0.016$ $0.358 \pm 0.018$	0.99 1.17	$0.548 \pm 0.055$ $0.324 \pm 0.039$	F95 F95	$-0.33 \pm 0.15$ $0.00 \pm 0.06$	G14b G14b
	9.554		0.95	$0.324 \pm 0.039$ $0.289 \pm 0.007$	F95 F95		G14b G14b
YZ Sgr	7.554	$0.860 \pm 0.024$	0.33	0.409 ± 0.007	ГЭЭ	$0.06 \pm 0.08$	G140

Table 3 (Continued)

Star	Period (days)	$\pi_{\mathrm{EDR3}}$ (mas)	RUWE	E(B-V) (mag)	Reference	[Fe/H] (dex)	Reference
Z Lac	10.886	$0.510 \pm 0.021$	1.05	$0.352 \pm 0.015$	F95	$0.10 \pm 0.06$	G14b
Z Sct	12.901	$0.357 \pm 0.018$	0.90	$0.535 \pm 0.039$	F95	$0.12 \pm 0.09$	G15

Note. Parallaxes from Gaia EDR3 include ZP correction. Stars with an RUWE parameter larger than 1.4 were marked with a star and excluded from the sample. References. (F95): reddening from Fernie et al. (1995) multiplied by 0.94; (A12): reddening from Acharova et al. (2012), (G14): metallicity from Genovali et al. (2014); (G14b): metallicity from the literature (Yong et al. 2006; Lemasle et al. 2007; Sziládi et al. 2007; Romaniello et al. 2008; Pedicelli et al. 2010; Luck et al. 2011; Luck & Lambert 2011; Genovali et al. 2013) rescaled to Genovali et al. (2014) solar abundance; (G15): metallicity from Genovali et al. (2015). (This table is available in machine-readable form.)

 Table 4

 Optical and NIR Mean Apparent Magnitudes for the Sample of Milky Way Cepheids

Star	V (mag)	I (mag)	J (mag)	H (mag)	$K_S$ (mag)	Reference NIR
AA Gem	$9.735 \pm 0.008$		$7.647 \pm 0.011$	$7.206 \pm 0.010$	$7.069 \pm 0.020$	M11
AC Mon	$10.100 \pm 0.016$	$8.708 \pm 0.012$	$7.590 \pm 0.013$	$7.072 \pm 0.011$	$6.867 \pm 0.012$	M11
AD Gem	•••		$8.453 \pm 0.006$	$8.154 \pm 0.006$	$8.043 \pm 0.007$	B97, M11
AD Pup	$9.898 \pm 0.006$	$8.716 \pm 0.006$	•••	•••	•••	•••
AE Vel	$10.257 \pm 0.009$	$8.730 \pm 0.007$	•••	•••		•••
AG Cru	$8.228 \pm 0.006$	$7.346 \pm 0.006$		•••	•••	
AP Pup	$7.385 \pm 0.006$	$6.463 \pm 0.006$	•••	•••	•••	
AP Sgr	$6.967 \pm 0.006$	$6.053 \pm 0.006$	•••	•••		•••
AQ Car	$8.892 \pm 0.023$	$7.895 \pm 0.020$	•••	•••		
AQ Pup	$8.690 \pm 0.006$	$7.153 \pm 0.006$	$6.000 \pm 0.006$	$5.484 \pm 0.008$	$5.256 \pm 0.009$	L92
AS Per	•••	•••	$6.941 \pm 0.014$	$6.482 \pm 0.007$	$6.279 \pm 0.017$	M11
T Pup	$7.985 \pm 0.006$	$7.080 \pm 0.006$			•••	•••
AV Sgr	$11.331 \pm 0.021$	$8.851 \pm 0.013$				
W Per	$7.473 \pm 0.140$	•••	$5.222 \pm 0.010$	$4.836 \pm 0.009$	$4.676 \pm 0.010$	M11
XX Cir	$5.887 \pm 0.006$	$4.987 \pm 0.006$				
AY Cas	$11.543 \pm 0.024$					
AY Cen	$8.818 \pm 0.006$	$7.701 \pm 0.006$		•••	•••	
AY Sgr	$10.559 \pm 0.012$	$8.729 \pm 0.009$	$7.140 \pm 0.008$	$6.534 \pm 0.010$	$6.282 \pm 0.016$	M11
BB Her	$10.093 \pm 0.007$	$8.941 \pm 0.010$				
BB Sgr	$6.952 \pm 0.006$	$5.848 \pm 0.006$	$5.025 \pm 0.006$	$4.643 \pm 0.007$	$4.496 \pm 0.008$	L92, W84
E Mon	$10.574 \pm 0.008$	$9.243 \pm 0.008$	$8.265 \pm 0.014$	$7.857 \pm 0.011$	$7.701 \pm 0.024$	M11
F Oph	$7.342 \pm 0.006$	$6.367 \pm 0.006$	$5.626 \pm 0.008$	$5.298 \pm 0.007$	$5.147 \pm 0.009$	L92, W84
G Lac	$8.897 \pm 0.006$	$7.811 \pm 0.014$	$7.023 \pm 0.006$	$6.655 \pm 0.006$	$6.500 \pm 0.006$	B97, M11
BG Vel	$7.653 \pm 0.006$	$6.342 \pm 0.006$				
BK Aur	$9.445 \pm 0.015$		$7.300 \pm 0.015$	$6.890 \pm 0.019$	$6.735 \pm 0.021$	M11
BM Per	$10.428 \pm 0.028$		$6.680 \pm 0.015$	$6.007 \pm 0.012$	$5.724 \pm 0.018$	M11
BM Pup	$10.846 \pm 0.006$	$9.414 \pm 0.006$				
BN Pup	$9.907 \pm 0.016$	$8.585 \pm 0.020$	$7.534 \pm 0.008$	$7.079 \pm 0.009$	$6.880 \pm 0.008$	L92
BP Cas	$10.951 \pm 0.021$					
BZ Cyg	$10.221 \pm 0.006$	$8.327 \pm 0.018$	$6.774 \pm 0.014$	$6.153 \pm 0.010$	$5.879 \pm 0.014$	M11
Dor	$3.737 \pm 0.006$	$2.939 \pm 0.006$	$2.365 \pm 0.006$	$2.038 \pm 0.006$	$1.925 \pm 0.006$	F08, L92
CD Cas	$10.782 \pm 0.009$		$7.644 \pm 0.006$	$7.093 \pm 0.012$	$6.878 \pm 0.012$	M11
CD Cyg	$8.963 \pm 0.009$	$7.498 \pm 0.028$	$6.363 \pm 0.015$	$5.853 \pm 0.012$	$5.668 \pm 0.011$	W84, M11
E Pup	$11.832 \pm 0.010$	$9.968 \pm 0.007$				
CF Cas	$11.138 \pm 0.006$	$9.756 \pm 0.012$	$8.606 \pm 0.010$	$8.136 \pm 0.012$	$7.923 \pm 0.012$	W84, M11
CG Cas	$11.378 \pm 0.000$					
CK Sct		•••	$7.393 \pm 0.006$	$6.822 \pm 0.010$	$6.610 \pm 0.014$	M11
CN Car	$10.684 \pm 0.008$	$9.355 \pm 0.009$	7.575 ± 0.000			
CP Cep	$10.588 \pm 0.012$	$8.766 \pm 0.024$	$7.348 \pm 0.010$	$6.726 \pm 0.012$	$6.492 \pm 0.012$	M11
R Cep	$9.646 \pm 0.008$	$7.979 \pm 0.020$	$6.654 \pm 0.006$	$6.101 \pm 0.007$	$5.890 \pm 0.007$	M11
R Ser	$10.857 \pm 0.009$	$8.899 \pm 0.026$	$7.353 \pm 0.007$	$6.763 \pm 0.007$	$6.503 \pm 0.007$	M11
CS Mon	$11.005 \pm 0.006$	$9.651 \pm 0.006$	7.333 ± 0.007	0.703 ± 0.007	0.303 ± 0.012	
CS Ori	$11.399 \pm 0.037$	$10.261 \pm 0.000$	$9.341 \pm 0.011$	$8.960 \pm 0.009$	$8.810 \pm 0.017$	M11
CS Vel	$11.702 \pm 0.007$	$10.261 \pm 0.019$ $10.069 \pm 0.007$	$8.735 \pm 0.010$	$8.228 \pm 0.014$	$7.973 \pm 0.017$	L92, W84
CV Mon	$10.291 \pm 0.006$	$8.645 \pm 0.006$	$7.323 \pm 0.010$	$6.790 \pm 0.007$	$6.545 \pm 0.007$	L92, W84, M1
CY Car	$9.755 \pm 0.007$	$8.712 \pm 0.006$	7.323 ± 0.011	0.790 ± 0.007	0.545 ± 0.007	L92, W64, WII
- i Cai	7.133 ± 0.001	$0.712 \pm 0.000$	•••	•••		•••

Table 4 (Continued)

Star	V (mag)	I (mag)	J (mag)	H (mag)	$K_S$ (mag)	Reference NIR
CZ Cas	$11.752 \pm 0.009$	$10.059 \pm 0.021$				•••
DD Cas	$9.888 \pm 0.007$	$8.561 \pm 0.025$	$7.537 \pm 0.008$	$7.073 \pm 0.011$	$6.909 \pm 0.014$	M11
DF Cas	$10.879 \pm 0.006$					
DL Cas	$8.971 \pm 0.006$	•••	$6.560 \pm 0.014$	$6.106 \pm 0.011$	$5.912 \pm 0.015$	W84, M11
DW Per	$11.577 \pm 0.008$					
$\delta$ Cep	$3.930 \pm 0.010$		$2.676 \pm 0.006$	$2.393 \pm 0.006$	$2.291 \pm 0.006$	F08, B97
EK Mon	$11.062 \pm 0.006$	$9.617 \pm 0.006$	•••	•••	•••	•••
ER Car	$6.828 \pm 0.006$	$5.961 \pm 0.006$	•••	•••	•••	•••
EX Vel	$11.573 \pm 0.007$	$9.775 \pm 0.006$	•••	•••		•••
EY Car	$10.359 \pm 0.010$	$9.260 \pm 0.008$	•••	•••	•••	•••
Eta Aql	$3.878 \pm 0.006$	$3.024 \pm 0.006$	$2.386 \pm 0.006$	$2.067 \pm 0.006$	$1.951 \pm 0.006$	B97, W84
FI Car	$11.626 \pm 0.010$	$9.855 \pm 0.009$				
FM Aql	$8.278 \pm 0.006$	$6.780 \pm 0.010$	$5.681 \pm 0.006$	$5.217 \pm 0.006$	$5.026 \pm 0.006$	B97, W84, M11
FN Aql	$8.383 \pm 0.006$	$6.992 \pm 0.006$	$5.965 \pm 0.006$	$5.495 \pm 0.006$	$5.315 \pm 0.006$	B97, W84, M11
FN Vel	$10.303 \pm 0.006$	$8.830 \pm 0.007$	7.262   0.011			 M11
GH Cyg	$9.904 \pm 0.006$	$8.432 \pm 0.011$	$7.262 \pm 0.011$	$6.804 \pm 0.006$	$6.598 \pm 0.016$	M11
GI Cyg GQ Ori	$11.745 \pm 0.012 \\ 8.965 \pm 0.011$	$7.885 \pm 0.007$			•••	•••
GU Nor	$10.354 \pm 0.006$	$8.799 \pm 0.007$	•••	•••	•••	•••
GX Car	$9.344 \pm 0.009$	$8.137 \pm 0.007$ $8.137 \pm 0.006$	•••	•••		•••
GY Sge	$10.163 \pm 0.006$	0.137 ± 0.000	$5.604 \pm 0.008$	$4.887 \pm 0.007$	$4.546 \pm 0.006$	L92, W84
HW Car	$9.136 \pm 0.006$	$8.028 \pm 0.006$				
IQ Nor	$9.665 \pm 0.019$	$8.115 \pm 0.020$				
IT Car	$8.102 \pm 0.006$	$7.070 \pm 0.006$				
KK Cen	$11.452 \pm 0.036$	$9.934 \pm 0.026$	•••			
KN Cen	$9.865 \pm 0.006$	$7.994 \pm 0.006$	$6.399 \pm 0.007$	$5.747 \pm 0.008$	$5.440 \pm 0.006$	L92
KQ Sco	$9.835 \pm 0.006$	$7.659 \pm 0.006$	$5.909 \pm 0.012$	$5.215\pm0.010$	$4.901 \pm 0.013$	L92, W84
ℓCar	$3.723 \pm 0.006$	$2.554 \pm 0.006$	$1.679 \pm 0.006$	$1.218\pm0.006$	$1.054 \pm 0.006$	L92
LS Pup	$10.462 \pm 0.007$	$9.073 \pm 0.008$	$7.999 \pm 0.006$	$7.521 \pm 0.007$	$7.312 \pm 0.006$	L92
MW Cyg	$9.483 \pm 0.006$	•••	$6.700 \pm 0.006$	$6.209 \pm 0.009$	$5.998 \pm 0.014$	M11
MZ Cen	$11.553 \pm 0.007$	$9.786 \pm 0.010$	•••	•••	•••	•••
QY Cen	$11.784 \pm 0.006$	$9.350 \pm 0.007$	•••	•••	•••	•••
R Cru	$6.771 \pm 0.006$	$5.901 \pm 0.006$	•••	•••	•••	•••
R Mus	$6.313 \pm 0.006$	$5.497 \pm 0.006$	•••	•••		•••
R TrA RR Lac	$6.656 \pm 0.006$	$5.843 \pm 0.006$ $7.814 \pm 0.015$	 6 077   0 009	 6 629 ± 0.010	 6 499   0 011	 M11
RS Nor	$8.846 \pm 0.006$ $10.019 \pm 0.018$	$8.541 \pm 0.013$	$6.977 \pm 0.008$	$6.628 \pm 0.010$	$6.488 \pm 0.011$	M11
RS Ori	$8.410 \pm 0.011$	$7.282 \pm 0.012$	$6.408 \pm 0.016$	$6.027 \pm 0.017$	$5.880 \pm 0.019$	M11
RS Pup	$7.008 \pm 0.006$	$5.478 \pm 0.006$	$4.341 \pm 0.009$	$3.830 \pm 0.007$	$3.605 \pm 0.008$	L92, W84
RT Aur	$5.469 \pm 0.076$	$4.811 \pm 0.043$	$4.236 \pm 0.008$	$3.998 \pm 0.007$	$3.906 \pm 0.006$	B97, M11
RU Sct			$5.909 \pm 0.008$	$5.298 \pm 0.007$	$5.036 \pm 0.009$	L92, W84, M11
RV Sco	$7.046 \pm 0.006$	$5.907 \pm 0.006$				
RW Cam	$8.657 \pm 0.010$	•••	$5.828 \pm 0.012$	$5.291 \pm 0.013$	$5.093 \pm 0.010$	M11
RW Cas	$9.248 \pm 0.019$	$7.871 \pm 0.020$	$6.841 \pm 0.024$	$6.372 \pm 0.011$	$6.194 \pm 0.026$	M11
RX Aur	$7.670 \pm 0.007$		$5.737 \pm 0.008$	$5.363 \pm 0.011$	$5.233 \pm 0.017$	M11
RX Cam	$7.670 \pm 0.012$	•••	$5.178 \pm 0.023$	$4.732 \pm 0.020$	$4.561 \pm 0.012$	M11
RY CMa	$8.109 \pm 0.006$	$7.133 \pm 0.006$	•••	•••	•••	•••
RY Sco	$7.999 \pm 0.006$	$6.253 \pm 0.006$	$4.899 \pm 0.006$	$4.368 \pm 0.006$	$4.102 \pm 0.007$	L92, W84
RY Vel	$8.376 \pm 0.006$	$6.827 \pm 0.006$	$5.604 \pm 0.008$	$5.124 \pm 0.007$	$4.886 \pm 0.006$	L92, W84
RZ CMa	$9.702 \pm 0.007$	$8.504 \pm 0.007$				
RZ Gem	$10.048 \pm 0.249$		$7.612 \pm 0.010$	$7.169 \pm 0.009$	$6.970 \pm 0.015$	M11
RZ Vel	$7.089 \pm 0.006$	$5.862 \pm 0.006$	$4.889 \pm 0.012$	$4.463 \pm 0.007$	$4.267 \pm 0.006$	L92
S Cru	$6.601 \pm 0.006$	$5.732 \pm 0.006$	4 472 + 0 006	4 125 + 0 006	2 002 + 0 000	
S Mus	$6.133 \pm 0.006$	$5.199 \pm 0.006$ $5.428 \pm 0.006$	$4.473 \pm 0.006$	$4.135 \pm 0.006$	$3.983 \pm 0.008$	L92, W84
S Nor	$6.427 \pm 0.006$ $5.612 \pm 0.006$	$5.428 \pm 0.006$ $4.772 \pm 0.010$	$4.652 \pm 0.006$	$4.286 \pm 0.006$ $3.847 \pm 0.006$	$4.131 \pm 0.008$ $3.732 \pm 0.006$	L92, W84 W84, B97
S Sge S TrA	$5.612 \pm 0.006$ $6.391 \pm 0.006$	$4.772 \pm 0.010$ $5.592 \pm 0.006$	$4.155 \pm 0.006$	$3.847 \pm 0.006$	$3.732 \pm 0.006$	W84, B97 
S ITA SS CMa	6.391 ± 0.006	$5.592 \pm 0.006$ $8.480 \pm 0.010$				
SS Sct		8.460 ± 0.010 	$6.299 \pm 0.008$	$5.938 \pm 0.006$	$5.807 \pm 0.008$	W84, M11
ST Tau	$8.243 \pm 0.014$	$7.171 \pm 0.016$	0.299 ± 0.008	3.938 ± 0.000 	3.807 ± 0.008 	w 64, WIII
	$9.699 \pm 0.006$	$8.286 \pm 0.006$				
ST vei		J.=UU - J.UUU				
ST Vel SU Cyg	$6.855 \pm 0.007$	$6.198 \pm 0.013$	$5.638 \pm 0.007$	$5.397 \pm 0.007$	$5.295 \pm 0.008$	W84, M11

Table 4 (Continued)

Star	V (mag)	I (mag)	J (mag)	H (mag)	$K_S$ (mag)	Reference NIR
SV Per	$8.977 \pm 0.011$	•••	$6.802 \pm 0.021$	$6.360 \pm 0.016$	$6.198 \pm 0.018$	M11
SV Vel	$8.583 \pm 0.006$	$7.329 \pm 0.006$	•••	•••	•••	•••
SV Vul	$7.216 \pm 0.006$	$5.697 \pm 0.009$	$4.571 \pm 0.006$	$4.077 \pm 0.006$	$3.887 \pm 0.006$	W84, L92, B97, M1
SW Cas	$9.713 \pm 0.007$	$8.438 \pm 0.020$	$7.412 \pm 0.009$	$6.987 \pm 0.013$	$6.820 \pm 0.015$	M11
SW Vel	$8.137 \pm 0.014$	$6.850 \pm 0.008$	$5.852 \pm 0.018$	$5.407 \pm 0.012$	$5.203 \pm 0.011$	L92
SX Car	$9.082 \pm 0.006$	$8.039 \pm 0.006$				
SX Per	$11.223 \pm 0.104$		$8.769 \pm 0.010$	$8.352 \pm 0.007$	$8.187 \pm 0.013$	M11
SX Vel	$8.278 \pm 0.006$	$7.262 \pm 0.006$	$6.474 \pm 0.006$	$6.127 \pm 0.006$	$5.965 \pm 0.006$	L92
SY Aur SY Nor	$9.069 \pm 0.009$ $9.520 \pm 0.023$	$7.949 \pm 0.030$	$6.923 \pm 0.009$	$6.530 \pm 0.012$	$6.367 \pm 0.014$	M11 
SZ Aql	$9.520 \pm 0.023$ $8.636 \pm 0.011$	$7.949 \pm 0.030$ $7.082 \pm 0.015$	$5.865 \pm 0.008$	$5.351 \pm 0.006$	$5.138 \pm 0.006$	B97, W84, L92, M1
SZ Aqı SZ Cas	$9.843 \pm 0.006$	$8.110 \pm 0.008$	J.803 ± 0.008	3.331 ± 0.000 	J.138 ± 0.000	D97, W 04, L92, WIT.
SZ Cas SZ Cyg	$9.435 \pm 0.000$ $9.435 \pm 0.011$	$7.798 \pm 0.026$	$6.530 \pm 0.009$	$5.960 \pm 0.007$	$5.732 \pm 0.014$	M11
T Ant	$9.331 \pm 0.006$	$8.523 \pm 0.006$	0.550 ± 0.007	3.700 ± 0.007 	3.732 ± 0.014	
T Cru	$6.570 \pm 0.006$	$5.608 \pm 0.006$	•••	•••		
T Mon	$6.138 \pm 0.006$	$4.987 \pm 0.006$	$4.092 \pm 0.009$	$3.648 \pm 0.009$	$3.487 \pm 0.008$	W84, L92, M11
T Vel	$8.029 \pm 0.006$	$6.964 \pm 0.006$	$6.143 \pm 0.006$	$5.775 \pm 0.006$	$5.605 \pm 0.006$	L92
T Vul	$5.750 \pm 0.006$	$5.077 \pm 0.015$	$4.532 \pm 0.006$	$4.272 \pm 0.006$	$4.174 \pm 0.006$	W84, B97
TT Aql	$7.141 \pm 0.006$	$5.732 \pm 0.009$	$4.671 \pm 0.009$	$4.194 \pm 0.007$	$4.017 \pm 0.006$	W84, M11, B97
TV CMa	$10.587 \pm 0.011$	$9.173 \pm 0.011$	$8.035 \pm 0.008$	$7.588 \pm 0.011$	$7.386 \pm 0.014$	M11
TV Cam	$11.729 \pm 0.018$	***	•••	•••	•••	•••
TW CMa	$9.573 \pm 0.007$	$8.458 \pm 0.007$	$7.577 \pm 0.010$	$7.183 \pm 0.009$	$7.029 \pm 0.017$	M11
TW Nor	$11.670 \pm 0.007$	$9.306 \pm 0.010$	$7.406 \pm 0.022$	$6.705 \pm 0.013$	$6.358 \pm 0.029$	L92, W84
TX Cen	$10.527 \pm 0.006$	$8.618 \pm 0.006$				
TX Cyg	$9.490 \pm 0.012$	$7.225 \pm 0.030$	$5.342 \pm 0.020$	$4.633 \pm 0.018$	$4.323 \pm 0.018$	M11
TX Mon	$10.960 \pm 0.010$	$9.634 \pm 0.008$	$8.581 \pm 0.013$	$8.121 \pm 0.013$	$7.943 \pm 0.017$	M11
TY Sct	$10.821 \pm 0.013$	$8.811 \pm 0.016$	$7.247 \pm 0.011$	$6.637 \pm 0.009$	$6.386 \pm 0.021$	M11
TZ Mon	$10.793 \pm 0.008$	$9.472 \pm 0.006$	$8.458 \pm 0.012$	$8.009 \pm 0.014$	$7.815 \pm 0.016$	M11
TZ Mus	$11.690 \pm 0.006$	$10.144 \pm 0.008$	•••	•••	•••	•••
U Aql	$6.432 \pm 0.006$	$5.271 \pm 0.010$	$4.389 \pm 0.012$	$3.999 \pm 0.009$	$3.844 \pm 0.010$	W84, M11
U Car	$6.284 \pm 0.006$	$5.052 \pm 0.006$	$4.104 \pm 0.007$	$3.674 \pm 0.006$	$3.483 \pm 0.006$	L92, W84
U Nor		•••	$5.825 \pm 0.006$	$5.236 \pm 0.006$	$4.944 \pm 0.006$	L92
U Sgr	$6.697 \pm 0.006$	$5.436 \pm 0.006$	$4.512 \pm 0.006$	$4.100 \pm 0.006$	$3.933 \pm 0.007$	W84, L92, M11
U Vul	$7.122 \pm 0.006$	$5.602 \pm 0.011$	$4.528 \pm 0.009$	$4.093 \pm 0.007$	$3.912 \pm 0.006$	B97, M11
UU Mus		0.010   0.012	$7.439 \pm 0.007$	$6.994 \pm 0.006$	$6.788 \pm 0.006$	L92 
UW Car UX Car	$9.424 \pm 0.008$ $8.295 \pm 0.006$	$8.218 \pm 0.013$	•••			
UX Car UX Per	$8.293 \pm 0.006$ $11.650 \pm 0.018$	$7.554 \pm 0.006$	•••			
UY Car	$8.948 \pm 0.006$	$8.007 \pm 0.010$	•••	•••	•••	
UY Per	$11.319 \pm 0.003$	$9.493 \pm 0.016$	•••	•••	•••	
UZ Car	$9.327 \pm 0.006$	$8.365 \pm 0.006$	•••	•••	•••	•••
UZ Cas	$11.379 \pm 0.007$		•••	•••		
UZ Sct	$11.289 \pm 0.022$	$9.148 \pm 0.035$	$7.418 \pm 0.010$	$6.741 \pm 0.010$	$6.485 \pm 0.016$	M11
V Car	$7.368 \pm 0.006$	$6.433 \pm 0.006$	$5.728 \pm 0.006$	$5.396 \pm 0.006$	$5.249 \pm 0.006$	L92
V Cen	$6.830 \pm 0.006$	$5.794 \pm 0.006$	$4.995 \pm 0.006$	$4.638 \pm 0.006$	$4.479 \pm 0.009$	L92, W84
V Lac	$8.932 \pm 0.007$	•••	•••	•••		
V Vel	$7.586 \pm 0.006$	$6.691 \pm 0.006$	•••	•••		•••
V0339 Cen	$8.714 \pm 0.013$	$7.384 \pm 0.010$	•••	•••	•••	•••
V0340 Ara	$10.228 \pm 0.014$	$8.580 \pm 0.007$	•••	•••	•••	•••
V0340 Nor	$8.403 \pm 0.008$	$7.167 \pm 0.008$	•••	•••	•••	•••
V0350 Sgr	$7.481 \pm 0.006$	$6.435 \pm 0.006$	$5.627 \pm 0.011$	$5.256 \pm 0.011$	$5.130 \pm 0.008$	W84
V0378 Cen	$8.479 \pm 0.006$	$7.260 \pm 0.006$	•••	•••	•••	•••
V0381 Cen	$7.675 \pm 0.006$	$6.791 \pm 0.006$	•••	•••	•••	•••
V0386 Cyg	$9.624 \pm 0.007$	***	$6.375 \pm 0.007$	$5.809 \pm 0.007$	$5.540 \pm 0.015$	M11
V0395 Cas	$10.748 \pm 0.019$	$9.447 \pm 0.035$		•••	•••	•••
V0402 Cyg	$9.864 \pm 0.006$		$7.809 \pm 0.006$	$7.416 \pm 0.006$	$7.263 \pm 0.015$	M11
V0459 Cyg	$10.576 \pm 0.033$	$8.881 \pm 0.019$	$7.613 \pm 0.011$	$7.075 \pm 0.010$	$6.859 \pm 0.016$	M11
V0470 Sco	$11.005 \pm 0.008$	$8.246 \pm 0.007$	•••	•••	•••	•••
V0493 Aql	$11.046 \pm 0.006$		•••	•••	•••	•••
V0496 Aql	$7.769 \pm 0.006$	$6.489 \pm 0.008$	•••	•••	•••	•••
V0496 Cen	$9.945 \pm 0.006$	$8.539 \pm 0.006$	•••	•••	•••	•••
VILIDIAY BALON	$10.502 \pm 0.006$	$9.461 \pm 0.006$	•••	•••	•••	•••
V0508 Mon V0520 Cyg	$10.852 \pm 0.006$	$9.306 \pm 0.029$		•••		

Table 4 (Continued)

Star	V (mag)	I (mag)	J (mag)	H (mag)	$K_S$ (mag)	Reference NIR
V0538 Cyg	$10.449 \pm 0.009$	$8.971 \pm 0.049$	$7.803 \pm 0.007$	$7.311 \pm 0.006$	$7.119 \pm 0.008$	M11
V0600 Aq1	$10.034 \pm 0.006$	$8.281 \pm 0.011$	•••			
V0609 Cyg	$11.026 \pm 0.017$	$8.683 \pm 0.015$	$6.832 \pm 0.013$	$6.128 \pm 0.010$	$5.800 \pm 0.017$	M11
V0636 Cas	$7.183 \pm 0.006$					
V0636 Sco	$6.654 \pm 0.006$	$5.649 \pm 0.006$				
V0733 Aql	$9.976 \pm 0.006$	$9.040 \pm 0.012$	•••	•••	•••	•••
V0737 Cen	$6.724 \pm 0.006$	$5.701 \pm 0.006$	•••	•••	•••	•••
V1154 Cyg	$9.186 \pm 0.006$	$8.180 \pm 0.018$	•••	•••	•••	•••
V1162 Aql	$7.806 \pm 0.006$	$6.850 \pm 0.007$	$6.143 \pm 0.008$	$5.814 \pm 0.017$	$5.682 \pm 0.020$	M11
VV Cas	$10.768 \pm 0.016$	$9.432 \pm 0.018$	$8.328\pm0.008$	$7.885 \pm 0.006$	$7.719 \pm 0.008$	M11
VW Cen	$10.263 \pm 0.007$	$8.783 \pm 0.006$	$7.555 \pm 0.007$	$7.015 \pm 0.006$	$6.775 \pm 0.006$	L92
VW Cru	$9.597 \pm 0.009$	$7.977 \pm 0.006$	•••	•••	•••	•••
VW Pup	$11.393 \pm 0.007$	$10.091 \pm 0.006$	•••	•••	•••	•••
VY Car	$7.460 \pm 0.006$	$6.283 \pm 0.006$	$5.375 \pm 0.015$	$4.943 \pm 0.010$	$4.760 \pm 0.010$	L92, W84
VY Cyg	$9.594 \pm 0.006$	$8.127 \pm 0.019$	$7.009 \pm 0.006$	$6.552 \pm 0.009$	$6.355 \pm 0.010$	M11
VY Per	$11.221 \pm 0.014$	$9.297 \pm 0.026$	•••	•••	•••	•••
VY Sgr	$11.469 \pm 0.012$	$9.129 \pm 0.013$	•••	•••	•••	•••
VZ Cyg	$8.970 \pm 0.008$	$7.966 \pm 0.015$	$7.201 \pm 0.007$	$6.864 \pm 0.006$	$6.721 \pm 0.006$	B97, W84, M11
VZ Pup	$9.657 \pm 0.009$	$8.302 \pm 0.006$	$7.277 \pm 0.007$	$6.830 \pm 0.006$	$6.626 \pm 0.006$	L92
W Gem	$7.012 \pm 0.049$		$5.129 \pm 0.033$	$4.771 \pm 0.026$	$4.656 \pm 0.021$	M11
W Sgr	$4.664 \pm 0.006$	$3.850 \pm 0.006$				
WW Car	$9.750 \pm 0.010$	$8.644 \pm 0.007$				
WW Pup	$10.599 \pm 0.010$	$9.525 \pm 0.007$				
WX Pup	$9.070 \pm 0.007$	$7.968 \pm 0.006$				
WY Pup	$10.599 \pm 0.013$	$9.662 \pm 0.008$				
WZ Pup	$10.320 \pm 0.006$	$9.424 \pm 0.006$				
WZ Sgr	$8.046 \pm 0.011$	$6.544 \pm 0.010$	$5.282 \pm 0.008$	$4.761 \pm 0.006$	$4.538 \pm 0.008$	L92, W84, M11
X Cru	$8.404 \pm 0.006$	•••		•••	•••	
X Cyg	$6.385 \pm 0.009$	$5.236 \pm 0.028$	$4.383 \pm 0.008$	$3.960 \pm 0.006$	$3.799 \pm 0.006$	W84, B97
X Pup	$8.517 \pm 0.011$	$7.161 \pm 0.006$	$6.077 \pm 0.023$	$5.599 \pm 0.011$	$5.386 \pm 0.011$	L92
X Sct	$10.031 \pm 0.017$	$8.613 \pm 0.033$				
X Sgr	$4.548 \pm 0.006$	$3.652 \pm 0.006$	$2.950 \pm 0.007$	$2.635 \pm 0.007$	$2.505 \pm 0.010$	F08, W84
X Vul	$8.834 \pm 0.006$	$7.198 \pm 0.020$	$5.928 \pm 0.010$	$5.433 \pm 0.008$	$5.214 \pm 0.015$	M11
XX Cen	$7.824 \pm 0.006$	$6.743 \pm 0.006$	$5.914 \pm 0.008$	$5.541 \pm 0.006$	$5.375 \pm 0.007$	L92, W84
XX Mon	$11.914 \pm 0.007$	$10.505 \pm 0.009$	•••	•••	•••	•••
XX Sgr	$8.869 \pm 0.006$	$7.506 \pm 0.006$	$6.412 \pm 0.033$	$5.964 \pm 0.018$	$5.799 \pm 0.022$	W84
XX Vel	$10.676 \pm 0.006$	$9.302 \pm 0.006$	•••	•••	•••	•••
XZ Car	$8.597 \pm 0.006$	$7.248 \pm 0.006$	•••	•••	•••	•••
Y Aur	$9.809 \pm 0.044$	•••	$7.660 \pm 0.007$	$7.291 \pm 0.008$	$7.133 \pm 0.026$	M11
Y Lac	$9.159 \pm 0.007$	$8.308 \pm 0.026$	$7.626 \pm 0.006$	$7.316 \pm 0.006$	$7.201 \pm 0.008$	B97, M11
Y Oph	$6.148 \pm 0.006$	$4.533 \pm 0.006$	$3.349 \pm 0.006$	$2.874 \pm 0.006$	$2.662 \pm 0.008$	W84, L92
Y Sct			$6.472 \pm 0.009$	$5.897 \pm 0.011$	$5.646 \pm 0.014$	M11
Y Sgr	$5.739 \pm 0.006$	$4.790 \pm 0.006$		•••		•••
YZ Aur	$10.346 \pm 0.009$	•••	$7.498 \pm 0.015$	$6.905 \pm 0.011$	$6.689 \pm 0.024$	M11
YZ Car	$8.714 \pm 0.006$	$7.438 \pm 0.006$		•••		•••
YZ Sgr	$7.351 \pm 0.006$	$6.226 \pm 0.006$	$5.379 \pm 0.007$	$5.004 \pm 0.009$	$4.861 \pm 0.010$	M11, W84
Z Lac	$8.417 \pm 0.006$	$7.198 \pm 0.043$	$6.235 \pm 0.009$	$5.811 \pm 0.006$	$5.653 \pm 0.008$	B97, M11
Z Sct			$6.962 \pm 0.017$	$6.483 \pm 0.016$	$6.282 \pm 0.017$	M11
$\zeta$ Gem	$3.889 \pm 0.006$	$3.096 \pm 0.006$	$2.538 \pm 0.006$	$2.210 \pm 0.006$	$2.096 \pm 0.006$	F08

**Note.** The magnitudes do not include the reddening correction. The uncertainties are only the random errors and do not include photometric ZP errors. **References.** (B97): Barnes et al. (1997); (F08): Feast et al. (2008); (L92): Laney & Stobie (1992); (M11): Monson & Pierce (2011); (W84): Welch et al. (1984). All magnitudes in *V* and *I* are from Berdnikov (2008).

(This table is available in machine-readable form.)

#### Appendix C

### Data for the Sample of LMC Cepheids

In Table 5 we provide the period, distance, coordinates, photometry, and reddening of the Cepheids in our LMC sample. The sample is described in Section 2.2.

 Table 5

 Sample of Large Magellanic Cloud Cepheids and Their Main Parameters

Cepheid	P (days)	(J2000)	δ (J2000)	d (kpc)	V (mag)	I (mag)	J (mag)	H (mag)	K <sub>S</sub> (mag)	$\frac{E(B-V)}{(\text{mag})}$
0107	8.739	72.214	-69.356	$50.63 \pm 0.56$	14.761	13.947	$13.332 \pm 0.018$	$13.027 \pm 0.015$	$12.941 \pm 0.014$	0.182
0174	15.863	72.719	-69.316	$50.55 \pm 0.56$	14.739	13.666	$12.876 \pm 0.022$	$12.454 \pm 0.020$	$12.312 \pm 0.019$	0.174
0328	34.460	73.599	-70.902	$50.68 \pm 0.56$	13.124	12.088	$11.460 \pm 0.031$	$11.111 \pm 0.027$	$11.001 \pm 0.024$	0.133
0467	22.718	74.301	-67.383	$50.06\pm0.55$	13.704	12.775	$12.113 \pm 0.033$	$11.767 \pm 0.031$	$11.668 \pm 0.029$	0.112
0473	2.634	74.331	-68.821	$50.25 \pm 0.56$	16.335	15.590	$15.093 \pm 0.082$	$14.856 \pm 0.116$	$14.641 \pm 0.114$	0.141
0478	2.764	74.355	-69.567	$50.36 \pm 0.56$	16.160	15.471	$14.961 \pm 0.057$	$14.666 \pm 0.073$	$14.624 \pm 0.076$	0.150
0480	4.035	74.364	-69.355	$50.33 \pm 0.56$	16.865	15.779	$15.107 \pm 0.049$	$14.513 \pm 0.052$	$14.515 \pm 0.080$	0.161
0482	7.466	74.370	-69.227	$50.31 \pm 0.56$	15.655	14.661	$13.977 \pm 0.081$	$13.439 \pm 0.031$	$13.315 \pm 0.030$	0.151
0487	3.109	74.422	-69.406	$50.33 \pm 0.56$	16.221	15.469	$15.002 \pm 0.124$	$14.614 \pm 0.041$	$14.488 \pm 0.090$	0.165
0488	3.647	74.422	-68.800	$50.24 \pm 0.56$	16.535	15.608	$14.921 \pm 0.037$	$14.517 \pm 0.045$	$14.451 \pm 0.066$	0.140
0494	2.727	74.441	-69.062	$50.27 \pm 0.56$	16.973	16.013	$15.441 \pm 0.087$	$14.953 \pm 0.100$	$14.658 \pm 0.091$	0.134
0498	3.630	74.455	-68.720	$50.22 \pm 0.56$	15.914	15.154	$14.617 \pm 0.071$	$14.295 \pm 0.059$	$14.286 \pm 0.061$	0.139
0514	3.504	74.554	-69.203	$50.28 \pm 0.56$	16.276	15.458	$14.879 \pm 0.063$	$14.458 \pm 0.055$	$14.381 \pm 0.068$	0.152
0518	3.249	74.577	-69.367	$50.30 \pm 0.56$	16.550	15.589	$14.988 \pm 0.044$	$14.565 \pm 0.044$	$14.543 \pm 0.046$	0.174
0529	2.856	74.637	-69.041	$50.24 \pm 0.56$	16.603	15.777	$15.168 \pm 0.087$	$14.746 \pm 0.084$	$14.698 \pm 0.087$	0.134
0539	3.455	74.672	-68.865	$50.21 \pm 0.55$	16.064	15.320	$14.758 \pm 0.056$	$14.373 \pm 0.069$	$14.299 \pm 0.054$	0.131
0540	3.750	74.673	-69.526	$50.31 \pm 0.56$	15.841	15.069	$14.574 \pm 0.061$	$14.198 \pm 0.058$	$14.188 \pm 0.056$	0.160
•••	•••	•••	•••	•••		•••		•••	•••	•••

**Note.** The Cepheid names in the first column are of the form OGLE-LMC-CEP-XXXX. The uncertainties on V- and I-band mean magnitudes are 0.02 mag, and the uncertainty on E(B-V) values is 0.017 mag. The distances listed in Column (5) are corrected for their position in the LMC by the equations provided in Section 3.2. Apparent magnitudes in this table are not corrected for the reddening.

(This table is available in its entirety in machine-readable form.)

#### Appendix D

Data for the Sample of SMC Cepheids

In Table 6 we provide the period, distance, coordinates, photometry, and reddening of the Cepheids in our SMC sample. The sample is described in Section 2.3.

 Table 6

 Sample of Small Magellanic Cloud Cepheids and Their Main Parameters

Cepheid	P	α	δ	d	V	I	J	$K_S$	E(B-V)
	(days)	(J2000)	(J2000)	(kpc)	(mag)	(mag)	(mag)	(mag)	(mag)
0443	4.037	10.525	-73.061	$63.36 \pm 0.95$	16.443	15.671	$15.139 \pm 0.018$	$14.742 \pm 0.006$	0.096
0489	3.242	10.734	-73.160	$63.42 \pm 0.95$	16.493	15.822	$15.096 \pm 0.006$	$14.492 \pm 0.010$	0.101
0494	4.758	10.742	-73.335	$63.72 \pm 0.96$	15.884	15.025	$14.447 \pm 0.006$	$14.030 \pm 0.004$	0.103
0495	6.312	10.743	-73.092	$63.30 \pm 0.95$	16.038	15.217	$14.604 \pm 0.012$	$14.164 \pm 0.004$	0.097
0499	6.229	10.751	-73.304	$63.66 \pm 0.96$	15.986	15.258	$14.740 \pm 0.004$	$14.374 \pm 0.006$	0.108
0514	2.542	10.774	-73.082	$63.27 \pm 0.95$	16.842	16.145	$15.687 \pm 0.010$	$15.306 \pm 0.010$	0.097
0518	15.773	10.802	-73.326	$63.67 \pm 0.96$	15.184	14.173	$13.449 \pm 0.002$	$12.948 \pm 0.004$	0.108
0524	10.527	10.828	-73.339	$63.68 \pm 0.96$	15.383	14.536	$13.934 \pm 0.008$	$13.492 \pm 0.006$	0.105
0533	3.909	10.859	-73.254	$63.52 \pm 0.95$	16.122	15.390	$14.895 \pm 0.006$	$14.489 \pm 0.010$	0.105
0551	3.262	10.905	-73.129	$63.28 \pm 0.95$	16.473	15.807	$15.302 \pm 0.006$	$14.954 \pm 0.016$	0.101
0570	10.883	10.947	-73.241	$63.45 \pm 0.95$	15.213	14.354	$13.738 \pm 0.010$	$13.294 \pm 0.004$	0.112
0571	4.897	10.948	-73.335	$63.62 \pm 0.95$	15.872	15.178	$14.662 \pm 0.006$	$14.297 \pm 0.008$	0.104
0576	14.426	10.963	-73.333	$63.61 \pm 0.95$	15.110	14.122	$13.470 \pm 0.016$	$12.923 \pm 0.018$	0.104
0584	4.654	10.989	-73.192	$63.35 \pm 0.95$	16.058	15.296	$14.777 \pm 0.006$	$14.418 \pm 0.006$	0.111
0596	3.072	11.013	-73.277	$63.48 \pm 0.95$	17.170	16.282	$15.673 \pm 0.006$	$15.184 \pm 0.012$	0.120
•••						•••			

**Note.** The Cepheid names in the first column are of the form OGLE-SMC-CEP-XXXX. The uncertainties on V- and I-band mean magnitudes are 0.02 mag, and the uncertainty on E(B-V) values is 0.015 mag. The distances listed in Column (5) are corrected for their position in the SMC by the equations provided in Section 3.3. Apparent magnitudes in this table are not corrected for the reddening.

(This table is available in its entirety in machine-readable form.)

#### Appendix E

Results of the PLZ Fit in Different Conditions

In Table 7 we provide the coefficients of the PLZ relation fitted under different conditions. The various tests are described in Sections 5.1 and 5.2.

Table 7
Results of the PLZ Linear Fit of the Form  $M = \alpha(\log P - 0.7) + \delta + \gamma$  [Fe/H] for Milky Way, Large Magellanic Cloud, and Small Magellanic Cloud Cepheids Fitted Together for Different Conditions

Band	δ	γ	N	Comments
$\overline{V}$	$-3.252 \pm 0.020$	$-0.048 \pm 0.051$	1908	Initial conditions <sup>a</sup>
, I	$-3.948 \pm 0.020$	$-0.138 \pm 0.051$	1907	Initial conditions
$W_{VI}$	$-5.005 \pm 0.022$	$-0.251 \pm 0.057$	1864	Initial conditions
J	$-4.463 \pm 0.022$	$-0.208 \pm 0.051$	1196	Initial conditions
H	$-4.748 \pm 0.020$	$-0.152 \pm 0.092$	905	Initial conditions
$K_S$	$-4.826 \pm 0.019$	$-0.221 \pm 0.050$	1199	Initial conditions
$W_{JK}$	$-5.075 \pm 0.022$	$-0.214 \pm 0.057$	1198	Initial conditions
$\overline{V}$	$-3.274 \pm 0.020$	$-0.084 \pm 0.051$	1908	Gaia EDR3 parallax $ZP = -17 \mu as$
I	$-3.966 \pm 0.020$	$-0.165 \pm 0.050$	1907	Gaia EDR3 parallax $ZP = -17 \mu as$
$W_{VI}$	$-5.020 \pm 0.022$	$-0.275 \pm 0.058$	1864	Gaia EDR3 parallax $ZP = -17 \mu as$
J	$-4.495 \pm 0.022$	$-0.258 \pm 0.052$	1196	Gaia EDR3 parallax $ZP = -17 \mu as$
H	$-4.778 \pm 0.020$	$-0.241 \pm 0.099$	905	Gaia EDR3 parallax $ZP = -17 \mu as$
$K_S$	$-4.857 \pm 0.019$	$-0.271 \pm 0.051$	1199	Gaia EDR3 parallax $ZP = -17 \mu as$
$W_{JK}$	$-5.106 \pm 0.022$	$-0.263 \pm 0.058$	1198	Gaia EDR3 parallax $ZP = -17 \mu as$
$\overline{V}$	$-3.252 \pm 0.020$	$-0.036 \pm 0.052$	1952	$R = 0.7^{\circ}$ around SMC center
I	$-3.948 \pm 0.020$	$-0.130 \pm 0.052$	1951	$R = 0.7^{\circ}$ around SMC center
$W_{VI}$	$-5.005 \pm 0.022$	$-0.252 \pm 0.058$	1908	$R = 0.7^{\circ}$ around SMC center
J	$-4.464 \pm 0.022$	$-0.206 \pm 0.052$	1241	$R = 0.7^{\circ}$ around SMC center
$K_S$	$-4.826 \pm 0.019$	$-0.218 \pm 0.051$	1244	$R = 0.7^{\circ}$ around SMC center
$W_{JK}$	$-5.075 \pm 0.022$	$-0.208 \pm 0.058$	1242	$R = 0.7^{\circ}$ around SMC center
$\overline{V}$	$-3.250 \pm 0.020$	$-0.077 \pm 0.051$	1845	$R = 0.5^{\circ}$ around SMC center
I	$-3.947 \pm 0.020$	$-0.160 \pm 0.053$	1842	$R = 0.5^{\circ}$ around SMC center
$W_{VI}$	$-5.005 \pm 0.022$	$-0.251 \pm 0.059$	1800	$R = 0.5^{\circ}$ around SMC center
J	$-4.462 \pm 0.022$	$-0.225 \pm 0.054$	1132	$R = 0.5^{\circ}$ around SMC center
$K_S$	$-4.825 \pm 0.019$	$-0.234 \pm 0.050$	1132	$R = 0.5^{\circ}$ around SMC center
$W_{JK}$	$-5.075 \pm 0.022$	$-0.222 \pm 0.057$	1132	$R = 0.5^{\circ}$ around SMC center

Note. The slope values are the same as in Table 2.

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a Initial conditions correspond to Gaia EDR3 parallaxes corrected for individual ZP and SMC Cepheids limited to a radius of 0.6° around the SMC center.

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