The future of IMF studies with the ELT and MICADO*

I: The local Universe as a resolved IMF laboratory

K. Leschinski¹ and J. Alves¹

University of Vienna, Department of Astrophysics, Vienna, Austria e-mail: kieran.leschinski@univie.ac.at

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ABSTRACT

Context. Young stellar cluster cores in the local Universe provide the most pristine information available on the stellar Initial Mass Function (IMF), but their stellar densities are too high to be resolved by present-day instrumentation. With a resolving power 100 times better than the Hubble Space Telescope, the MICADO near-infrared camera on the Extremely Large Telescope (ELT) will provide access for the first time to a significant number of dense young stellar clusters critical to direct studies on the universality and shape of the IMF.

Aims. In this work we aim to estimate the lowest stellar mass that MICADO will be able to detect given a stellar density and distance robustly, what instrumental effects will play a critical role, and how many young clusters will be accessible for IMF studies in the local Universe with the ELT.

Methods. We used SimCADO¹, the instrument simulator package for the MICADO camera, to generate observations of 56 dense stellar regions with densities similar to the cores of young stellar clusters. We placed the cluster fields at distances between 8 kpc and 5 Mpc from the Earth implying core densities from 10^2 to 10^5 stars $arcsec^{-2}$ and determined the lowest reliably observable mass for each stellar field via PSF fitting photometry.

Results. Our results show that stellar densities of $<10^3$ stars $\rm arcsec^{-2}$ will be easily resolvable by MICADO. The lowest reliably observable mass in the LMC will be around $0.1~\rm M_{\odot}$ for clusters with densities $<10^3$ stars $\rm arcsec^{-2}$. MICADO will be able to access the stellar content of the cores of all dense young stellar clusters in the Magellanic clouds, allowing the peak and shape of the IMF to be studied in great detail outside the Milky Way. At a distance of 2 Mpc all stars with $\rm M > 2~\rm M_{\odot}$ will be resolved in fields of $<10^4$ stars $\rm arcsec^{-2}$, allowing the high-mass end of the IMF to be studied in all galaxies out to, and including, NGC 300.

Conclusions. We show that MICADO on the ELT will be able to probe the IMF of star clusters 10× denser than what JWST will be able to access, and over 100× denser than those imaged by Hubble. While the sensitivity of MICADO will not allow us to study the brown dwarf regime outside the Milky Way, it will enable access to all stellar members of over 1000 young clusters in the Milky Way and the Magellanic clouds. Furthermore, direct measurements of the Salpeter slope of the IMF will be possible in more than 1500 young clusters out to a distance of 5 Mpc. MICADO on the ELT will be able to measure resolved IMFs for a large ensemble of young clusters under starkly different environments and test the universality of the IMF in the local Universe.

1. Introduction

The stellar Initial Mass Function (IMF), or the spectrum of stellar masses at birth, has implications in almost all fields of astrophysics. On the local scale, the IMF determines the number of available massive stars and with it the fate of a star formation region and creating the environments that emergent planet-forming circumstellar disks will be exposed too. On the large scale, the IMF is irrevocably connected to the composition of the stellar populations in a galaxy and has a critical impact on the mass and energy cycle of a galaxy. The larger the amount of mass locked up in low mass stars, the smaller the reservoir of gas available for the next generation of stars and consequently the smaller the potential for the enrichment of the interstellar medium (ISM). Finally, cosmological simulations of galaxy formation and large scale structure inevitably rely on a universal IMF to determine stellar yields and the strength of feedback mechanisms governing the transport of energy and material.

In his original work, Salpeter (1955) used a single power-law distribution with a slope of 2.35 to describe the IMF for masses between ${\sim}1$ and ${\sim}10\,M_{\odot}$. This description was later modified

to a series of broken power laws to include the stars below the hydrogen-burning limit by Kroupa (2001). Chabrier (2005) proposed a log-normal distribution with a power-law modification for the high mass regions. As both descriptions are empirical and not the prediction from theory, it has proved difficult from observations to decide which of these two descriptions more aptly describes the IMF.

Most observational studies suggest that the shape of the IMF is constant (Lada & Lada 2003; Kroupa 2002; Bastian et al. 2010). Definitive deviations from the accepted IMF form are elusive, and when found, often controversial (van Dokkum & Conroy 2010; Conroy & van Dokkum 2012; Drass et al. 2016). One major challenge hinders a concluding result on the universality of the IMF: directly derived IMFs from star-counts for environments substantially different from the solar neighbourhood. Table 1 shows that even in the closest star forming galaxies like the Magellanic clouds, only the Hubble space telescope (HST) has the sensitivity to reach below one solar mass (see references in Table 1). Long exposures with HST have observed stars just below the first break in the Kroupa power law at 0.5 M_o (Da Rio et al. 2009; Kalirai et al. 2013; Geha et al. 2013), but not far enough into the lower mass regions to put reliable constraints on the shape of the IMF in these extragalactic environments.

^{*} This work uses the instrument simulation package for MICADO, SimCADO: https://simcado.readthedocs.io/

Table 1. A compilation of mass limits for a selection of studies of the IMF outside the Milky Way with the Hubble space telescope. It should be noted that for the study by Gallart et al. (1999) the estimated global star formation history was consistent with a Salpeter slope, rather than a Salpeter slope being extracted from the photometric data.

Galaxy	Target	Distance	Mass range	IMF Slope(s)	Break Mass	Reference
		kpc	${ m M}_{\odot}$		${ m M}_{\odot}$	
LMC	R136	50	2.8-15	2.22		Hunter et al. (1995)
LMC	NGC 1818	50	0.85-9	2.23		Hunter et al. (1997)
LMC	R136	50	1.35-6.5	2.28, 1.27	2.1	Sirianni et al. (2000)
LMC	LH 95	50	0.43-20	2.05, 1.05	1.1	Da Rio et al. (2009)
SMC	NGC 330	62	1-7	2.3		Sirianni et al. (2002)
SMC	NGC 602	62	1-45	2.2		Schmalzl et al. (2008)
SMC		62	0.37 - 0.93	1.9		Kalirai et al. (2013)
Hercules		135	0.52-0.78	1.2		Geha et al. (2013)
Leo IV		156	0.54-0.77	1.3		Geha et al. (2013)
Leo I*		250	0.6-30	2.3		Gallart et al. (1999)

Adding to observers' woes is the lack of spatial resolution. At the distance of the LMC, star forming regions can contain anywhere from 10² to 10⁵ stars arcsec⁻². Figure 1 of Sirianni et al. (2000) shows a perfect example of why current studies struggle to reliably determine the IMF for dense stellar populations outside the Milky Way. The depicted cluster core (R136) is completely dominated by the flux of a few of the brightest stars. Thus studies of the IMF are limited to the outer regions of these clusters where stellar densities are low enough for individual low mass stars to be resolved. Unconstrained mass segregation can also skew the results when considering the IMF in massive clusters (e.g., Ascenso et al. 2009). More importantly, without being able to study the massive clusters in- and outside the Milky Way, it is difficult to make strong assertions on the universality of the IMF. In order to systematically study unambiguously (via star-counts) the lower mass part of the IMF and be able to characterize differences between IMFs, telescopes with higher spatial resolution and better sensitivity than the current generation of ground and space based telescope is needed.

In the middle of the next decade, the era of the extremely large telescopes will begin. ESO's Extremely Large Telescope (ELT) (Gilmozzi & Spyromilio 2007) with the help of advanced adaptive optics (Diolaiti 2010) will have the power to resolve spatial scales at the diffraction limit of a 40m-class mirror. This will provide a linear improvement of a factor of ~15× over HST and a factor of ~6× over the future JWST telescope. With a collecting area of 978 m² the ELT will have at least the same sensitivity as the HST in sparse field and will be able to observe much deeper than HST in crowded fields. The MICADO instrument (Davies et al. 2016, 2018) will be the ELT's first-light near-infrared (NIR) wide-field imager and long slit spectrograph. With a diffraction limit of 7 mas at $1.2\mu m$ and an AO corrected field of view of almost a square arcminute, MICADO will be perfectly suited to address the IMF science case.

The main focus of this paper is to determine to what extent MICADO will improve our ability to study the IMF and other properties of dense stellar populations. More precisely, we have attempted to addressed the following three questions: 1) What is the lowest mass star that MICADO will be able to observe for a given density and distance? 2) What instrumental effects will play a critical role when undertaking such studies with MICADO and the ELT? and 3) How many young clusters will be available for IMF studies with the ELT? In our quest for answers we used SimCADO, the instrument data simulator for MICADO (Leschinski et al. 2016, 2019), to simulate a wide range of densely populated stellar fields at various distances. The cur-

rent version of SimCADO takes into account all the major and most of the minor spatial and spectral effects along the line of sight between the source and the detector. We use the software to generate realistic images of model stellar fields and conduct several iterations of PSF photometry and star subtraction to extract as many stars as possible from the simulated observations. The extracted stars were compared with the input catalogue to determine the completeness of the extraction and to define a "limiting reliably observable mass" for the different stellar field densities and distances.

This paper follows several recent works on resolved stellar populations with Extremely Large Telescopes (e.g., Deep et al. 2011; Greggio et al. 2012; Gullieuszik et al. 2015; Tolstoy 2019). A brief overview of the major MICADO science cases is given in Davies et al. (2016). The latest science cases and simulations for IRIS on the TMT can be found in Wright et al. (2016).

This paper is organised in the following way: Section 2 describes the stellar fields used in our simulations, how the simulations were run, and also describe the algorithm for detecting and subtracting stars in the simulated images. In Section 3 we describe the results of the simulations and discuss their validity in the context of possible future observations of real young stellar clusters. Section 4 summarizes our results.

2. Data sets

The most reliable way to determine the IMF is to look at a population of stars that is still young enough for all (or most) of its original members to be around still, yet old enough that the main phase of star formation activity has ceased. If a population is too young, it will not have finished forming all its stars, and dust extinction will be a significant source of uncertainty and incompleteness. Too old and the most massive members will already have exploded as supernovae. Dynamical effects will also have lead to the evaporation of stars from the cluster, posing a problem to IMF completeness. Unfortunately, such ideal conditions are rarely found. Star formation happens on time scales of 10⁶ years. The most massive stars burn their hydrogen reserves within the first few to several ten million years and move off the main sequence. Given that the dispersion time for stellar clusters is on the order of hundreds of millions of years (e.g., Lada & Lada 2003), at any point in time relatively few of the observable new clusters will be found in the ideal age range (between 5 and 20 Myr) for studying the IMF. The majority of IMF studies focus on the clusters which come closest to meeting these conditions - namely the cores of open clusters (OC) and young massive

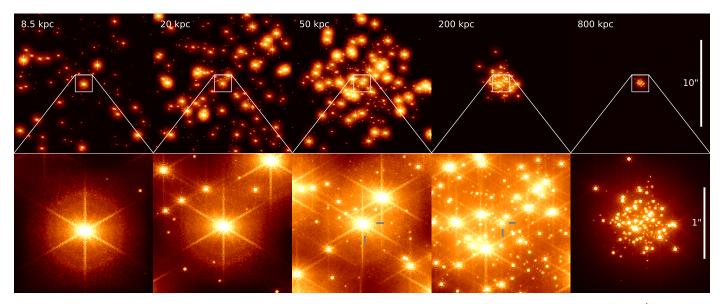


Fig. 1. An illustration of the synthetic data used in this study. The model young massive cluster depicted here contains a mass of $2\times10^4~\rm M_\odot$ (approx. $5\times10^4~\rm stars$) and has a half-light radius of 1 pc, and contains stars in the mass range $[0.01, 100]\rm M_\odot$, sampled from a Kroupa IMF. The model cluster was observed with the MICADO instrument simulator (SimCADO) at distances from 8 kpc to 800 kpc. The top row shows the cluster as seen by the central detector of MICADO, (covering an on-sky area of $16''\times16''$). The bottom row shows a $2''\times2''$ window ($512\times512~\rm pixels$) at the centering of this detector, corresponding to the area we used for our study. Here the unique structure of the ELT's PSF is visible. This Figure illustrates the difficulties that observers will face when studying crowded fields with MICADO and the ELT.

clusters (YMC). OB associations also provide a laboratory for studying the IMF with the apparent advantage that stellar density does not pose a problem. However, as OB associations are spread out over distances as vast as a few hundred parsecs, the chances of contamination from background sources are higher.

2.1. Parameter Space

HST has a diffraction limit of $\sim 0.1''$ at 1.2 μ m and can reach magnitudes as faint as J=28.6^m (Rajan & et al. 2011) in a 10 hour observation. Using AO assisted ground-based instruments on 8 m-class telescopes (similar to NACO at the VLT), diffractionlimited observations can be achieved over small (\sim 1') fields of view. The diffraction limit of the VLT telescope (~0.03"at $1.2 \,\mu\text{m}$) is $\sim 3 \times$ smaller than HST, however, due to the atmospheric background, the sensitivity limits of VLT instruments are many magnitudes brighter than for HST. As boundary conditions for our suite of stellar fields, we took the resolution limit of HST, as cluster cores with densities lower than this are already accessible to the HST. Assuming an average of one star per FWHM of the PSF, our lower density limit was set to 100 stars arcsec⁻². For the upper-density limit, we first took the theoretical diffraction limit of the ELT: 7 mas at $1.2 \,\mu\text{m}$, or $2 \times 10^4 \,\text{stars arcsec}^{-2}$. As we wanted crowding-limited observations at large distances (>1 Mpc), where the faint stars had already dropped below the sensitivity limit, we increased the true stellar density by a factor of 15× so that stars with masses $M > 1 M_{\odot}$ alone would meet the crowding criterion of 1 star per FWHM. Thus we set the upper limit for the true cluster stellar density to 3×10^5 stars arcsec⁻²

Current telescopes are capable of detecting almost all main sequence stars above the hydrogen-burning limit ($\sim\!0.08\,M_\odot$) within a few kiloparsecs of the Sun (e.g. Mužić et al. 2017). Detecting all main sequence stars in clusters further afield, e.g., in the galactic centering and beyond, is where MICADO's increased sensitivity and resolution will bring the most significant breakthroughs. Indeed the question of whether the IMF is truly universal dictates that we study the IMF outside the

Milky Way. Figure 2 illustrates the regions of the IMF that will be available to MICADO at various distances from Earth assuming a sensitivity limit of $K_S = 28^m$. We therefore placed our model proxy-clusters at distances corresponding to important regions which will be critical for studying the effect of the interstellar environment on the IMF, e.g. The Galactic centering (\sim 8 kpc), the LMC (\sim 50 kpc), Leo I dwarf galaxy (\sim 200 kpc), $M33 (\sim 850 \text{ kpc})^1$, NGC 300 ($\sim 2 \text{ Mpc}$), and M83 ($\sim 5 \text{ Mpc}$). Figure 3 shows the parameter space covered by open clusters of average mass ($\sim 1000\,M_\odot$) with radii between 0.1 pc and 3 pc and OB Associations of average mass (~5000 M_{\odot}) with radii between 10 pc and 100 pc as distance from Earth increases. The lower bounds of the open cluster parameter space also cover the cores of YMCs. Average cluster properties were derived for the OB Associations from Mel'Nik & Efremov (1995), for the open clusters from Piskunov et al. (2007), and for the YMCs from Portegies Zwart et al. (2010).

2.2. Artificial stellar fields

Figure 1 shows a model cluster placed at ever increasing distances from Earth. It is evident from Figure 1 that placing a single cluster at different distances would result in inhomogeneous datasets after running our source finding algorithm. In order to create a homogenous dataset that would allow for a direct comparison of the effects of distance and the ELT optics on crowded fields, we generated 56 densely populated stellar fields, that could function as proxies for the dense regions at the cores of young stellar clusters. Each stellar field was generated for a unique combination of stellar density and distance. The parameter space covered by these cluster proxies is shown by the crosses in Figure 3. The size of each stellar field was set at 2"×2"(see section 2.3). The stellar fields were populated by

¹ We recognize that the location of the ELT in the southern hemisphere is unfavorable for effectively observing M33. We provide this data point because M33 will be observable by the Thirty Meter Telescope.

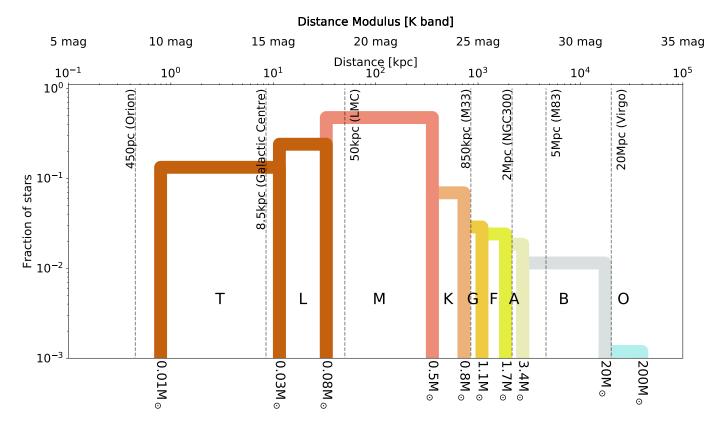


Fig. 2. A qualitative illustration of the observational horizons of main sequence spectral types assuming a sensitivity limit of $K_S = 28^m$ with MICADO and the ELT. The vertical dotted lines show the distance moduli of important regions for studying the IMF in environments significantly different to the solar neighbourhood. This height of each bar corresponds to the cumulative fraction of all stars belonging to a specific spectral type.

continually drawing stars from an IMF until the required stellar density was reached. The mass of each star was drawn at random from an IMF distribution with minimum and maximum masses of $0.01\,M_{\odot}$ and $300\,M_{\odot}$. The IMF followed a standard Kroupa (2001) broken power law distribution². Table 5 from Pecaut & Mamajek (2013)³ was used to obtain the absolute J and Ks magnitudes for each star for the given mass. The requisite distance modulus for the stellar fields was added to give each star an apparent magnitude. We did not include extinction in the distance modulus, as this varies with the line of sight, in particular for Milky Way clusters. Since we are tackling the worst-case scenario, the core of the massive clusters, the stars were assigned random coordinates within the 2"×2"bounding box. Real clusters will have a decreasing radial density profiles except for the inner cluster core radius, which will result in a easier characterization of the IMF over our conservative approach.

2.3. Observations

To "observe" our synthetic stellar fields we used the standard imaging mode of SimCADO⁴ (Leschinski et al. 2016), an open-

source instrument simulator which mimics observations with the wide-field mode of MICADO at the ELT. The core regions of open clusters and YMC have radii on the order of \sim 1 pc (Portegies Zwart et al. 2010). At a distance of 200 kpc (\sim Leo 1 Dwarf), this translates to an angular diameter of \sim 2". Thus we thought it safe to assume that the stellar density within the inner 2"×2" region should remain relatively constant. For the sake of computational effort, we decided to restrict to observations to this 2"×2" window in the centering of the detector.

At the very least dual-band photometry is required to determine the mass of a star. Therefore detections in at least the J and K_S filters are necessary. We deemed a detection in the K_S filter to be critical for any study of the IMF and therefore restricted our observations to this filter. The reason for this is as follows: The sky background in the K_S filter is the highest of all NIR filters and the NIR stellar flux is for all main sequence stars (and many brown dwarfs) weakest in the K_S filter. If a source is undetectable in the K_S filter it will not be possible to determine its mass accurately. Given the AO-nature of the observations and the expected low Strehl ratio at 1.2µm (Clénet et al. 2016), it could be argued that detections in the J filter will be more difficult. Ultimately the fluxes of the stars and the sky are set by nature, whereas the Strehl ratio is a question of engineering and optical design. The stars cannot be made brighter, whereas optical quality can be improved. Hence we deemed a detection in the K_S filter to be the critical point for determining the mass of cluster members.

Exposure times were kept to 1 hour for no other reason than observing time at the ELT will be in very high demand once it

 $^{^{2}}$ By "standard" we mean: $\alpha=0.3$ for M < $0.08M_{\odot}$, $\alpha=1.3$ for $0.08M_{\odot}$ < M < $0.5M_{\odot}$, and $\alpha=2.3$ for M > $0.5M_{\odot}$ as defined in Kroupa (2001)

³ Masses are not given in Table 5, but rather in the online supplement at http://www.pas.rochester.edu/~emamajek/EEM_ dwarf_UBVIJHK_colors_Teff.txt

⁴ For documentation, see: https://simcado.readthedocs.io/. Github code base: https://github.com/astronomyk/SimCADO

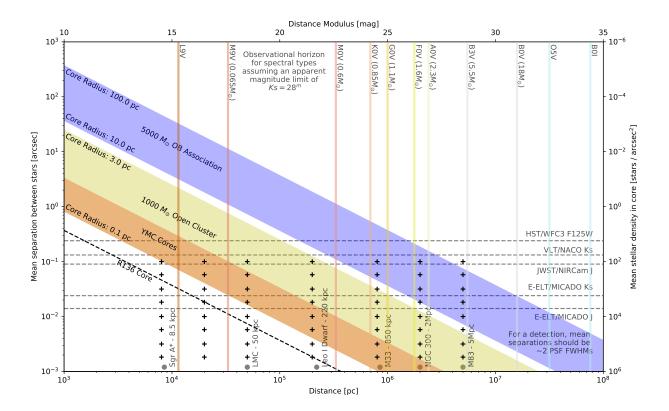


Fig. 3. Stellar density parameter space covered by the dense stellar fields in this study (crosses). The diagonal bands represent the range of core densities for the three major categories of young stellar populations: young massive clusters (orange), open clusters (green), and OB associations (blue). The vertical lines represent the furthest distance at which a particular type of main-sequence star will still be above the detection limit of MICADO, i.e., Ks=28^m. The dashed horizontal lines show the theoretical confusion limit for MICADO/ELT, JWST, HST, and an instrument similar to NACO/VLT. The confusion limit assumes an average minimum distance of 2× the PSF FWHM between stars.

comes online, and observations in two or more filters are needed to accurately determine the mass of stars.

2.4. Source extraction and matching

Figures A.1 and A.2 in the Appendix show a graphical representation of the process described in this section. They show two examples of "observed" stellar fields placed at a distance of 50 kpc and containing 10^3 and 10^4 stars $\operatorname{arcsec}^{-2}$ respectively. The stark features of the SCAO PSF are clearly visible in the images. The diffraction core of the PSF is however still well modeled by a Gaussian distribution. To find and measure the stars in the images we used the following method:

- Find the brightest star in the image with DAOStarFinder from photutils (Bradley et al. 2017)
- 2. Find the centering of the star in a 5×5 pixel window around the coordinates given by DAOStarFinder
- 3. Fit a 2D Gaussian profile to the core of the star
- 4. Scale an image of a reference star to match the amplitude, baseline and offset of the found star
- 5. Subtract the scaled reference star from the image
- 6. Repeat until DAOStarFinder no longer finds any sources above 5 σ

In practice, we found that we could subtract ~100 stars at once and thus greatly increase the speed of the process. The amplitudes and baselines were converted to magnitudes based

on the reference star. Our reference star was a solitary "field" star with a magnitude of $K_S = 15$, observed for the minimum MI-CADO exposure time of 2.6 s so as to maximize the signal-tonoise ratio while not saturating the detector. We calculated the mass of each star based on the observed fluxes in the K_S filter. This step is only permissible because of the simplified context of this study. We were free to equate the luminosity function with an equivalent mass function because all our stellar fields have the intrinsic property that they only contain main sequence stars and the luminosity and mass functions enjoy a one-to-one relationship for this conversion in the K_S filter, mathematically speaking. Furthermore, our primary goal is to determine what the lowest reliably observable mass is, based on how well MI-CADO will perform in crowded fields - not to directly measure the mass of the original stars. We are confident that this step does not significantly detract from achieving the goal of this study.

Finally, we cross-matched the coordinates of the extracted sources with the original table of coordinates to determine what fraction of stars were correctly detected with our algorithm. Due to noise and confusion from stars closer than a few FWHMs, the centroid coordinates of the extracted star were not always exactly equal to the original coordinates. The cross-matching algorithm was instructed to search for the closest star within a 25 mas radius. If a fainter or brighter star happened to be closer, then the algorithm chose that star from the catalog as the match. We determined whether the extracted masses for stars in a certain mass bin were "reliable" by binning the extracted stars according to mass. We then took the mean and standard deviation of all stars

within a mass bin. As long as the mean extracted mass to true mass ratio was in the range 1.0 ± 0.1 and the standard deviation was less than 0.1, the mass bin was classed as reliable. By this definition, the lowest reliably detectable mass for a stellar field was given by the lower edge of the lowest mass bin which satisfied these criteria.

3. Results and Discussion

3.1. The lowest reliably observable masses for given stellar densities and distances.

The first of the questions we asked with this study – "What is the lowest mass star that MICADO will be able to observe reliably for a given density and distance?" – can be answered by Figure 4. For each of the distances and densities, we have plotted the lowest reliable mass bin. The scatter in the plot reflects the random nature of the simulations. The positions of the stars in each of the stellar field were randomised, the sampling of the mass function was random, and the detector and shot noise was applied to the image as part of SimCADO's read-out process. Thus no two stellar fields were the same. Each stellar field configuration was only run once. We, therefore, only have one data point for each density and distance. The bin size used for the reliability statistics was set to 0.2 dex and is the uncertainty in the limiting observable mass.

From Figure 4, we can immediately see the two limiting regimes of sensitivity and crowding. The flat parts of the curves in Figure 4 show the densities for which MICADO will be sensitivity limited at each distance, and the diagonal regions show when crowding becomes the limiting factor. For example, observations of a cluster at a distance of 8 kpc observations will always be crowding limited for densities above 100 stars arcsec⁻². At a distance of 200 kpc observations will be limited by sensitivity up to a density of $10^4 \, stars \, arcsec^{-2}$, thereafter crowding will be the dominant factor. At 5 Mpc all observations will be sensitivity limited. As a reference, we have included the approximate stellar densities for three well known young clusters in Figure 4 if they were located at the distance of the simulated clusters. For example, if the YMC Westerlund 1 were to be located in the LMC, it would fall into the crowding-limited regime for MICADO. The lowest reliably observable mass in the densest region of the core would only be $\sim 0.5 \, M_{\odot}$. This is equivalent to what HST is capable of observing in the outer rim territories of LMC clusters. For clusters in the LMC with stellar densities less than 10³ stars arcsec⁻² MICADO will be limited by sensitivity to masses above $0.1\,M_{\odot}$. While this mass is only $0.3\,M_{\odot}$ lower than what current Hubble observations can achieve, it should be emphasized that this increase of "only" $0.3\,M_\odot$ will reveal the majority of M-type stars, which account for almost three-quarters of all main sequence stars (Ledrew 2001). Given that the limit of current studies is around the 0.5 M_☉ knee from Kroupa (2001), opening up this range will allow future studies to pin down precisely what the shape of the IMF looks like in the dense cores of young LMC clusters.

As previously noted, the exposure time for the simulated images was one hour. By observing for longer times, the lowest observable mass will decrease; however the change is disproportionate to the exposure time. Additional "observations" with SimCADO showed that increasing the exposure time from 1 to 10 hours per cluster only increases the sensitivity limit by around $1.5^{\rm m}$ and $1^{\rm m}$ in the J and $K_{\rm S}$ filters, respectively. For the case of the LMC, this would decrease the lowest observable mass to around $0.06M_{\odot}$, i.e., just below the hydrogen-burning limit.

The majority of young clusters have cores less dense than that of Westerlund 1, and therefore the limiting observable mass will also be lower than the $0.5\,M_\odot$ mass quoted for a Westerlund 1-like YMC in the LMC. Given MICADO's resolving power it will be possible to determine to what extent apparent mass segregation has played a role in previous studies of the IMF in the LMC (Ascenso et al. 2009). More to the point, MICADO will enable us to understand the apparent deviations from the Salpeter IMF as reported by Da Rio et al. (2009), Geha et al. (2013), and Kalirai et al. (2013).

At distances of 100 kpc to 200 kpc and with careful photometry and longer observations MICADO should be able to detect stars down to the sensitivity limit of $0.5\,M_\odot$. This will only be possible though for stellar densities less than 10^4 stars $arcsec^{-2}.$ As a reference, an ONC-like cluster at a distance of 200 kpc would have a stellar density on the order of 10^5 stars $arcsec^{-2}.$ Such observations would be useful for determining the composition of OB associations and sparser (older) open clusters, if there were any present in the non-Magellanic satellites of the Milky Way. Nevertheless, MICADO will still allow us to observe the power-law break at $0.5\,M_\odot$ in the field population of the nearest low metallicity dwarf spheroidal galaxies.

Closer to home MICADO should be able to detect $10\,M_{Jup}$ objects in ONC-like clusters at a distance of 8 kpc (along low extinction lines of sight). An obvious candidate for studies of the IMF in extreme environments is the Arches cluster, given its proximity to the galactic center. The main hindrance to deep observations of the Arches cluster is, somewhat counter-intuitively, not the >2 magnitudes of variable Ks-band extinction along the line of site (Espinoza et al. 2009), but rather the >350 stars in the cluster (Nogueras-Lara et al. 2019) brighter than the saturation limit for MICADO⁵. Indeed there are very few regions in the cores of Milky Way open clusters which do not contain stars brighter than the saturation limit, making deep MICADO observations of these regions difficult.

3.2. The core densities of young star clusters

The second of the questions we asked with this study was, "What instrumental effects will play a critical role when undertaking such studies with MICADO and the ELT?". The instrumental effect which plays the most significant role by far regarding the accuracy of the estimates given here is our knowledge of the PSF. For this study, we used a single SCAO PSF. We assumed that the PSF orientation stayed the same for the length of the observation. Consequently, we had a very good model of our reference star for the PSF subtraction. This will not be the case for real observations as the pupil of the telescope will rotate with respect to the sky, causing an axial broadening of the PSF over the course of an observing run. This broadening should improve the results from our subtraction method as it will smooth out many of the sharp features of the instantaneous PSF that lead to false-positive detections. Information on both the structure of the PSF and the extent of the wings will however be lost due to the rotational broadening. Thus the PSF subtraction algorithm will less accurately be able to estimate the background level when fitting the reference PSF to a star. As a consequence, faint stars caught in the PSF wings of the brighter stars may not be detected as often as they would be if the PSF remained rotationally aligned with the sky. To extract the most stars possible given the shape of

 $^{^5}$ A MICADO internal analysis shows that point sources with magnitudes $K_{\it S}\!>\!14.8\,^{\rm m}$ will saturate the MICADO detectors within the 2.6 s minimum exposure time.

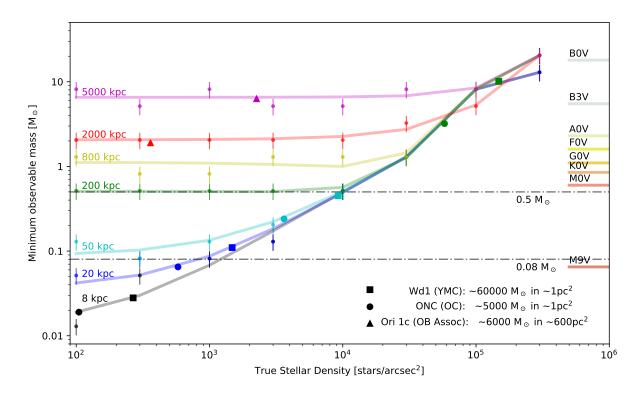


Fig. 4. The lowest observable masses for given stellar densities and distances. The errors in the observable mass are 0.2 dex and correspond to the size of the mass bins used. Two trends are visible in the best fit lines for each distance: a flat regime where the limiting mass is constrained by the sensitivity limit of MICADO, and an exponential regime where crowding becomes the limiting factor. The void to the lower right shows the parameter space in which stars of a given mass will not be observable for a given stellar density.

the ELT PSF, we propose the following hybrid approach: Subtract the brightest stars from each exposure using an instantaneous PSF derived from the brightest stars in that exposure, then stack the residual images and extract the faintest stars using a rotationally broadened PSF. Further investigation is required to determine whether this approach would indeed increase the detection rate for faint stars.

Although it may seem obvious, it is worth mentioning that regardless of the PSF shape, it is clear from our simulations that resolving stellar densities of 10^3 stars $\operatorname{arcsec}^{-2}$ is well within the capabilities of MICADO. With an optimized PSF fitting and subtraction algorithm, extracting upwards of 5×10^3 stars $\operatorname{arcsec}^{-2}$ should also be in the realms of possibility. This is equivalent to approximately one star in an area equivalent to ~2.5 ELT H-band PSF FWHMs. This is similar to being able to resolve every star in the core of an ONC-like cluster in the LMC. For JWST and HST, the equivalent stellar densities are only 160 stars $\operatorname{arcsec}^{-2}$ and 20 stars $\operatorname{arcsec}^{-2}$, respectively. Although MICADO may not have the sensitivity of a space-based telescope, the resolving power will give us full access to the core populations of dense stellar clusters in the major satellites of the Milky Way.

3.3. Opportunities and targets for future observations with MICADO and the ELT

These simulations are a helpful theoretical exercise; however, without an application to observations, they are not all that useful. Figure 5 shows the estimated stellar densities in the cores of the open clusters and YMCs compiled by Portegies Zwart et al.

(2010). The density values, $\log_{10}(\rho)$, only take into account the stars with apparent magnitudes above the sensitivity limit of MI-CADO and thus reflect the "real" observable density for the clusters (also listed in Table A.1). The limits set for HST, JWST, and MICADO are the critical stellar density above which our extraction algorithm struggles to detect and remove more than 90% of the stars in a field. We find that for the Galactic clusters, the resolution of JWST will be sufficient to resolve all stars in most cluster cores down to the sensitivity limit of the instrument.

For clusters in the galactic plane, JWST observations will struggle to disentangle the cluster stars from the field stars. To robustly determine cluster membership, observations of the proper motion of the cluster relative to the field will be required. Stolte et al. (2008) show that the proper motion of the Arches cluster near the Galactic center is ~5 mas yr⁻¹. This equates to around a sixth the size of a pixel in the JWST NIRCam instrument. MICADO, in contrast, will have a plate scale of 1.5 mas in the high-resolution mode, meaning that cluster membership could be determined by observations spaced only several months apart. Greater certainty regarding cluster membership will significantly increase the accuracy of estimates of the cluster IMF based on star counts.

Further afield, resolving the cores of the massive young clusters in the Magellanic clouds will not be possible with JWST. MICADO, however, will enable access to these cluster cores, which in turn will open up to the possibility to study the dynamical processes (e.g., evaporation, core-collapse, etc.) involved in the evolution of extra-galactic clusters. Additionally, observations of a series of LMC clusters with varying ages will give a

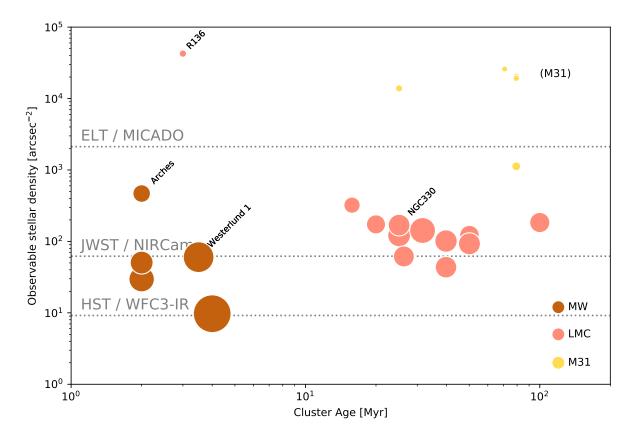


Fig. 5. The stellar densities in the cores of the young massive clusters listed in Table A.1, assuming a sensitivity limit of K_S =28 $^{\rm m}$. While these clusters are spread over the whole sky, only the handful of YMCs in M31 are outside the observing window of the ELT. The sizes of the circles illustrate, roughly, the relative on-sky sizes of the cluster cores. The colours reflect the minimum observable mass, as shown in Figure 4 and listed in Table A.1. Brown: M>0.01M $_{\odot}$; Pink: M>0.1M $_{\odot}$; Yellow: M>0.9M $_{\odot}$. The densities shown here take into account the sensitivity limit and therefore are only for observable stars in each cluster, i.e, stars with K_S >28 $^{\rm m}$ are omitted from the density calculation. This means all stars in the Milky Way, M-type stars and brighter in the LMC, and G-type stars and brighter in M31, are included. The dashed lines in this figure represent the (estimated) limit to the resolving capability of the HST, JWST and ELT. We define the limiting density as the density when the mean distance between stars being equal to 2× the H-band PSF FWHM. Cluster cores of the majority of young clusters outside the Milky Way are far too dense for either HST or JWST observations.

much better picture of how the initial mass function evolves into the present-day mass function, and how the dynamical evolution of the cluster influences the observations, and calculations of, a cluster's IMF.

Portegies Zwart et al. (2010) provides a curated list of the most well known massive young clusters in- and outside the Milky Way. However, many more clusters exist within the local group of galaxies. Indeed to fully understand the environmental dependence on cluster formation and evolution, a statistically significant number of extra-galactic clusters will need to be observed. Figure 6 shows the pool of clusters available to MICADO at the ELT along with the corresponding observational limits of stars of various masses. Within the Milky Way alone, over 500-star clusters become available for which a fully resolved IMF (including the Brown Dwarf regime) could be determined. If the Magellanic clouds are included for studying the region on either side of the IMF peak, this number increases to over 1000 young cluster targets. Out to 2Mpc the resolved high-mass slope of the IMF could be studied in between 1500

and 2500 clusters, including up to 1000 new previously undocumented star clusters⁶.

MICADO will enable IMF studies of fully resolved populations to move from direct IMF measurements of single clusters in and around the solar neighborhood to statistically significant numbers of clusters in a diverse set of environments both in- and outside the Milky Way. Such a statistically meaningful sample of resolved IMFs will hopefully enable a robust determination of any environmental parameters that influence the star formation process, thus answering the major open question of IMF universality.

4. Conclusion

MICADO and the ELT will provide the chance to finally resolve the core populations of dense star clusters in the Local Group. With MICADO observations of young stellar clusters, one can

⁶ This estimate is based on each galaxy's total H_{α} flux with the conversion to an approximate number of clusters based on the H_{α} derived star formation rate and young cluster catalog for M31 (Caldwell et al. 2009).

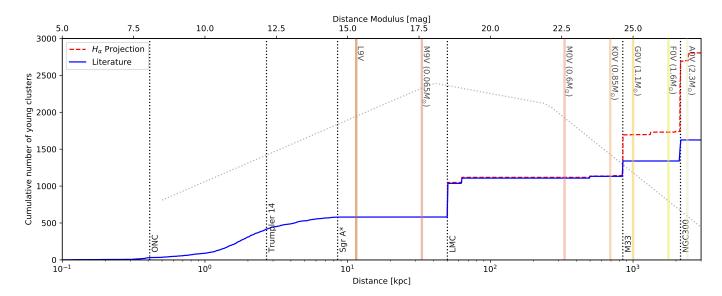


Fig. 6. Cumulative number of young cluster targets that will be available to MICADO ($\delta < +35^{\circ}$) out to 2 Mpc. The blue line shows the cumulative number of young clusters with increasing distance from Earth as reported in catalogs and the literature (see references in Table A.2. The red dotted line shows the expected number of young clusters in a given galaxy based on an extrapolation of a galaxy's star formation rate from its total H_{\alpha} flux (Caldwell et al. 2009). The solid vertical lines represent the observational horizons for given stellar spectral types assuming a detection limit of K=28^m with MICADO at the ELT. The faint dotted grey line represents the regions of the IMF available to study with MICADO at different distances. The population of Milky Way clusters is taken from the HEASARC Milky Way Open Cluster database (Kharchenko et al. 2013) and represents only the clusters located at declinations accessible to the ELT (-85° < $\delta < +35^{\circ}$)

finally answer the question as to whether the IMF distribution is indeed universal, or whether its shape changes when we leave the solar neighborhood. Currently, these answers are locked inside the dense cores of young stellar clusters, as observations of these clusters are primarily limited by confusion.

The main goal of this work was to determine precisely how much more of these stellar populations will be visible to MI-CADO. We tried to answer three questions: What is the lowest mass star that MICADO will be able to observe reliably for a given stellar density and distance? What instrumental effects will play a critical role? How many clusters will be available for IMF studies? In order to answer these, we used the instrument simulator for MICADO (SimCADO) to generate synthetic observations of 56 dense stellar regions corresponding to the cores of young stellar clusters at varying distances from Earth. Here we present a summary of the results:

- 1. We have shown that MICADO will easily be able to resolve all members of a stellar population with a density up to 10^3 stars $arcsec^{-2}$. With proper knowledge of the PSF and an optimized detection and subtraction algorithm densities of 5×10^3 stars $arcsec^{-2}$ should also be achievable.
- 2. Observations with MICADO will enable direct (resolved) observations of the IMF in well over 1500 young clusters in diverse environments within the local group of galaxies. These observations will provide a statistically meaningful sample for robustly quantifying possible IMF variations and the role of environment on the shape of the IMF.
- 3. MICADO's resolution will allow the peak of the IMF $(0.1 \, M_{\odot} < M < 0.5 \, M_{\odot})$ to be extensively investigated in the Magellanic clouds, and the Salpeter slope of the high mass region of IMF out to distances of 5 Mpc (M83).
- 4. Observations focusing on the initial mass function of clusters in the LMC will be limited by sensitivity, not crowding, to $0.1\,M_\odot$.

- 5. Investigations of the transition around the hydrogen burning limit ($\sim 0.08 \, \mathrm{M}_\odot$) will not be possible outside the Milky Way. Instead, brown dwarf populations will be accessible in the cores of the densest Milky Way clusters, e.g. in the Westerlund clusters or the emerging W49A clusters. Objects with masses on the order of $10 \, \mathrm{M}_{Jup}$ will be accessible by MI-CADO for clusters within 8 kpc of Earth. The only caveat is that an appropriate observation strategy must be found to mask the many bright ($\mathrm{m}_{Ks} < 15^m$) stars present in all Milky Way clusters.
- 6. Finally, accurate knowledge of the ELT's PSF will be absolutely essential for good photometry and PSF subtraction algorithms. The sharp structures created by the segmented mirror design will lead to many fake low luminosity star detections if either the PSF is not well known or the extraction algorithm is not capable of differentiating between a star and an artifact of the PSF.

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Appendix A: Supplementary material

Table A.1. The age and observable stellar densities for a selection of young massive clusters found both in and outside the Milky Way, as listed in Portegies Zwart et al. (2010). Only clusters from Portegies Zwart et al. (2010) which have a defined core radius, r_c , are shown. The densities have been calculated to only include stars which are brighter than $Ks=28^m$, as fainter stars will not be detectable by MICADO. The table list the parameters for the clusters shown in Fig. 5.

Galaxy	Cluster	Distance	Age	log(Mass)	Core radius	$\log_{10}(\rho)$	Limiting mass	
•		kpc	Myr	$ m M_{\odot}$	arcsec	stars arcsec ⁻²	$ m M_{\odot}$	
	Cores resolvable by HST							
MW	ONC	0.4	1	3.7	100	-1.6	0.01	
Cores resolvable by JWST								
MW	Trumpler-14	2.7	2	4	10.7	1.1	0.01	
MW	Quintuplet	8.5	4	4.0	24	1.1	0.04	
MW	NGC3603	3.6	2	4.1	8.6	1.2	0.01	
MW	Westerlund-1	5.2	3.5	4.5	15.9	1.7	0.01	
LMC	NGC2214	50	39.8	4.0	7.5	1.9	0.1	
Cores resolvable by MICADO								
LMC	NGC1847	50	26.3	4.4	7.1	2.2	0.1	
LMC	NGC2157	50	39.8	4.3	8.2	2.2	0.1	
LMC	NGC1711	50	50.1	4.2	7.9	2.2	0.1	
LMC	NGC1818	50	25.1	4.4	8.5	2.3	0.1	
LMC	NGC2164	50	50.1	4.2	6.1	2.3	0.1	
SMC	NGC330	63	25.1	4.6	7.7	2.4	0.15	
LMC	NGC2136	50	100	4.3	6.6	2.4	0.1	
MW	Arches	8.5	2	4.3	4.9	2.5	0.04	
LMC	NGC1850	50	31.6	4.9	11	2.5	0.1	
LMC	NGC2004	50	20	4.4	5.8	2.5	0.1	
LMC	NGC2100	50	15.8	4.4	4.1	2.7	0.1	
M31	B257D	780	79.4	4.5	0.8	3.4	0.9	
Only outer regions resolvable by MICADO								
LMC	R136	50	3	4.8	0.41	3.7	0.1	
M31	B066	780	70.8	4.3	0.10	4.2	0.9	
M31	B040	780	79.4	4.5	0.15	4.3	0.9	
M31	B043	780	79.4	4.4	0.19	4.3	0.9	
M31	B318	780	70.8	4.4	0.05	4.4	0.9	
M31	B448	780	79.4	4.4	0.05	4.4	0.9	
M31	Vdb0	780	25.1	4.9	0.37	4.4	0.9	
M31	B327	780	50.1	4.4	0.05	4.5	0.9	
M31	B015D	780	70.8	4.8	0.06	4.6	0.9	

Table A.2. References for the cumulative cluster numbers within a 2 Mpc radius which will be observable by MICADO at the ELT. Star formation rate estimates are based on the integrated galaxy H_{α} fluxes from Karachentsev et al. (2013) and were used to estimate the true number of open clusters contained in each galaxy. The Milky Way clusters were taken from the HEASARC Milky Way Star Cluster catalogue (Kharchenko et al. 2013) and filtered to only include clusters visible to MICADO at the ELT (i.e. Dec < +35 deg).

Name	SFR	Distance	N Clusters	Reference
	$[\mathrm{M}_{\odot}/\mathrm{yr}]$	[kpc]		
MilkyWay		8	590	Kharchenko+13
LMC	0.30	50	456	Glatt+10
SMC	0.05	63	71	Glatt+10
NGC6822	0.01	499	24	Karampelas+09
M33	0.36	847	208	Fan+14
NGC0055	0.45	2128	168	Castro+08
NGC0300	0.18	2148	117	Pietrzynski+01
NGC4214	0.15	2938	52	Andrews+13

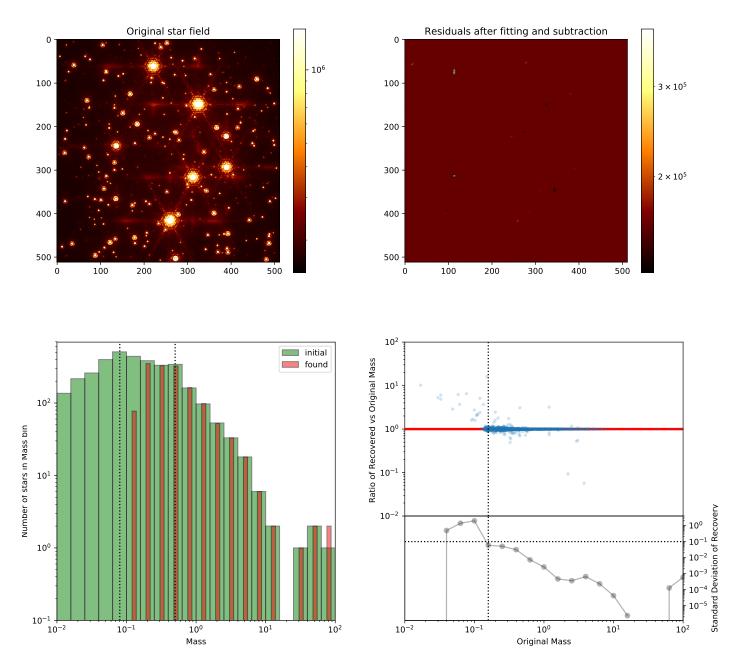


Fig. A.1. Results of extracting stars from a 1000 stars $\operatorname{arcsec^{-2}}$ cluster at a distance of 50 kpc. Top left: The original 2"×2" stellar field with a density of 10^3 stars $\operatorname{arcsec^{-2}}$. The stars in the field have masses between $0.01\,M_\odot$ and $300\,M_\odot$. The PSF used in this study was an instantaneous SCAO PSF, similar to what would be seen on a single MICADO detector $2.6\,s$ exposure. Top right: The same field after our detection and subtraction algorithm has iteratively removed all the stars. 10^3 stars $\operatorname{arcsec^{-2}}$ are extracted reasonably easily by our algorithm. Bottom left: The fraction of extracted stars in each mass bin which matched up with the original list of stars. The majority of stars more massive than $0.1\,M_\odot$ were detected. Bottom right: The upper panel shows the ratio of extracted mass to original mass. The vast majority (~97%) of the almost 4000 stars in the image fell almost perfectly on the red one-to-one line. The minor scatter around the line is due to a combination of our detection algorithm not being able to discern between to very close stars, and contamination for the PSF artefacts, e.g. the segmented diffraction spikes. The lower panel shows the standard deviation of masses around the one-to-one line in a certain mass bin. A mass bin was deemed reliable if the average recovered to original mass ratio was in the range 1±0.1 and the standard deviation was less than 10%.

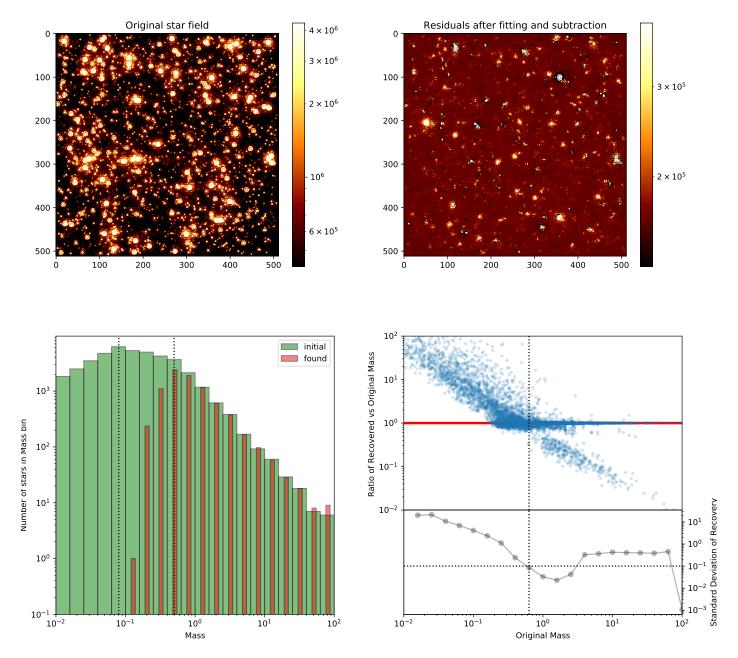


Fig. A.2. Same as Fig. A.1 but for a stellar density of 10^4 stars arcsec⁻². At these densities the number of "double" stars has increased to the point where our detection algorithm was unable to accurately fit and subtract many of the bright stars. Although a large number of incorrect mass determinations are visible in the big blue cloud, still around 60% of the \sim 40 000 sources in this image fall on the red one-to-one line. The segmented PSF meant that the the algorithm detected many fake sources which skewed the detection statistics in both the high and low mass regimes. We are still looking into ways of preventing this from happening in future studies.