

- (G1) A spacecraft of mass  $m$  and velocity  $\vec{v}$  approaches a massive planet of mass  $M$  and orbital velocity  $\vec{u}$ , as measured by an inertial observer. We consider a special case, where the incoming trajectory of the spacecraft is designed in a way such that velocity vector of the planet does not change direction due to the gravitational boost given to the spacecraft. In this case, the gravitational boost to the velocity the spacecraft can be estimated using conservation laws by measuring asymptotic velocity of the spacecraft before and after the interaction and angle of approach of the spacecraft.

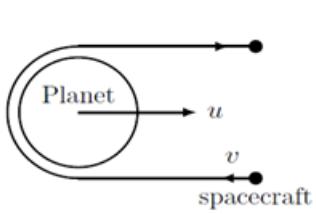


Figure 1

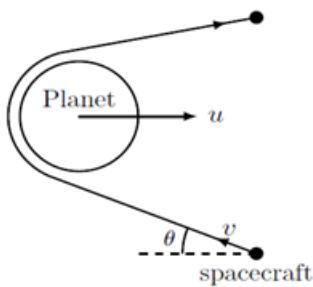


Figure 2

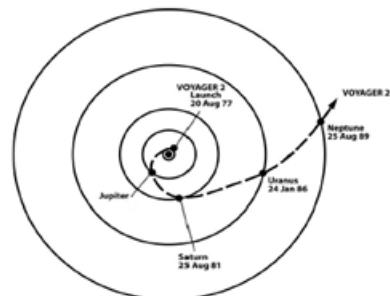


Figure 3

- (G1.1) What will be the final velocity ( $\vec{v}_f$ ) of the spacecraft, if  $\vec{v}$  and  $\vec{u}$  are exactly anti-parallel (see Figure 1). 3
- (G1.2) Simplify the expression for the case where  $m \ll M$ . 1
- (G1.3) If angle between  $\vec{v}$  and  $-\vec{u}$  is  $\theta$  and  $m \ll M$  (see Figure 2), use results above to write expression for the magnitude of final velocity ( $v_f$ ). 3
- (G1.4) Table on the last page gives data of Voyager-2 spacecraft for a few months in the year 1979 as it passed close to Jupiter. Assume that the observer is located at the centre of the Sun. The distance from the observer is given in AU and  $\lambda$  is heliocentric ecliptic longitude in degrees. Assume all objects to be in the ecliptic plane. Assume that the orbit of the Earth to be circular. Plot appropriate column against the date of observation to find the date at which the spacecraft was closest to the Jupiter, and label the graph as G1.4. 8
- (G1.5) Find the Earth-Jupiter distance, ( $d_{E-J}$ ) on the day of the encounter. 4
- (G1.6) On the day of the encounter, around what standard time ( $t_{std}$ ) had the Jupiter transited the meridian in the sky of Bhubaneswar ( $20.27^\circ N$ ;  $85.84^\circ E$ ; UT + 05:30)? 6
- (G1.7) Speed of the spacecraft (in  $km\ s^{-1}$ ) as measured by the same observer on some dates before the encounter and some dates after the encounter are given below. Here day n is the date of encounter. Use these data to find the orbital speed of Jupiter ( $u$ ) on the date of encounter and angle  $\theta$ . 12

date	n-45	n-35	n-25	n-15	n-5	n
v <sub>tot</sub>	10.1408	10.0187	9.9078	9.8389	10.2516	25.5150
date	n+5	n+15	n+25	n+35	n+45	
v <sub>tot</sub>	21.8636	21.7022	21.5580	21.3812	21.2365	

- (G1.8) Find eccentricity,  $e_j$ , of Jupiter's orbit. 8
- (G1.9) Find heliocentric ecliptic longitude,  $\lambda_p$ , of Jupiter's perihelion point. 5

Month	Date	$\lambda$ ( $^{\circ}$ )	Distance (AU)	Month	Date	$\lambda$ ( $^{\circ}$ )	Distance (AU)
June	1	135.8870	5.1589731906	July	17	138.4707	5.3684017790
June	2	135.9339	5.1629499712	July	18	138.5949	5.3722377051
June	3	135.9806	5.1669246607	July	19	138.7183	5.3760047603
June	4	136.0272	5.1708975373	July	20	138.8409	5.3797188059
June	5	136.0736	5.1748689006	July	21	138.9628	5.3833913528
June	6	136.1200	5.1788390741	July	22	139.0841	5.3870310297
June	7	136.1662	5.1828084082	July	23	139.2048	5.3906444770
June	8	136.2122	5.1867772826	July	24	139.3250	5.3942369174
June	9	136.2582	5.1907461105	July	25	139.4448	5.3978125344
June	10	136.3040	5.1947153428	July	26	139.5641	5.4013747321
June	11	136.3496	5.1986854723	July	27	139.6831	5.4049263181
June	12	136.3951	5.2026570402	July	28	139.8016	5.4084696349
June	13	136.4405	5.2066306418	July	29	139.9198	5.4120066575
June	14	136.4857	5.2106069354	July	30	140.0377	5.4155390662
June	15	136.5307	5.2145866506	July	31	140.1553	5.4190683021
June	16	136.5756	5.2185705999	August	1	140.2725	5.4225956100
June	17	136.6202	5.2225596924	August	2	140.3895	5.4261220723
June	18	136.6647	5.2265549493	August	3	140.5062	5.4296486357
June	19	136.7090	5.2305575243	August	4	140.6225	5.4331761326
June	20	136.7532	5.2345687280	August	5	140.7387	5.4367052982
June	21	136.7970	5.2385900582	August	6	140.8546	5.4402367851
June	22	136.8407	5.2426232385	August	7	140.9702	5.4437711745
June	23	136.8841	5.2466702671	August	8	141.0856	5.4473089863
June	24	136.9273	5.2507334797	August	9	141.2007	5.4508506867
June	25	136.9702	5.2548156324	August	10	141.3157	5.4543966955
June	26	137.0127	5.2589200110	August	11	141.4303	5.4579473912
June	27	137.0550	5.2630505798	August	12	141.5448	5.4615031166
June	28	137.0969	5.2672121872	August	13	141.6591	5.4650641822
June	29	137.1384	5.2714108557	August	14	141.7731	5.4686308707
June	30	137.1795	5.2756542053	August	15	141.8869	5.4722034391
July	1	137.2200	5.2799520895	August	16	142.0006	5.4757821220
July	2	137.2600	5.2843175880	August	17	142.1140	5.4793671340
July	3	137.2993	5.2887686308	August	18	142.2272	5.4829586711
July	4	137.3378	5.2933308160	August	19	142.3402	5.4865569133
July	5	137.3754	5.2980426654	August	20	142.4530	5.4901620256
July	6	137.4118	5.3029664212	August	21	142.5657	5.4937741595
July	7	137.4467	5.3082133835	August	22	142.6781	5.4973934544
July	8	137.4798	5.3140161793	August	23	142.7904	5.5010200385
July	9	137.5116	5.3210070441	August	24	142.9024	5.5046540300
July	10	137.5628	5.3312091210	August	25	143.0143	5.5082955377
July	11	137.6898	5.3405592121	August	26	143.1260	5.5119446617
July	12	137.8266	5.3466522674	August	27	143.2375	5.5156014948
July	13	137.9599	5.3516661563	August	28	143.3488	5.5192661222
July	14	138.0903	5.3561848203	August	29	143.4599	5.5229386226
July	15	138.2186	5.3604205657	August	30	143.5709	5.5266190687
July	16	138.3453	5.3644742164	August	31	143.6817	5.5303075275