Fourier spectrum of $n(x,t)$: initial vs final