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## PSO With Variable Accelerator Coefficients

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### Clearing memory, screen, etc.

```
close all; clear all; clc;

global P J JBest PBest GG N_particles N_elements V BLv BUv BLp BUp
global N_iterations GBest lambda
% useful if making any of the following parts into functions

%-----
%
mu_m=42828.375214;           %mars' gravitational parameter [km^3/
s^2]
mu_p=7.113588120963051e-4;   %phobos' gravitational parameter
[km^3/s^2]
R=9376;                     %average distance from m1 and m2 [km]
lambda=mu_p/(mu_m+mu_p);    %mass parameter

%Given DRO for AX=100km
Vy=-0.045620256764708;
T=2.731044880670166e4;
LU=R;
TU=sqrt(R^3/(mu_m+mu_p));

%find DRO for following Ax
Ax=125;
%nondimensional parameters
AX=Ax/LU;
T1=T/TU;
VY=Vy*TU/LU;
%-----
%
```

---

## Basic PSO initialization

```
N_particles = 90;  
% [ ] number of particles to initiate  
  
N_elements = 2;  
  
N_iterations = 800;  
% [ ] number of maximum iterations before PSO is stopped
```

## Particle initialization, particle "position" and "velocity"

```
BLp(1,1) = 1.5*VY; BUp(1,1) = VY;  
BLp(2,1) = T1; BUp(2,1) = 2*pi;  
% [ ] set lower and upper bounds on unknowns (particle elements)  
  
% create particles using uniform distribution according to BLp and BUp  
for k = 1:N_particles  
    for j=1:N_elements  
        P(k,j)=unifrnd(BLp(j,1),BUp(j,1));  
        % could also use the built-in function "unifrnd"  
    end  
end  
  
PBest = zeros(N_particles,N_elements);  
% [ ] initialize the "best" for each particle to all zeros (arbitrary)  
  
GGstar = zeros(1,N_iterations);  
% [ ] initialize the vector of best J's for all iterations  
  
V = zeros(N_particles, N_elements);  
% [ ] initialize particle velocity for each particle  
  
BUv = BUp-BLp; BLv = -BUv;  
% [ ] determine velocity bounds from position  
  
c_I = (1 + rand)/2;  
c_C = 1.49445*rand;  
c_S = 1.49445*rand;  
% [ ] acceleration coefficients (vary with application)
```

## Cost function

```
J = zeros(N_particles);  
for kk = 1:N_particles  
    JBest(kk) = inf;  
end  
GG = inf;  
% [ ] initialization of cost function (J), best overall particle  
    (JBest),
```

---

```
% and overall best cost function obtained (GG)
% NB: change "inf" to "-inf" if maximizing J instead of minimizing
```

## Main PSO computations

```
tic;
% keep track of time it takes to run PSO computations (use profiler to
    see
% where improvements can be made

%initializing r0 vector
r0=[AX+(1-lambda);0];
for j = 1:N_iterations

    %-----
    %
    % Evaluate cost function J for each particle in current iteration
    for i = 1:N_particles

        %integrating the CR3BP EOMs
        v0=[0;P(i,1)];
        y0=[r0;v0];
        timespan=[0 P(i,2)];
        options=odeset('RelTol',1e-12,'AbsTol',1e-12);
        [~,yf]=ode113(@orbitfunCR3BP,timespan,y0,options);
        pos=[yf(end,1);yf(end,2)];
        vel=[yf(end,3);yf(end,4)];
        %evaluating cost function
        J(i)= norm(pos-r0)+norm(vel-v0);
    end

    %-----
    %
    % Evaluate PBest and GBest (best particle and best cost)
    for i = 1:N_particles
        if J(i) < JBest(i)
            PBest(i,:) = P(i,:);
            JBest(i) = J(i);
        end
    end

    for i = 1:N_particles
        if J(i) < GG
            GG = J(i);
            GBest = P(i,:);
        end
    end

    % Update particle velocity
    for i = 1:N_particles
```

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---

```

V(i,:) = c_I*V(i,:) + c_C*(PBest(i,:) - P(i,:)) + ...
    c_S*(GBest - P(i,:));
% new particle velocity

% check if boundaries are being respected
for k = 1:N_elements
    if V(i,k) < BLv(k)
        V(i,k) = BLv(k);
    end
    if V(i,k) > BUv(k)
        V(i,k) = BUv(k);
    end
end
end

% update particle position for each particle
for i = 1:N_particles

    P(i,:) = P(i,:) + V(i,:);
    % new particle position

    % check position boundaries
    for k = 1:N_elements
        if P(i,k) < BLp(k)
            P(i,k) = BLp(k);
            V(i,k) = 0;
        end
        if P(i,k) > BUp(k)
            P(i,k) = BUp(k);
            V(i,k) = 0;
        end
    end
end

GGstar(j) = GG;

% give progress updates to the screen every 10%
if mod(j/N_iterations*100,10) == 0
    clc; fprintf('Progress: %2.0f %%\n',j/N_iterations*100)
end

end

plot(yf(:,1),yf(:,2))
axis equal
PSOtime = toc;
% [s] time it takes to run PSO

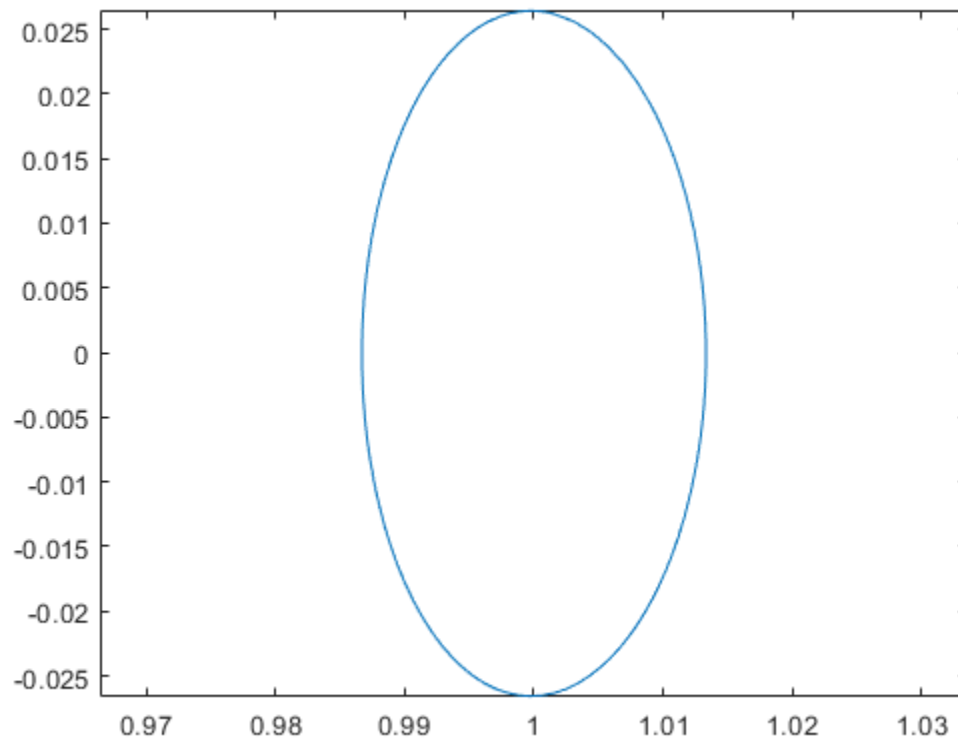
time = datestr(now, 'yyyy_mm_dd');
filename = sprintf('PSO_%s.mat',time);
save( fullfile('', filename) )
% save workspace with today's date

```

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---

Progress: 10 %  
Progress: 20 %  
Progress: 30 %  
Progress: 40 %  
Progress: 50 %  
Progress: 60 %  
Progress: 70 %  
Progress: 80 %  
Progress: 90 %  
Progress: 100 %



## Final Results

```
fprintf('\nThe particle with best J is: \n'); disp(GBest)
fprintf('\nAnd its corresponding best J is: \n'); disp(GG)
fprintf('The y component of the velocity for Ax = %i is:\n%1.8f km/s
\n',Ax,GBest(1,1)*LU/TU)
fprintf('The orbital period for Ax = %i is:\n%1.8f s
\n',Ax,GBest(1,2)*TU)
% output run time to the screen
if PSotime > 3600
    fprintf('\nThe PSO algorithm took %2.2f hours to complete
\n',PSotime)
elseif PSotime > 60
    fprintf('\nThe PSO algorithm took %2.2f minutes to complete
\n',PSotime)
```

---

```

else
    fprintf('\nThe PSO algorithm took %2.4f seconds to complete
\n',PSOtime)
end

%figure of J vs. iteration number (semilog plot if J > 0 for all J's)
if GGstar(end) > 0
    figure; semilogy(1:N_iterations, GGstar)
    title('J vs. Iteration Number')
    xlabel('Iteration Number'); ylabel('J (Cost Function)');
    grid on; set(gca,'FontSize',20);
else
    figure; plot(1:N_iterations, GGstar)
    title('J vs. Iteration Number')
    xlabel('Iteration Number'); ylabel('J (Cost Function)');
    grid on; set(gca,'FontSize',20);
end

% script ends here

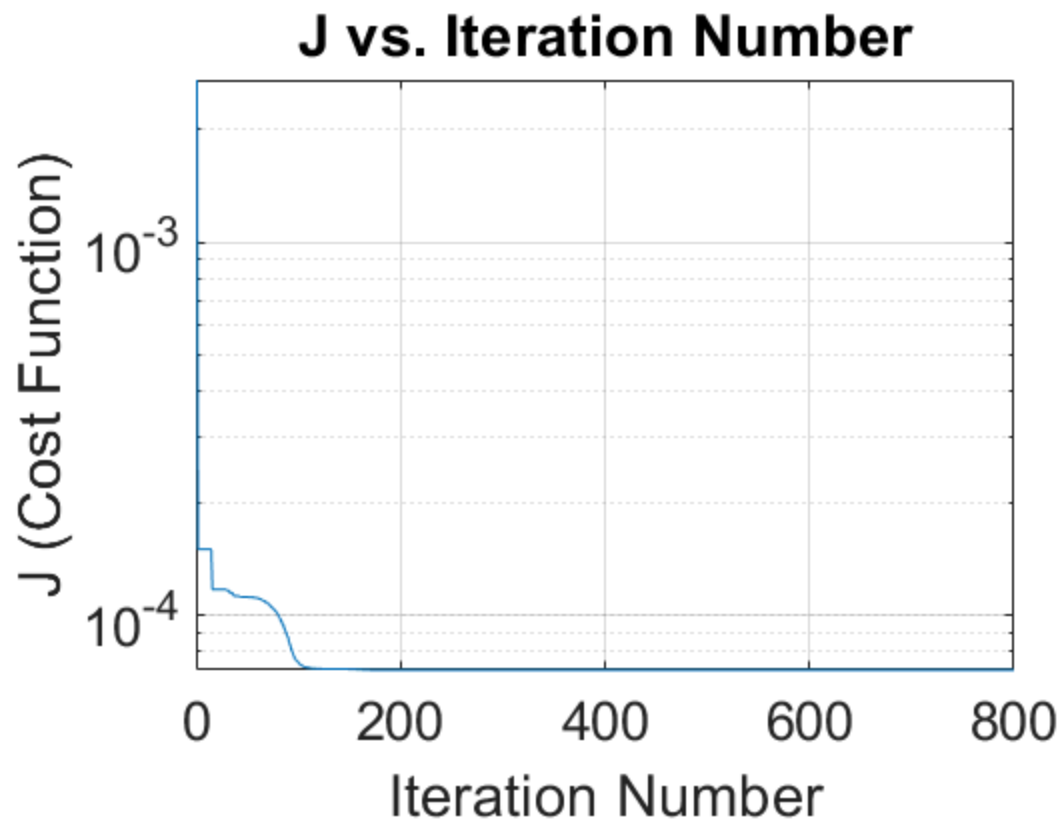
```

*The particle with best J is:*  
-0.0266      6.2477

*And its corresponding best J is:*  
7.1492e-05

*The y component of the velocity for Ax = 125 is:*  
-0.05688311 km/s  
*The orbital period for Ax = 125 is:*  
27408.20516624 s

*The PSO algorithm took 513.24 minutes to complete*



*Published with MATLAB® R2020a*