# Better than Chance: the importance of null models

http://users.soe.ucsc.edu/~karplus/papers/
better-than-chance-sep-11.pdf

Kevin Karplus karplus@soe.ucsc.edu

Biomolecular Engineering Department University of California, Santa Cruz

13 Sept 2011



#### **Outline of Talk**

- What is a protein?
- 4 The folding problem and variants on it.
- & What is a null model (or null hypothesis) for?
- Example 1: is a conserved ORF a protein?
- Example 2: is residue-residue contact prediction better than chance?
- Example 3: how should we remove composition biases in HMM searches?



## What is a protein?

- There are many abstractions of a protein: a band on a gel, a string of letters, a mass spectrum, a set of 3D coordinates of atoms, a point in an interaction graph, ....
- For us, a protein is a long skinny molecule (like a string of letter beads) that folds up consistently into a particular intricate shape.
- The individual "beads" are amino acids, which have 6 atoms the same in each "bead" (the *backbone* atoms: N, H, CA, HA, C, O).
- The final shape is different for different proteins and is essential to the function.
- The protein shapes are important, but are expensive to determine experimentally.

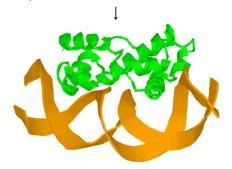


#### **Folding Problem**

The *Folding Problem*:

If we are given a sequence of amino acids (the letters on a string of beads), can we predict how it folds up in 3-space?

MTMSRRNTDA ITIHSILDWI EDNLESPLSL EKVSERSGYS KWHLQRMFKK ETGHSLGQYI RSRKMTEIAQ KLKESNEPIL YLAERYGFES QQTLTRTFKN YFDVPPHKYR MTNMQGESRF LHPLNHYNS







## Fold-recognition problem

The Fold-recognition Problem:

Given a sequence of amino acids *A* (the *target* sequence) and a library of proteins with known 3-D structures (the *template* library),

figure out which templates *A* match best, and align the target to the templates.

- 4 The backbone for the target sequence is predicted to be very similar to the backbone of the chosen template.
- Progress has been made on this problem, but we can usefully simplify further.



## **Remote-homology Problem**

The *Homology Problem*: Given a target sequence of amino acids and a library of protein *sequences*, figure out which sequences *A* is similar to and align them to *A*.

- No structure information is used, just sequence information. This makes the problem easier, but the results aren't as good.
- This problem is fairly easy for recently diverged, very similar sequences, but difficult for more remote relationships.



#### Scoring (Bayesian view)

- A model M is a computable function that assigns a probability P(A | M) to each sequence A.
- & When given a sequence A, we want to know how likely the model is. That is, we want to compute something like P(M | A).
- & Bayes Rule:

$$P(M \mid A) = P(A \mid M) \frac{P(M)}{P(A)}.$$

 $\triangle$  Problem: P(A) and P(M) are inherently unknowable.



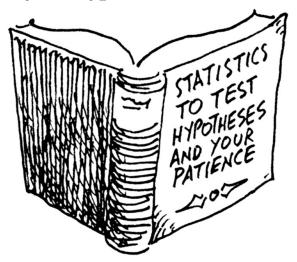
#### **Null models**

Standard solution: ask how much more likely *M* is than some *null hypothesis* (represented by a *null model N*):

$$\frac{\frac{P(M \mid A)}{P(N \mid A)}}{\frac{P(N \mid A)}{P(N \mid A)}} = \frac{\frac{P(A \mid M)}{P(A \mid N)}}{\frac{P(M)}{P(N)}} \cdot \frac{\frac{P(M)}{P(N)}}{\frac{P(N)}{P(N)}}.$$
posterior odds



# **Test your hypothesis**



Thanks to Larry Gonick The Cartoon Guide to Statistics



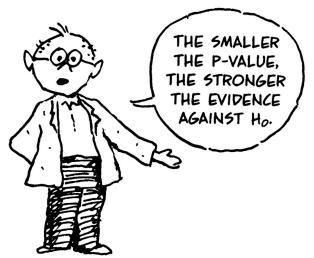
#### **Scoring (frequentist view)**

- We believe in models when they give a large score to our observed data.
- & Statistical tests (p-values or E-values) quantify how often we should expect to see such good scores "by chance".
- These tests are based on a null model or null hypothesis.





## Small p-value to reject null hypothesis



Thanks to Larry Gonick The Cartoon Guide to Statistics



## **Statistical Significance (2 approaches)**

Markov's inequality For any scoring scheme that uses

$$\ln \frac{P(\operatorname{seq} \mid M)}{P(\operatorname{seq} \mid N)}$$

the probability of a score better than T is less than  $e^{-T}$  for sequences distributed according to N.

Parameter fitting For "random" sequences drawn from some distribution other than N, we can fit a parameterized family of distributions to scores from a random sample, then compute P and E values.

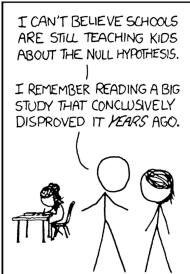


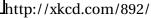


#### **Null models**

- A P-values (and E-values) often tell us nothing about how good our hypothesis is.
- & What they tell us is how bad our null model (null hypothesis) is at explaining the data.
- & A badly chosen null model can make a very wrong hypothesis look good.

#### xkcd







## **Example 1: long ORF**

- A colleague found an ORF in an archæal genome that was 388 codons long and was wondering if it coded for a protein and what the protein's structure was.
- & We know that short ORFs can appear "by chance".
- So how likely is this ORF to be a chance event?

#### Null Model 1a: no selection

- **G+C** content bias. (GC is 35.79%, AT is 64.21%.)
- Probability of start codon
  ATG = 0.321\*0.321\*0.179 = 0.01845
- Probability of stop codon
  TAG= 0.1845, TGA=0.01845, TAA=0.0331, so p(STOP)=0.06999
- (ATG, 387 codons without stop) =  $p(ATG)(1 p(STOP))^{387} = 1.18e 14$
- & E-value in double-strand genome (6e6 bases)  $\approx 7.05e 08$ .
- & We can easily reject this null hypothesis!





#### Null Model 1b: codon (3-mer) bias

- Count 3-mers in double-stranded genome.
- Probability of ATG start codon: 0.01567
- Probability of stop codon: 0.07048
- ATG, 387 codons without stop) =  $p(ATG)(1 p(STOP))^{387} = 8.15e 15$
- **♣** E-value in genome  $\approx 4.87e 08$ .
- We can easily reject this null hypothesis!



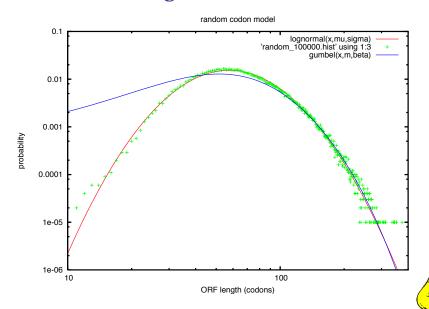


## Null Model 2: reverse of gene

- ORF is on the opposite strand of a known 560-codon thermosome gene!
- What is the probability of this long an ORF, on opposite strand of known gene?
- Generative model: simulate random codons using the codon bias of the organism, take reverse complement, and see how often ORFs 388-long or longer appear.
- $\stackrel{\blacktriangleleft}{\mathbf{L}}$  Taking 100,000 samples, we get estimates of P-value  $\approx 1.5e-05$
- $\stackrel{\blacktriangleleft}{\$} \approx 3000$  genes, giving us an E-value  $\approx 0.045$
- 4 Hard to reject null!

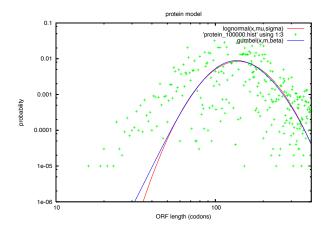


# Null Model 2 histogram



#### **Null Model 3**

- & Same sort of simulation, but use codons that code for the right protein on the forward strand.
- & P-value and E-value  $\approx 0.0025$  for long ORFs on the reverse strand of genes coding for this protein.

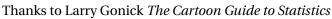






#### **Protein or chance ORF?**







#### Not a protein

- + A tblastn search with the sequence revealed similar ORFs in many genomes.
- All are on opposite strand of homologs of same gene.
- "Homologs" found by tblastn often include stop codons.
- There is no evidence for a TATA box upstream of the ORF.
- No strong evidence for selection beyond that explained by known gene.

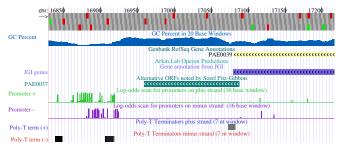
**Conclusion:** it is rather unlikely that this ORF encodes a protein.





#### Example 1b: another ORF

pae0037: ORF, but probably not protein gene in *Pyrobaculum aerophilum* 



- A Promoter on wrong side of ORF.
- ligh GC content (need local, not global, null)
- & Strong RNA secondary structure.





## **Example 2: contacts**

- Is residue-residue contact prediction better than chance?
- Early predictors (1994) reported results that were 1.4 to 5.1 times "better than chance" on a sample of 11 proteins.
- But they used a uniform null model:

P(residue i contacts residue j) = constant.

4 A better null model:

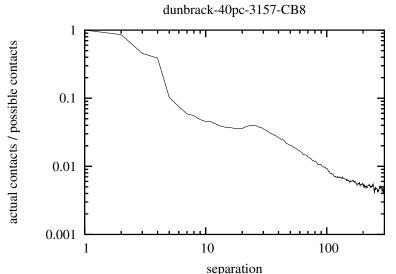
$$P(\text{residue } i \text{ contacts residue } j) = P(\text{contact } | \text{ separation} = |i-j|).$$





#### P(contact|separation)

Using CASP definition of contact, CB within 8 Å, CA for GLY.







#### Can get accuracy of 100%

- & By ignoring chain separations, the early predictors got what sounded like good accuracy (0.37–0.68 for L/5 predicted contacts)
- & But just predicting that i and i+1 are in contact would have gotten accuracy of 1.0 for even more predictions.
- More recent work has excluded small-separation pairs, with different authors choosing different thresholds.
- $\triangle$  CASP uses separation  $\geq 6$ ,  $\geq 12$ , and  $\geq 24$ , with most focus on  $\geq 24$ .





## Separation as predictor

If we predict all pairs with given separation as in contact, we do much better than uniform model.

sep	P(contact    i-j  = sep)	$P(\text{contact}    i-j  \ge \text{sep})$	"better than chance"
6	0.0751	0.0147	4.96
9	0.0486	0.0142	3.42
12	0.0424	0.0136	3.13
24	0.0400	0.0116	3.46



# **Evaluating contact prediction**

Two measures of contact prediction:

Accuracy:

$$\frac{\sum \chi(i,j)}{\sum 1}$$

Weighted accuracy:

$$\frac{\sum \chi(i,j) / P\left(\text{contact} \mid \text{separation} = |i-j|\right)}{\sum 1}$$

= 1 if predictions no better than chance, independent of separations for predicted pairs.

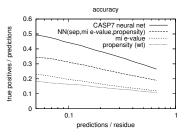


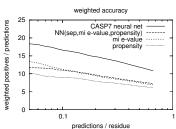
## **CASP7 Contact prediction**

- Use mutual information between columns of thinned alignment (≤ 50% identity)
- & Compute e-value for mutual info (correcting for small-sample effects).
- Compute rank of e-value within protein.
- Feed log(e-value), log(rank), contact potential, joint entropy, and separation along chain for pair, and amino-acid profile, predicted burial, and predicted secondary structure for window around each residue of pair into a neural net.

## Now doing better

 $separation \geq 9$  Predictions/residue taken separately for each protein.

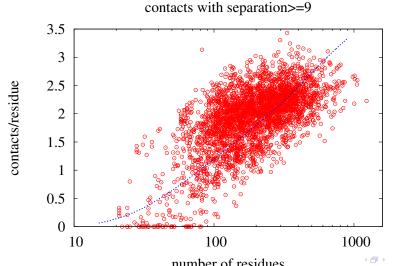






#### Contacts per residue

We can also use our null model to predict the number of contacts per residue (which is not a constant).





#### **Example 3: HMM**

- Hidden Markov models assign a probability to each sequence in a protein family.
- A common task is to choose which of several protein families (represented by different HMMs) a protein belongs to.



#### Standard Null Model

Null model is an i.i.d (independent, identically distributed) model.

$$P(A \mid N, len(A)) = \prod_{i=1}^{len(A)} P(A_i)$$
.

$$P(A \mid N) = P(\text{sequence of length len}(A))$$

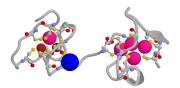
$$\prod_{i=1}^{\text{len}(A)} P(A_i).$$

## Composition as source of error

- When using the standard null model, certain sequences and HMMs have anomalous behavior. Many of the problems are due to unusual composition—a large number of some usually rare amino acid.
- For example, metallothionein, with 24 cysteines in only 61 total amino acids, scores well on any model with multiple highly conserved cysteines.

# **Composition examples**

#### Metallothionein Isoform II (4mt2)



Kistrin (1kst)



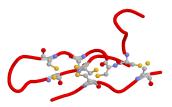


# **Composition examples**

Kistrin (1kst)



Trypsin-binding domain of Bowman-Birk Inhibitor (1tabl)





#### Reversed model for null

- & We avoid this (and several other problems) by using a reversed model  $M^r$  as the null model.
- $\clubsuit$  The probability of a sequence in  $M^r$  is exactly the same as the probability of the reversal of the sequence given M.
- This method corrects for composition biases, length biases, and several subtler biases.



## Helix examples

Tropomyosin (2tmaA)



Colicin Ia (1cii)

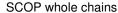


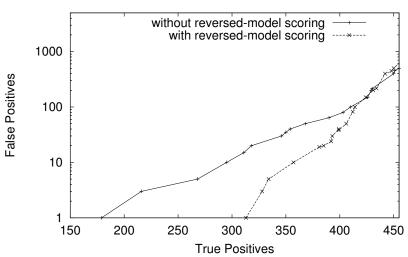
Flavodoxin mutant (1vsgA)



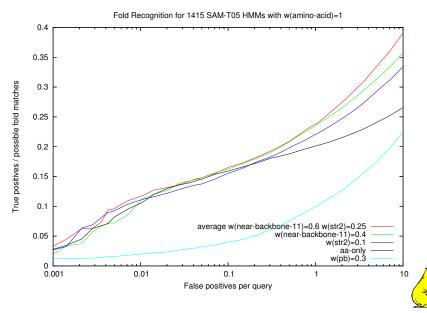


## Improvement from reversed model





#### Fold recognition results



#### **Take-home messages**

- Base your null models on biologically meaningful null hypotheses, not just computationally convenient math.
- Generative models and simulation can be useful for more complicated models.
- Picking the right model remains more art than science.



#### Web sites

```
These slides: http://users.soe.ucsc.edu/~karplus/papers/better-than-chance-sep-11.pdf
```

Reverse-sequence null: Calibrating E-values for hidden Markov models with reverse-sequence null models.

Bioinformatics, 2005. 21(22):4107–4115;
doi:10.1093/bioinformatics/bti629

Archæal genome browser: http://archaea.ucsc.edu

#### **UCSC** bioinformatics degree info:

http://www.bme.ucsc.edu/programs/



