



# 16 Advanced BFS

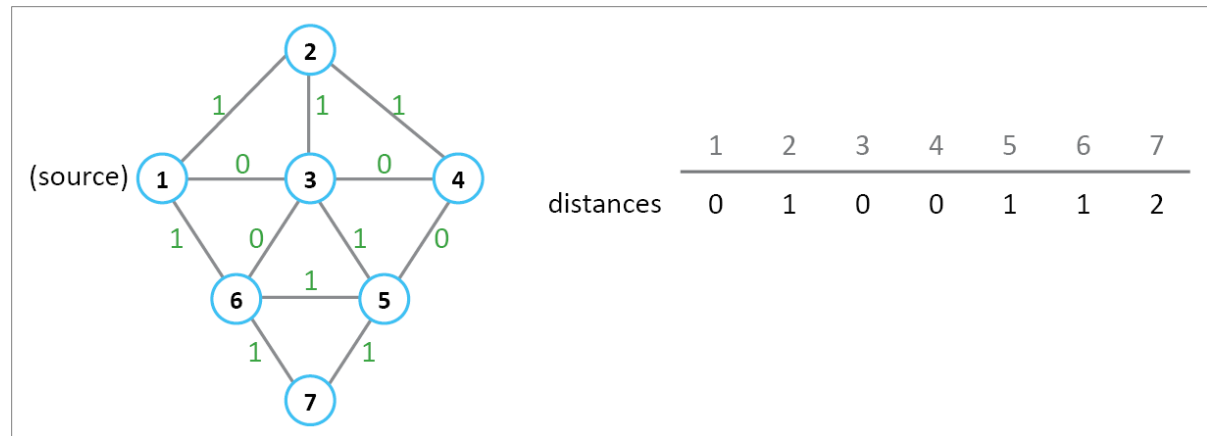
# 01 BFS

Sample Input

```
7 12
1 6 1
1 2 1
2 4 1
4 5 0
5 6 1
6 3 0
3 1 0
2 3 1
3 4 0
3 5 1
6 7 1
7 5 1
```

Sample Output

```
0 1 0 0 1 1 2
```



# Exercise 1: Matrix

Given a matrix of size  $N \times M$  consisting of integers 1, 2, 3 and 4. Each value represents one of the four possible movements from that cell:

1 : move up

2 : move right

3 : move down

4 : move left

There is no diagonal movement.

What is the minimum number of possible changes required in the matrix so that there exists a path from top-left cell (1, 1) to the bottom-right cell (N, M).

## Sample Input

```
3 4
3 2 3 3
2 1 4 3
1 3 2 1
```

## Sample Output

```
1
```



# BFS with Splitting Edges

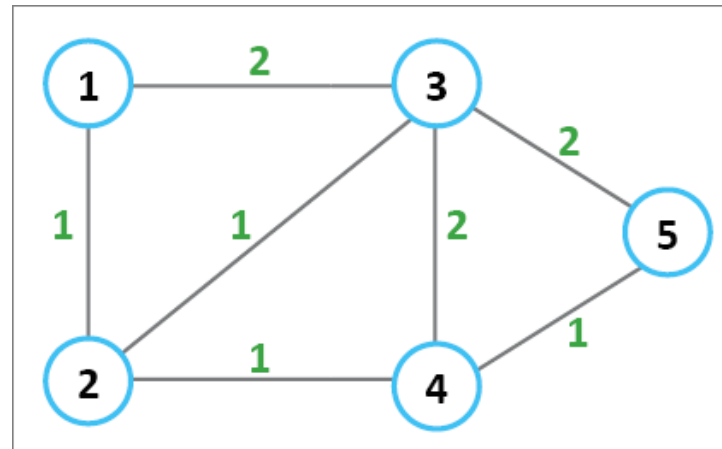
Calculate the distance of the shortest path from node 1 to node N in an undirected weighted graph where the edge costs are either 1 or 2.

## Sample Input

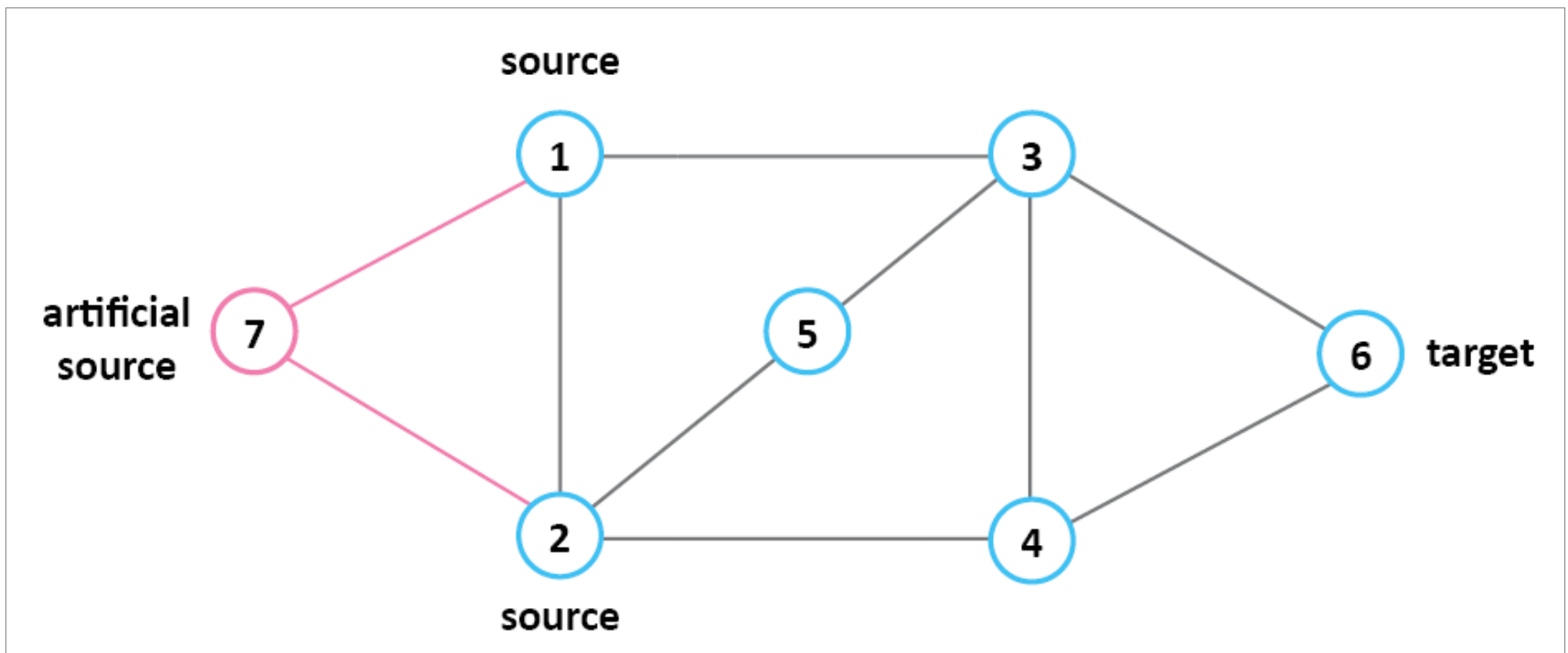
```
5 7
1 3 2
1 2 1
2 3 1
4 2 1
3 4 2
4 5 1
5 3 2
```

## Sample Output

```
3
```

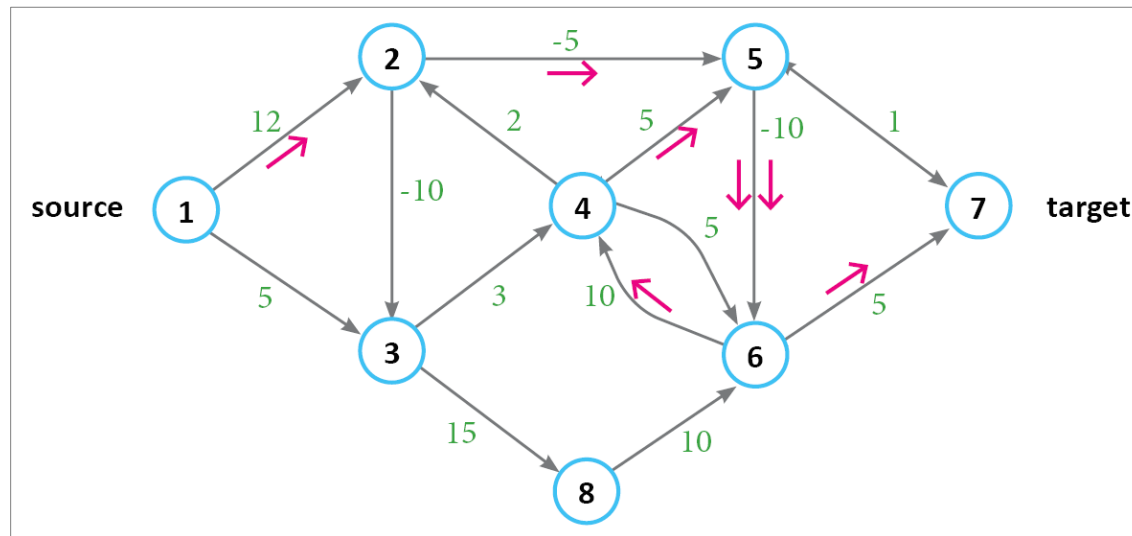


# Multisource BFS



# Minimum Cost Path with K Edges on a Weighted Graph

Given a weighted, directed graph  $G(V, E)$ , find the minimum cost path from a given source to a target node with exactly  $k$  edges on the path.



# BFS on a Complementary Graph

Calculate all shortest distances from the source node 1 to all other nodes on the complementary graph.

## Sample Input

```
6 2 1          //N, K, root
1 30 2 7 8 9
1 2
1 5
5 3
5 4
5 6
```



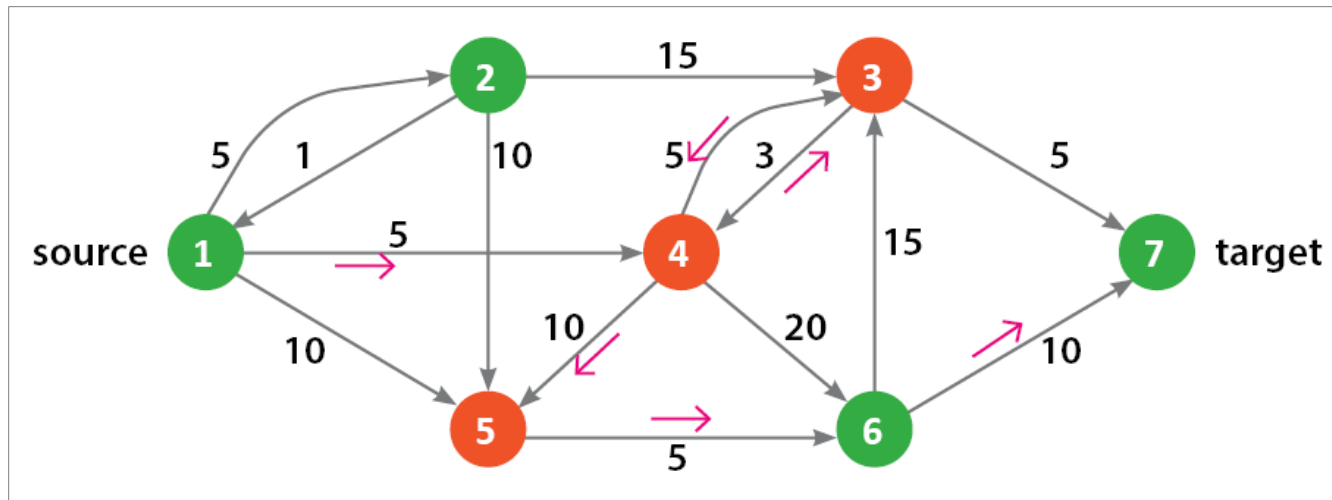
## Sample Output

9



# BFS with Bit Masking

Given a weighted, directed graph  $G(V, E)$ , and a set  $X$  of vertices. Find the Minimum Cost Path passing through all the vertices of the set  $X$ , from a given source vertex  $S$  to a target vertex  $T$ . The size of  $X$  is  $K$ . Source and target nodes are not member of  $X$ .





## Exercise 2: Minimum Cost Path with K Different Edges

Given a weighted, directed graph  $G(V, E)$ , find the minimum cost path from a given source to a target node with exactly  $k$  different edges on the path.

