

Merge & Count(A, B)

$j = 0$; Count = 0;

For ($i = 0$ to $|A|-1$)

while ($A[i] > B[j]$)
 $j = j + 1$ *and $j < |B|$*

Count += j

$C = \text{Merge}(A, B)$

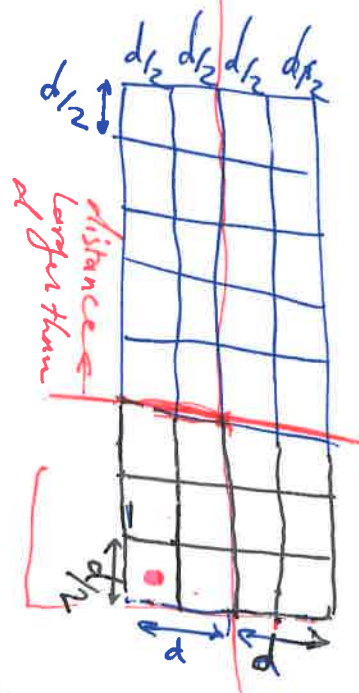
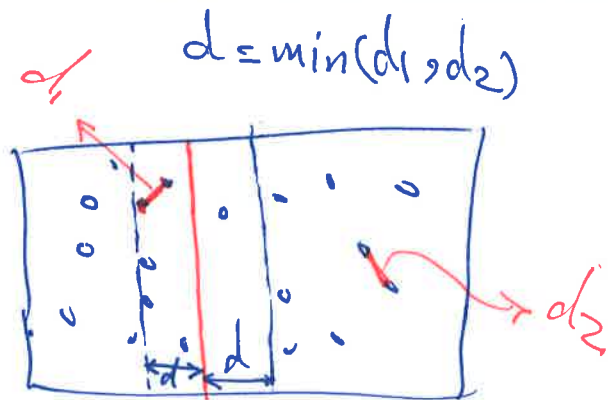
return (Count, C)

0	1	2	3	4	5	
3	7	10	14	18	19	A

0	1	2	3	4	5	
2	11	16	17	23	25	B

i	j	Count
	0	0
0	1	1
1	1	$1+1=2$
2	1	3
3	2	$3+2=5$
4	4	$5+4=9$
5	4	$9+4=13$

①



- There is at most 1 point in every cell
- Consider the point highlighted in the bottom-left cell.
 - Every point above the red horizontal line has distance larger than d from it
 - for every point in sorted list by y-axis, you need to compare it w/ 11 points

③

X = Sort Points by X-Coordinate
 Y = ~ ~ ~ Y-Coordinate

Closest-Pair (low-high)

$$m = \frac{l+h}{2}$$

$$X_L = X[l \dots m]$$

$$X_R = X[m+1 \dots h]$$

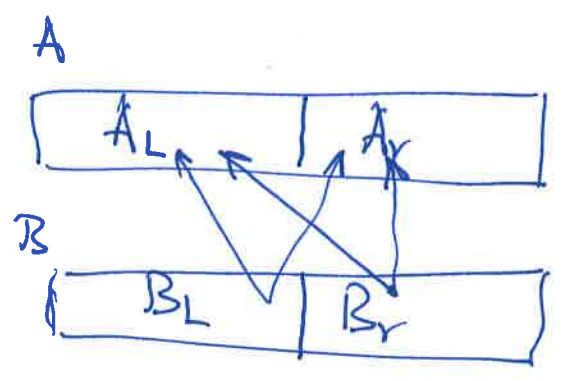
$$\delta_1 = \text{Closest-Pair}(X_L)$$

$$\delta_2 = \text{Closest-Pair}(X_R)$$

$$\delta = \min(\delta_1, \delta_2)$$

~~y~~ = empty list

for (i = 0 to |Y|-1)
 if (Y[i] belongs to the Stripe)
 add Y[i] to y

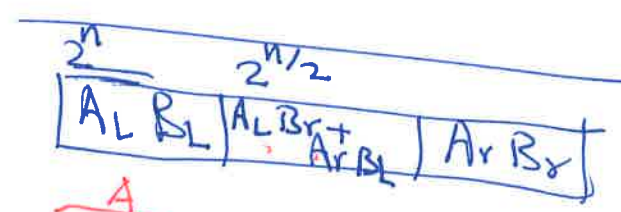
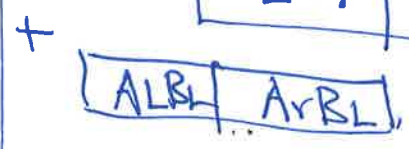
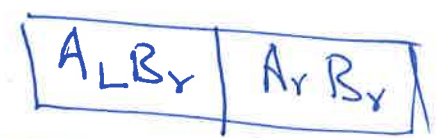


$A_R B_R$

$A_L B_R$

$A_R B_L$

$B_L B_R$



$$A_R B_R + 2^{n/2} (A_L B_R + A_R B_L) + 2^n A_L B_L$$

$$2^n B + A + 2^{n/2} ((A_L + A_R)(B_L + B_R) - A_L B_L - A_R B_R)$$

$$= 2^n B + A + 2^{n/2} (C - A - B)$$