



~~opt~~  
 $\text{opt}(n)$ : optimal solution

$$\text{SSE}(i, j) + \text{opt}(i-1) + C$$

$$\text{opt}(j) = \begin{cases} 0 & j=0 \\ \min_{0 \leq i < j} (\text{e}(i, j) + \text{opt}(i-1) + C) & j > 0 \end{cases}$$

$\text{opt}(n)$ :

for  $i = 1$  to  $n-1$   
 for  $j = i+1$  to  $n$   
 $\text{e}(i, j) = \text{SSE}_{\text{opt}}(i, j)$   
 $?O(n)$

$$M[0] = 0$$

for  $j = 1$  to  $n$   
 $\text{min} = \infty$

for  $i = 1$  to  $j$

$$\text{tmp} = \text{e}[i, j] + M[i-1] + C$$

if  $(\text{tmp} < \text{min})$

$$\text{min} = \text{tmp}$$

$$M[j] = \text{min}$$

return  $M[n]$

$$O(n^3)$$

$$X = \sum x_i$$

$$Y = \sum y_i$$

$$\overline{XY} = \sum x_i y_i$$

$$X_2 = \sum x_i^2$$

$$Y_2 = \sum y_i^2$$

$$X = X + x_j$$

$$Y = Y + y_j$$

...

$$b = \frac{Y - aX}{n}$$

$$a = \frac{n \overline{XY} - X \cdot Y}{n X_2 - X^2}$$

$$\sum (y_i - ax_i - b)(y_i - ax_i - b)$$

$$= \sum y_i^2 + a^2 \sum x_i^2 + nb^2$$

$$- 2a \sum x_i y_i + 2ab \sum x_i - b \sum y_i$$

$$= Y_2 + a^2 X_2 + nb^2 - 2a \overline{XY} + 2abX - bY$$