1) we have the ODE

we select to liveavite about the steady-state where consider it as an import. Under these conditions (Utc.) V=30, 8=0. We also assume that of is just an external disturbance and we linearite about \$=0 but we do not

standard himodel of the live or ited system becomes: 4= v-vo, u= u-vo, x=4. Then He

$$x = \frac{2GV_0}{m} \times + \frac{G_0}{m}u$$
 | $\frac{1}{m}u$ | $\frac{1}{m}$

In MARLAS: H= ss (-0.02,1,1,0), +f(H) + Sto.02

2.) We have $0 = bT - \epsilon \theta - asin \theta$, where $b = \frac{1}{mL^2}$, $a = \frac{9}{L}$, $|| \frac{1}{2} || \frac{1}{2$ In Maricas: H==>(A,B,C,D), +P(+)-> 7.27 We define x = (8)-(0.), y=(0-0.), u=T-To. We liveavite about $\theta=0$, $\theta=\pi$ and $T_0=0$. e = e 2 52+0.158-19-6

We have (m+H) = F-C2 -mL 8 cos0+mL 8 sin8 where a is the eart position rabble to the content moon. The equations are implicit in $\frac{1}{2}$, in the form

(a(θ) x = f(x, u)The Linearitation approximations are: (savier to substitute) where HOT are second order -or hister and u is the linearitation luput F-0. () - (o) A reasonable output is the court position, whichis given by Thuis-Bris HAM +& = B OS Bris HAM +E COS 0 = - 1+thor, 0 = 0+thor, 8100 = -(0-11) +thor

This matrix is always invertible since det [m+H -mL] We substitute the numerical values in matches = (m+H) ml2 - m22 = ml2 (m+H-1) = mH12 > 0. Q(0) x = 0(6)= T 8900 0 X5'0- 0 1 - 1 o mlasso o ml2 0 0 主土の 0 0 o mg/ 5 0 -0 xxxxxx o] x + [o]u mLcosA 0 0 100 better 0 0 0 X+ 115 10-m2 0 m12 100 O MAN O IM 0 0

H= ss(A,B,C,D), +P(H)-C=[1,0,0.17,0] 7 D=0 83 + a. 12652 - 0.01465 28+0.29

Produce algebraic equations that do not add states). there, it is easier to perform Leoparchysis instead of modal because there are only two loops. (The extra nodes would

with the handout notation:

-V_s + R₁I₁ + V_c + R₈I₁ = 0, V_c - L₄I₂ V_s - C₁ V_c - V_c + R₂I₂ + V_L = 0, V_c - L₄I₄ V_s - C₁ - V_{ot}.

-V_c + R₂I₂ + V_L = 0, V_c - L₄I₄ V_s - C₁ - I₂ and the rapacitor where, the inductor current is
$$I_L = I_2$$
 and the rapacitor wolldage is $V_c = \frac{1}{c} \int I_c = \frac{1}{c} \int I_1 - I_2 \rightarrow I_1 = \frac{c}{a} V_c + I_2$.

We define the circuit states $X = \begin{pmatrix} V_c \\ I_L \end{pmatrix}$, for which we are

The output
$$y = V_{out} = R_3 I_1 = R_3 \left[c \frac{dx_1}{dx_1} + x_2 \right]$$

 $= R_3 C \left[1, 0 \right] \left(Ax + Bu \right) + R_3 \left[0 \right] \times$
 $= \left(R_3 C \left(1, 0 \right) A + R_3 \left(0, 1 \right) \right) \times + \frac{R_3}{R_1 R_3} u$

Substituting,
$$\dot{x} = \begin{pmatrix} -9.091 & -164 \\ 14.2 & -1.42 \end{pmatrix} \times + \begin{pmatrix} 9.091 \\ 0 \end{pmatrix} u$$

$$\dot{y} = \begin{pmatrix} -0.9091 & 0 \end{pmatrix} \times + \begin{pmatrix} 0.9091 \end{pmatrix} u$$

whose transfer fountion is $4f(ss(a,b,c,d)) = \frac{0.909s^2 + 1.29 + 1.2965}{s^2 + 10.55 + 1.4265}$

For a finish difference discustionion, we let the xmin so the disaste-time state space representation becomes

XM = (I+TA) XX + TB TK gu = CXL+DWL Hd = 95 (I+T+A, T+B, C, D, T)

and T (here 16-5). If T is large, unstable responses try in marriage with, sail = 16-4, 16-5 and observe that

Compare responses by using "bode (H, Ha)" "shop (H, Hd)"