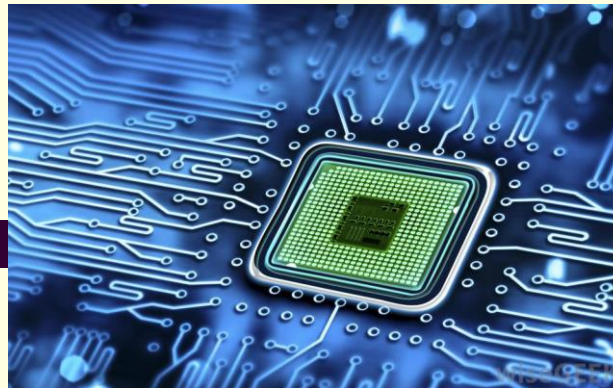


Information and Communication Technology

Class XI-XII



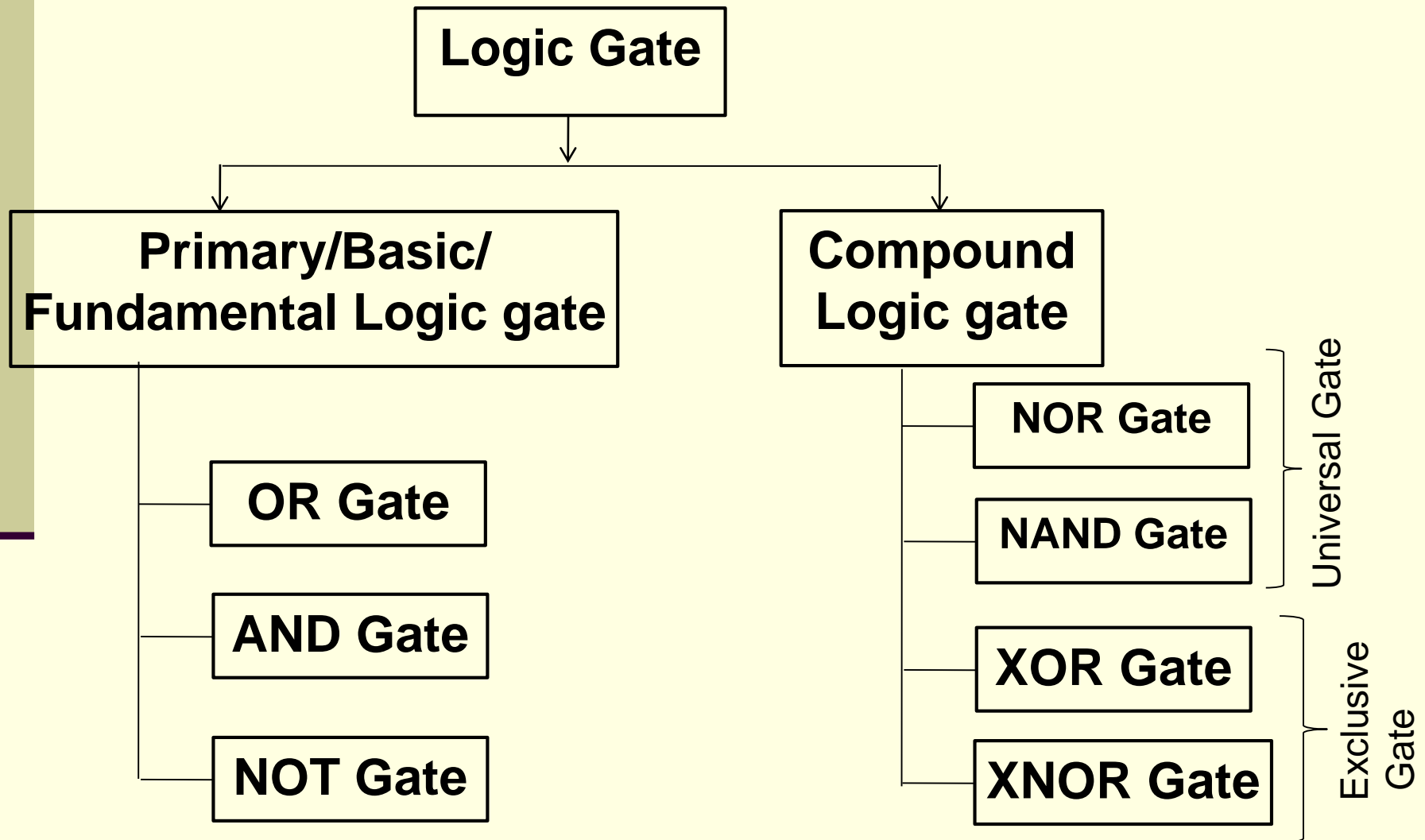
Chapter-3

Digital device

Logic Gate

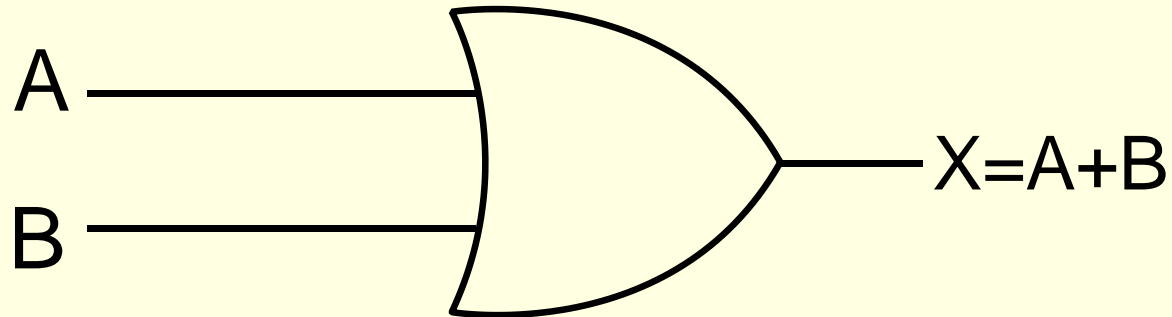
- Logic gate is used to implement Boolean algebra practically.
- Takes one or more inputs
- Produce only one output

Types of logic gate:



OR gate (Basic logic gate)

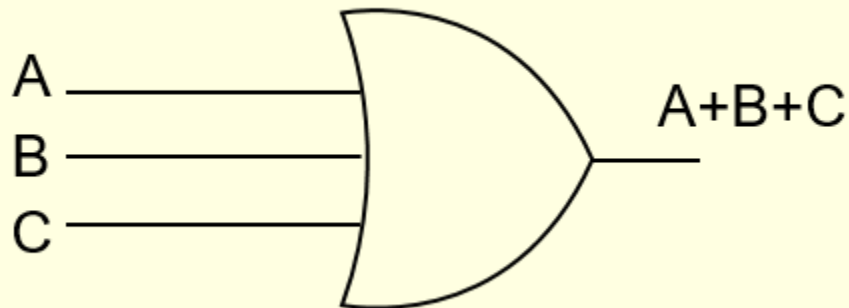
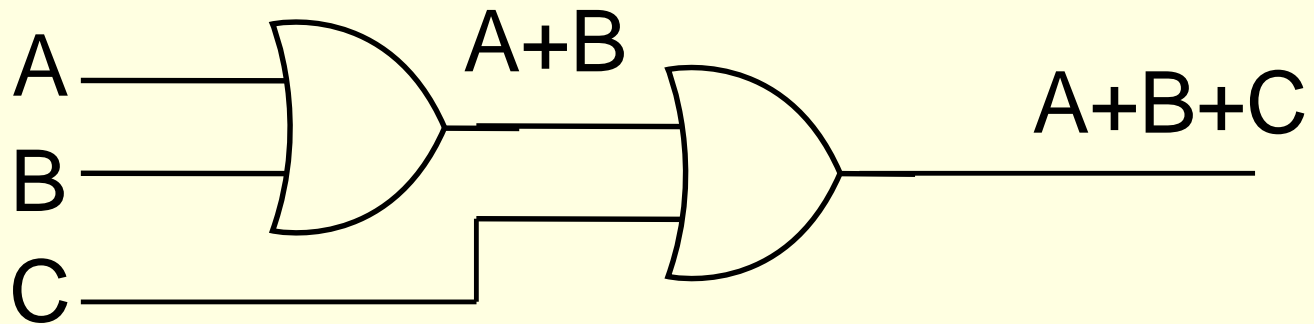
- performs logical addition of Boolean algebra
- A OR B
- $=A+B$

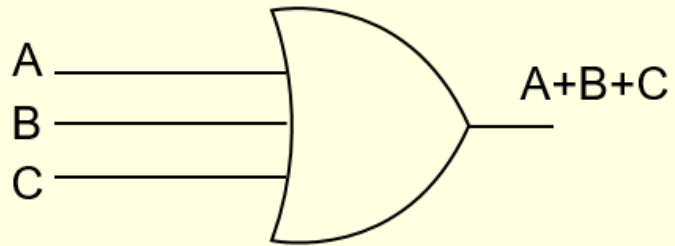


Truth table of OR gate

Input		Output
A	B	$X=A+B$
0	0	0
0	1	1
1	0	1
1	1	1

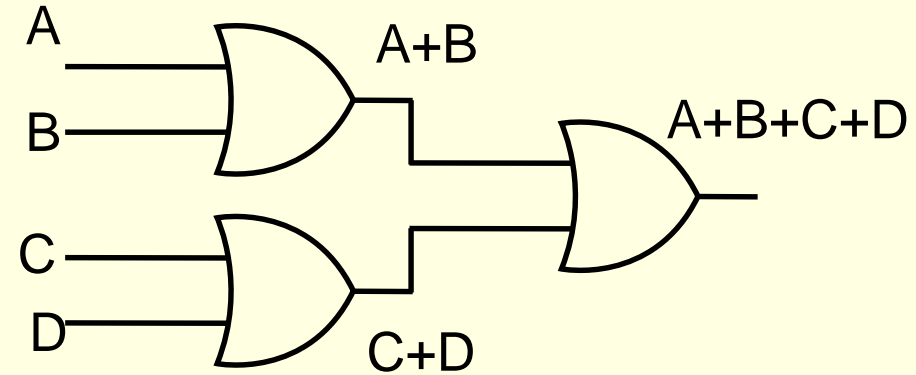
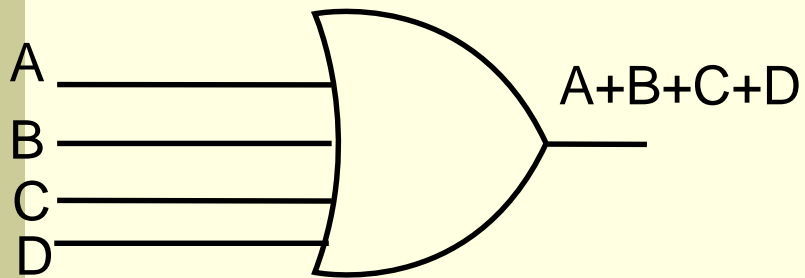
Truth behind 3 input OR gate





A	B	C	$Y=A+B+C$
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

4 input OR gate

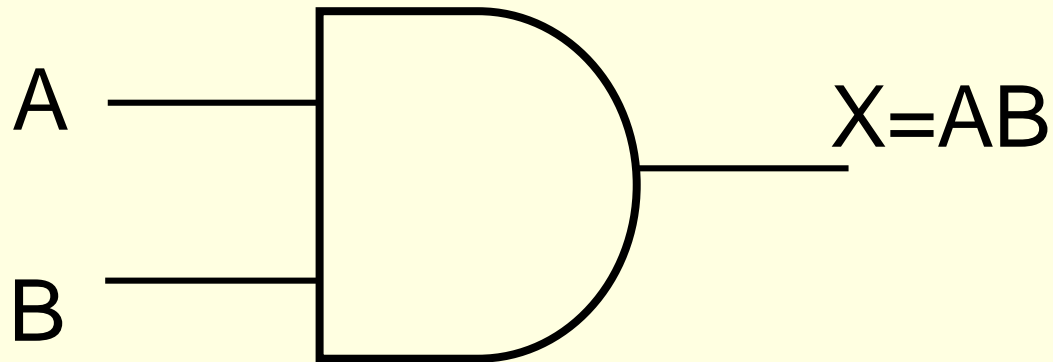


AND gate (Basic Logic gates)

AND gate: performs logical AND (multiplication) of Boolean algebra

A AND B

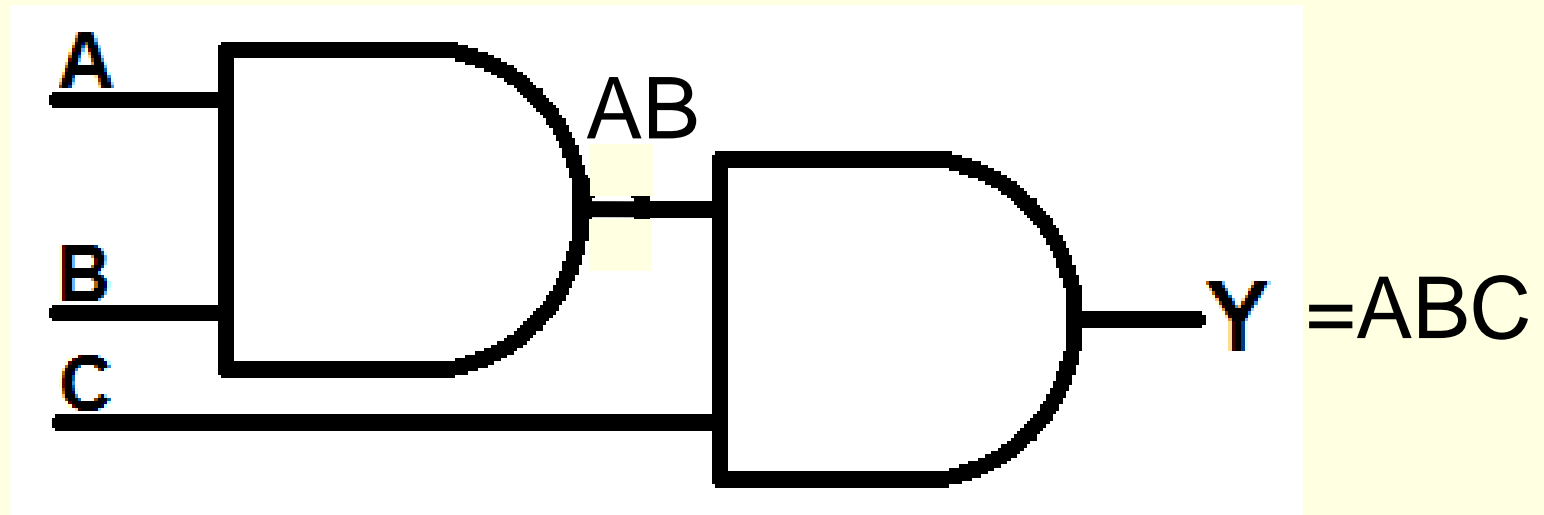
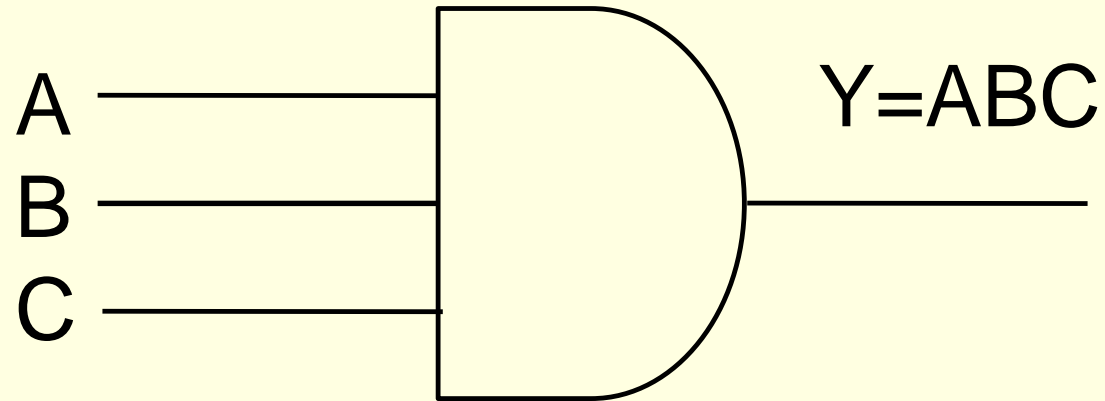
$=A.B$

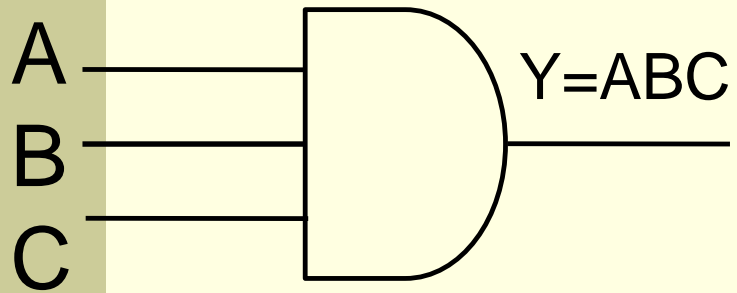


Truth table of AND gate

Input		Output
A	B	$X=AB$
0	0	0
0	1	0
1	0	0
1	1	1

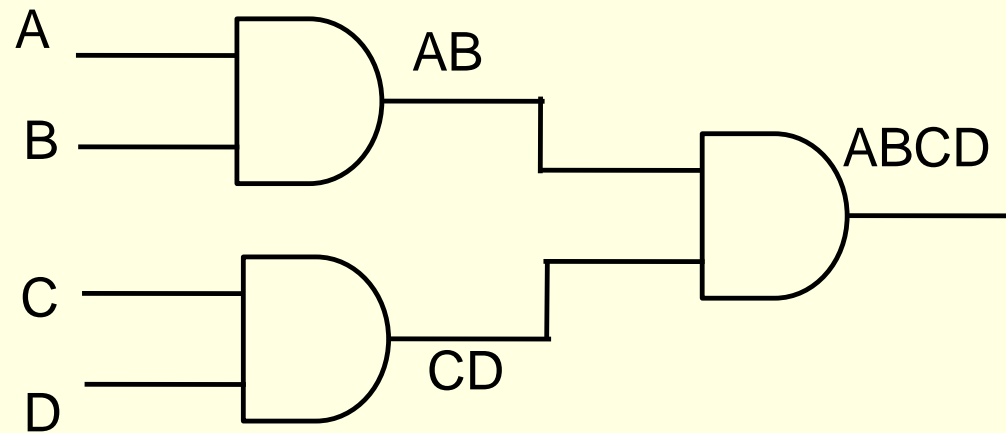
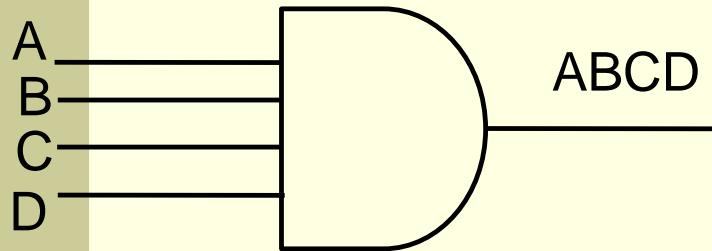
3 input AND gate





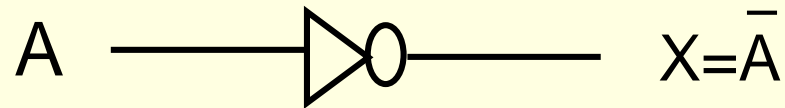
A	B	C	$Y=ABC$
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

4 input AND gate



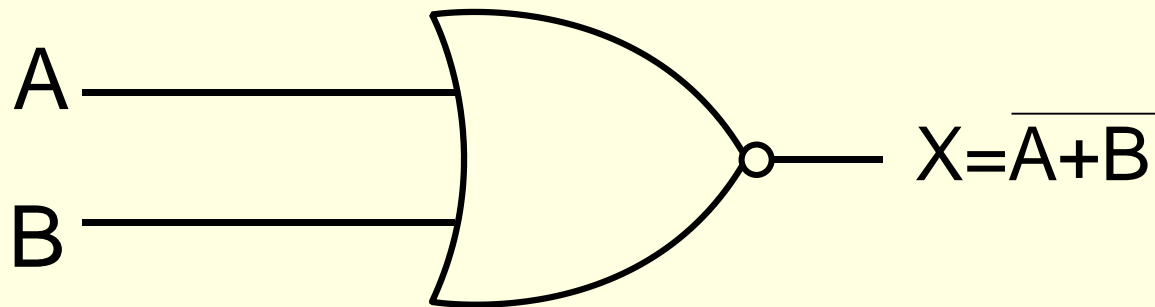
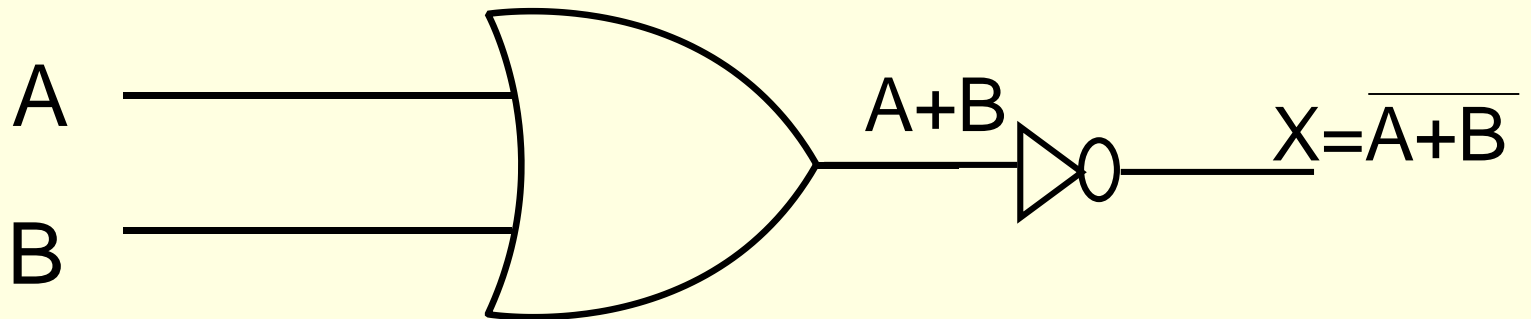
NOT gate

- performs Boolean complement

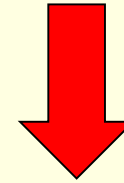


Input	Output
A	$X = \bar{A}$
0	1
1	0

NOR gate



Truth table of NOR gate



Input			Output
A	B	$A+B$	$X = \overline{A+B}$
0	0	0	1
0	1	1	0
1	0	1	0
1	1	1	0

Truth table of NOR gate

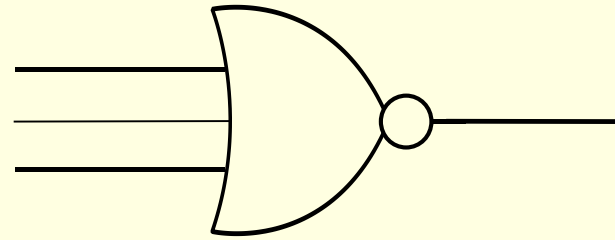
Input		Output
A	B	$X = \overline{A+B}$
0	0	1
0	1	0
1	0	0
1	1	0

CQ22

Input		Output
A	B	F
0	0	0
0	1	1
1	0	1
1	1	1

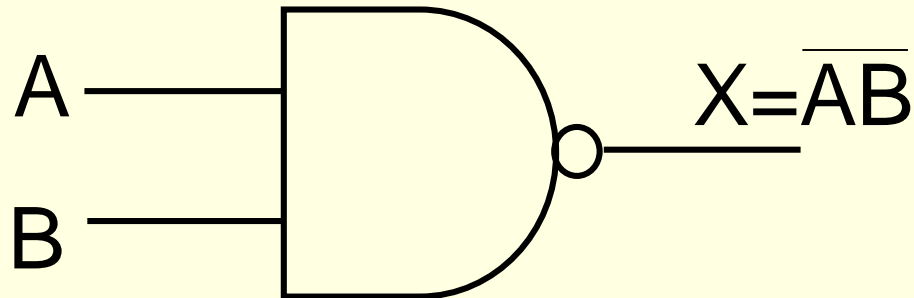
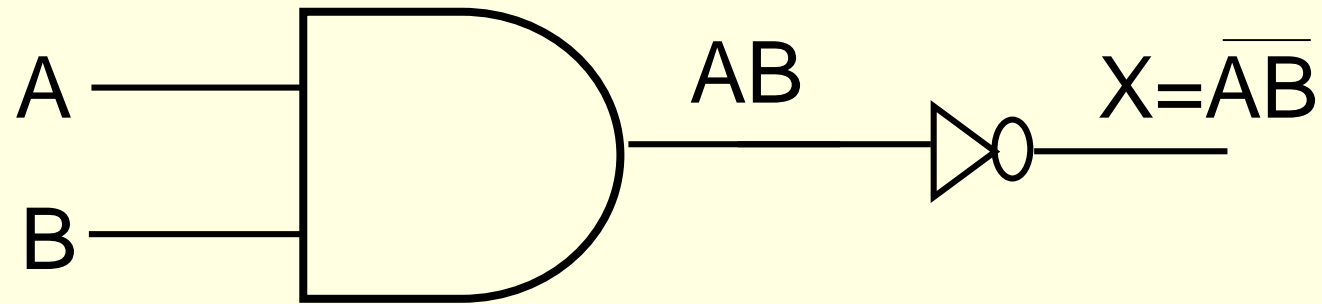
Input	Output
A	X
0	1
1	0

3 input NOR

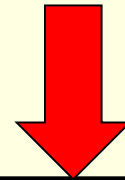


A	B	C	$A+B+C$	$\overline{A+B+C}$
0	0	0	0	1
0	0	1	1	0
0	1	0	1	0
0	1	1	1	0
1	0	0	1	0
1	0	1	1	0
1	1	0	1	0
1	1	1	1	0

NAND gate



Truth table of NAND gate

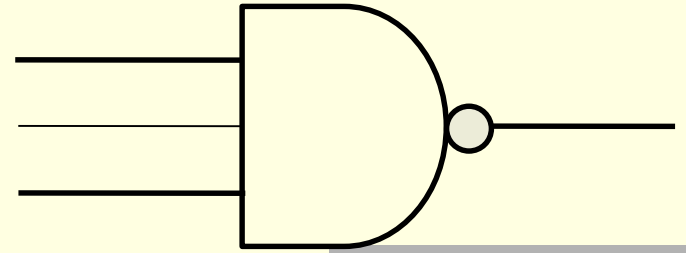


Input			Output
A	B	AB	$X = \overline{AB}$
0	0	0	1
0	1	0	1
1	0	0	1
1	1	1	0

Truth table of NAND gate

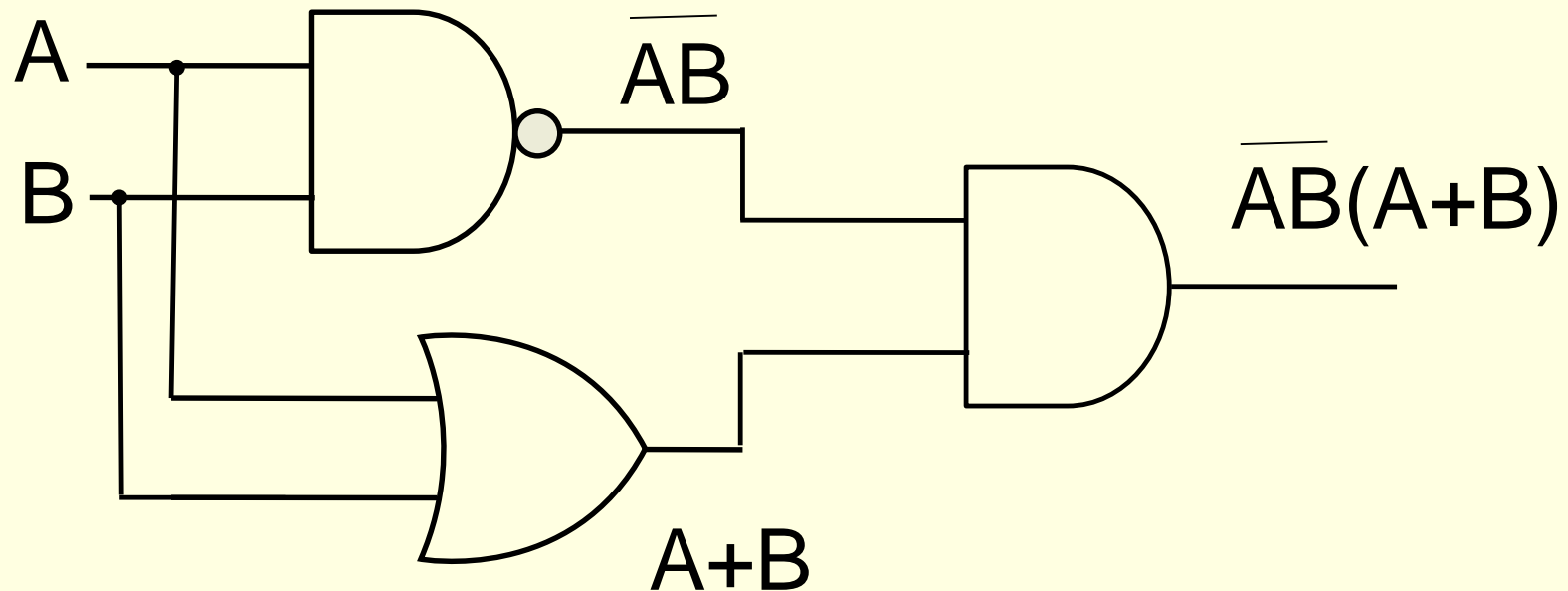
Input		Output
A	B	$X = \overline{AB}$
0	0	1
0	1	1
1	0	1
1	1	0

3 input NAND

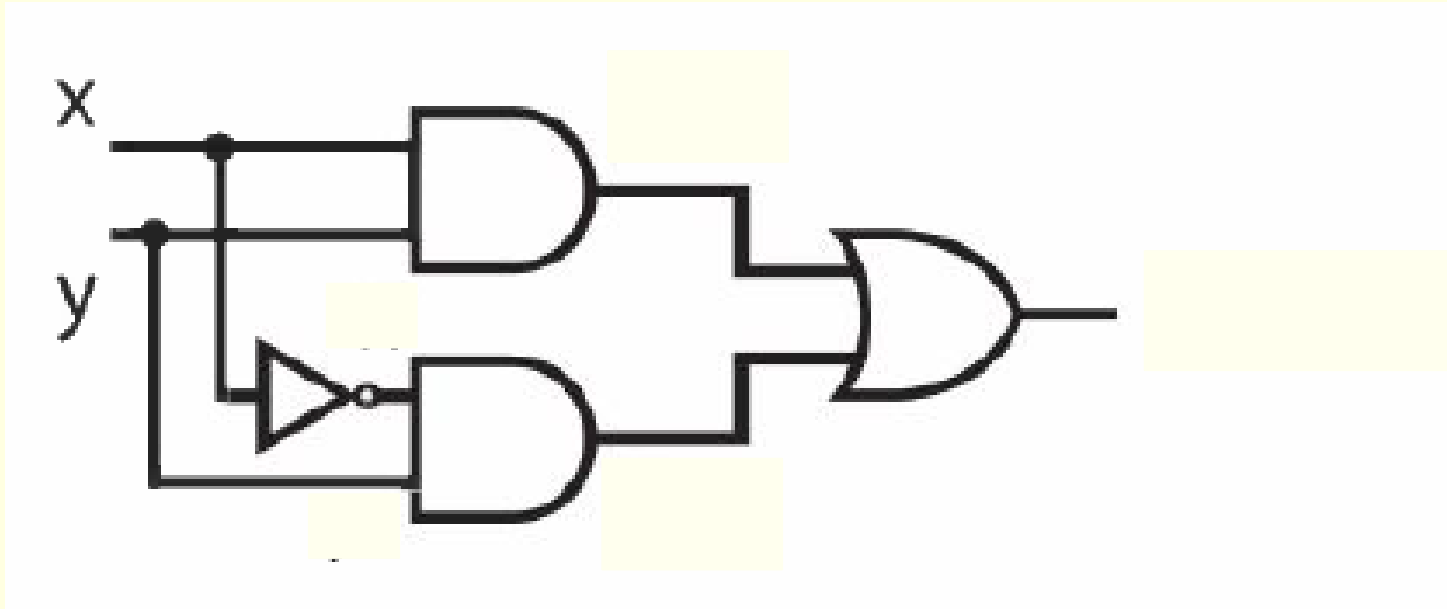


A	B	C	ABC	\overline{ABC}
0	0	0	0	1
0	0	1	0	1
0	1	0	0	1
0	1	1	0	1
1	0	0	0	1
1	0	1	0	1
1	1	0	0	1
1	1	1	1	0

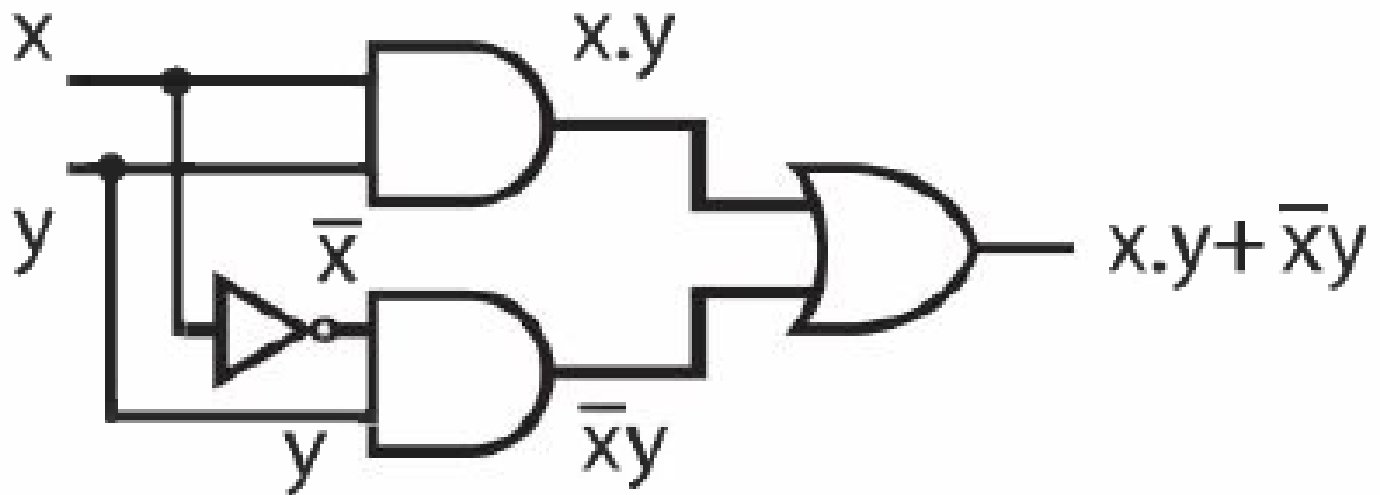
Determine output and simplify



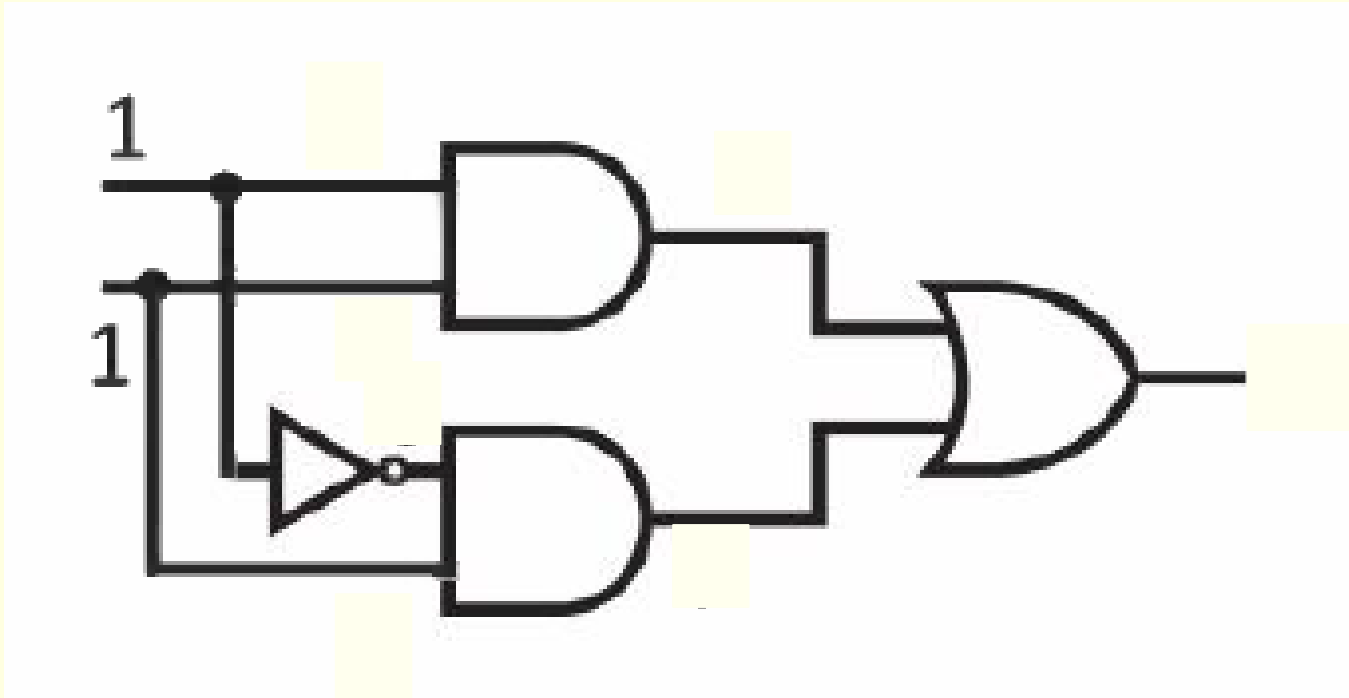
What will be the output if inputs are x and y

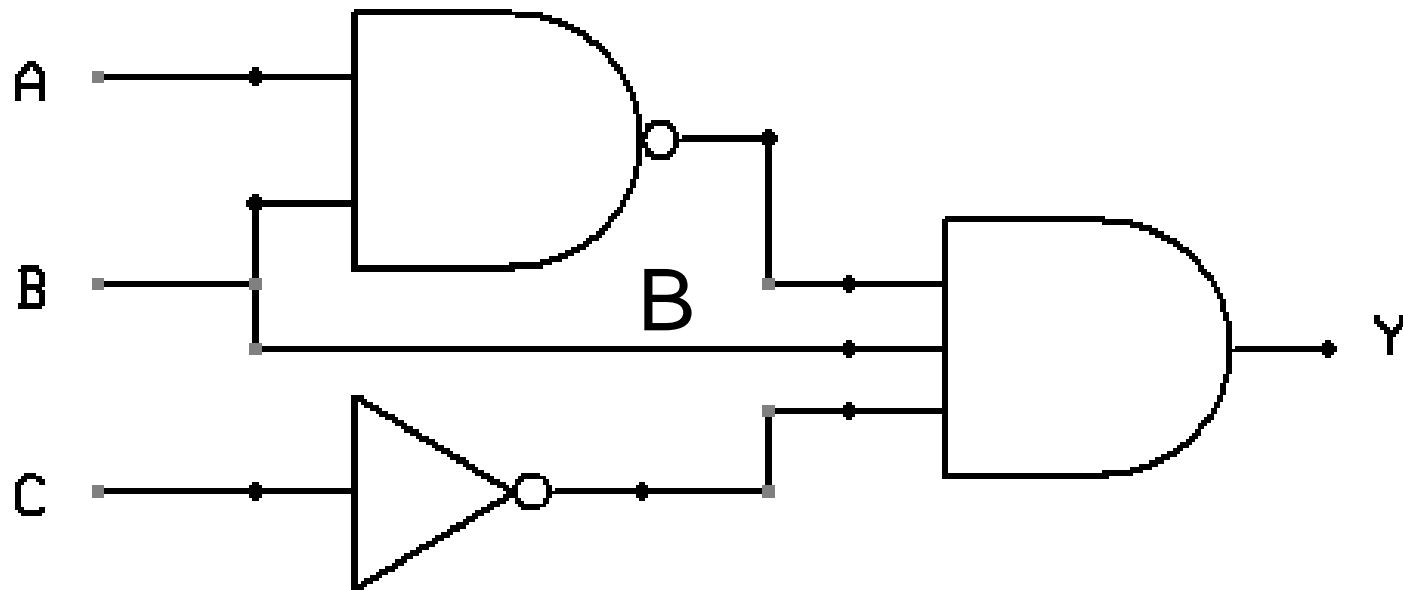


What will be the output if inputs are x and y



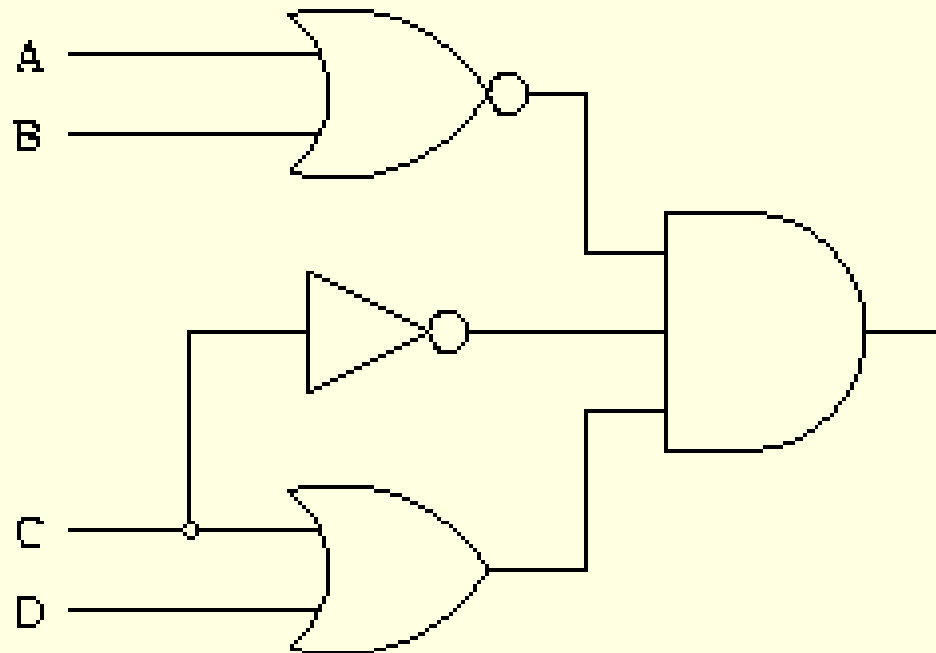
What will be the output if both inputs are 1



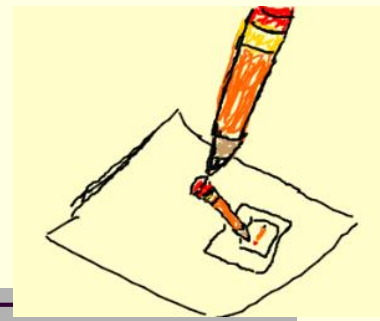


OUTPUT? SIMPLIFY

Output ?



Draw Circuit



$$F = \overline{\overline{A} + B}$$

$$Y = \overline{\overline{A}B}$$

$$F = \overline{A}B + A\overline{B}$$

$$F = \overline{A}.\overline{B} + AB$$

$$X = A\overline{B}C + B\overline{C}$$

$$Y = \overline{A}B + \overline{B}.\overline{C}$$

$$Y = \overline{\overline{A}B + \overline{C}}$$

$$F = \overline{\overline{A}CB + \overline{B}}$$

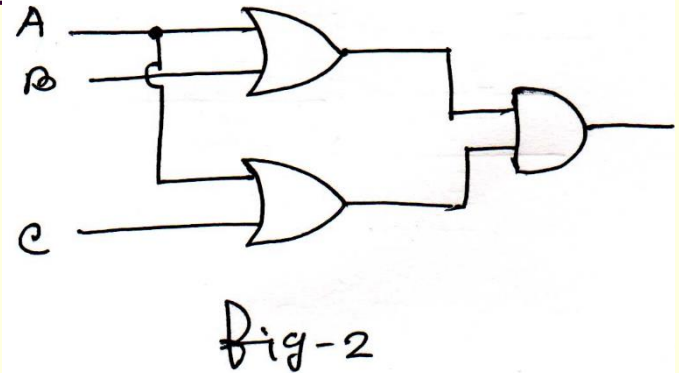
$$F = \overline{(\overline{X}Y)(X\overline{Y})}$$

$$X = AB + BC + AC$$

M-19

$$\bar{A}B + AC + BC$$

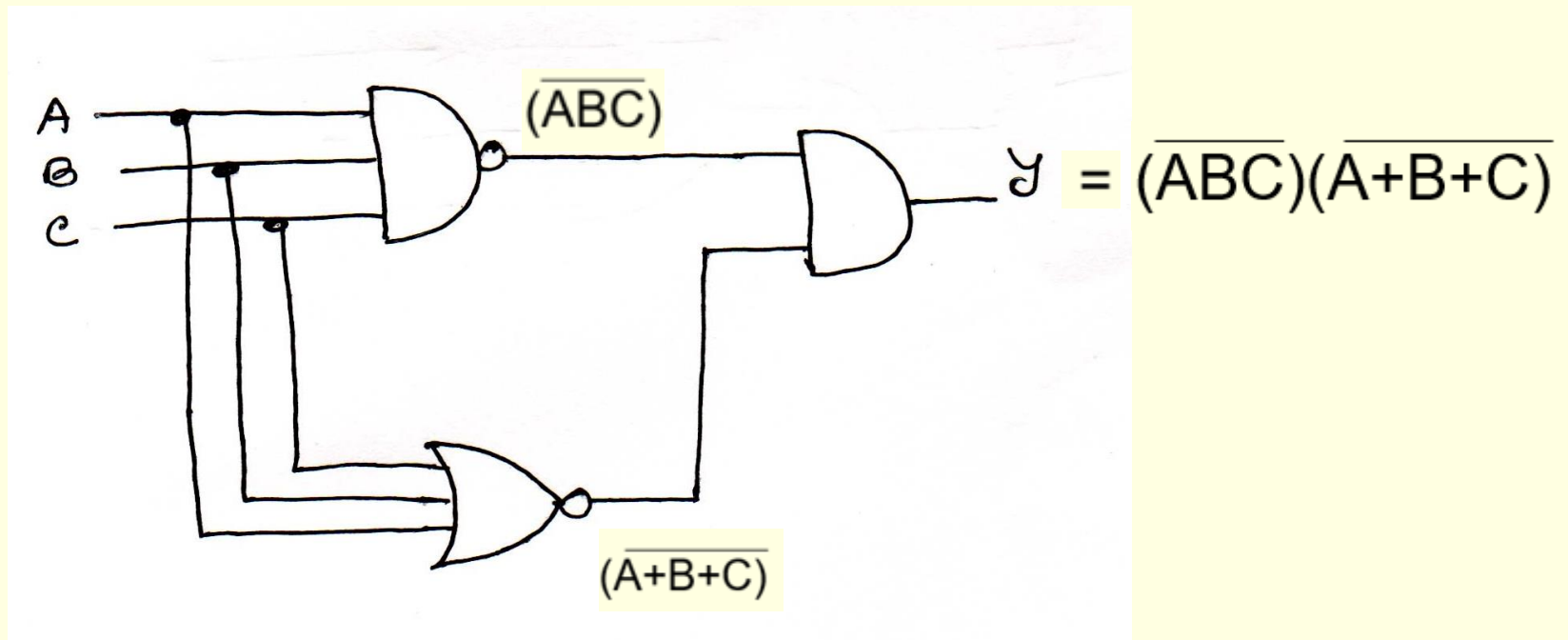
Fig-1



- C) Draw circuit for the fig-1
- D) is there any similarity between fig-1 and fig-2

S-19

- Simplify output Y



Stem: Use only **Basic** gates to implement the following circuit also compare after simplification

$$F = \overline{\overline{PQ}} + \overline{PR}$$

$$Y = \overline{A}(\overline{B + C}) + \overline{A}.\overline{B}$$

C) Show that simplification of Y leads to draw easy circuit

D) Truth table of Y. When Y=1 ?

$$F = \overline{(A + B + \overline{C})} + B\overline{\overline{C}}$$

- C) Simplify the above expression
- D) if result is 1, what are input values for A,B and C?

d) How it's possible to implement figure:1 by **minimum** number of **primary** gate. Show the circuit diagram.

$$\overline{AB} + \overline{C} + \overline{BC}$$

Figure : 1

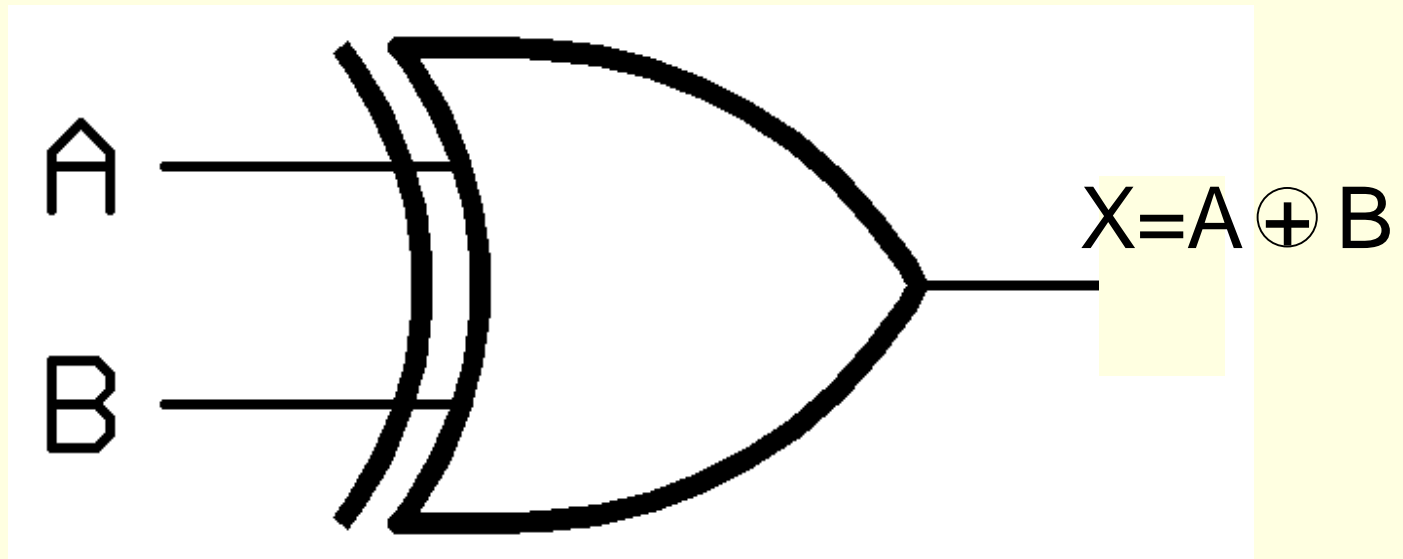
Stem: When $F=1$?

$$F = \overline{\overline{A} + B + B + \overline{C}}$$

$\overline{\overline{X}}(Y+\overline{Z})$ draw using only basic gate

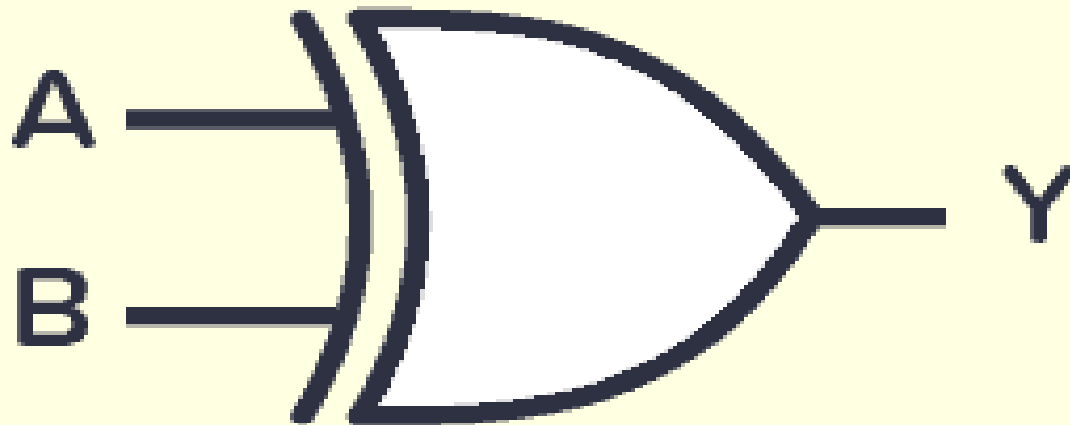
X-OR gate

- (Exclusive OR/Ex-OR)



X-OR gate

- (Exclusive OR/Ex-OR)



Truth table of X-OR gate

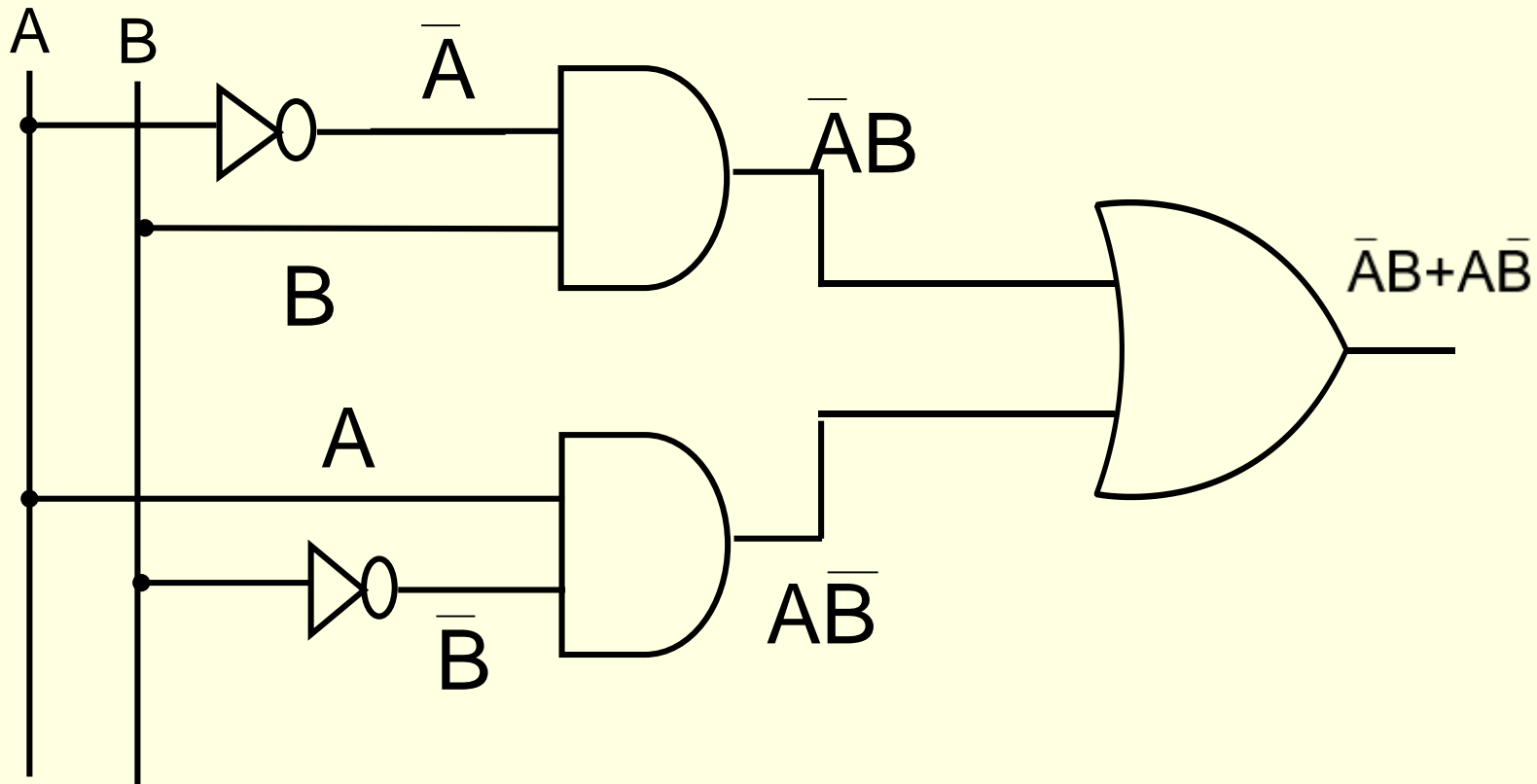
Produce 1 only if both inputs are different to each other

Input		Output
A	B	$X = A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

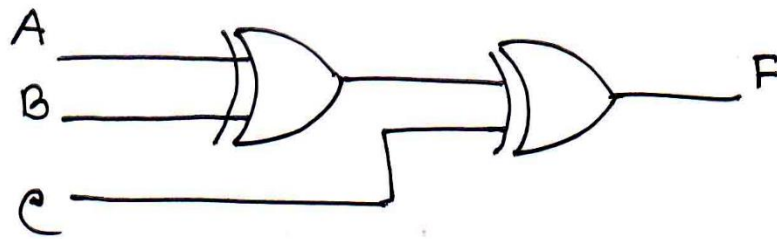
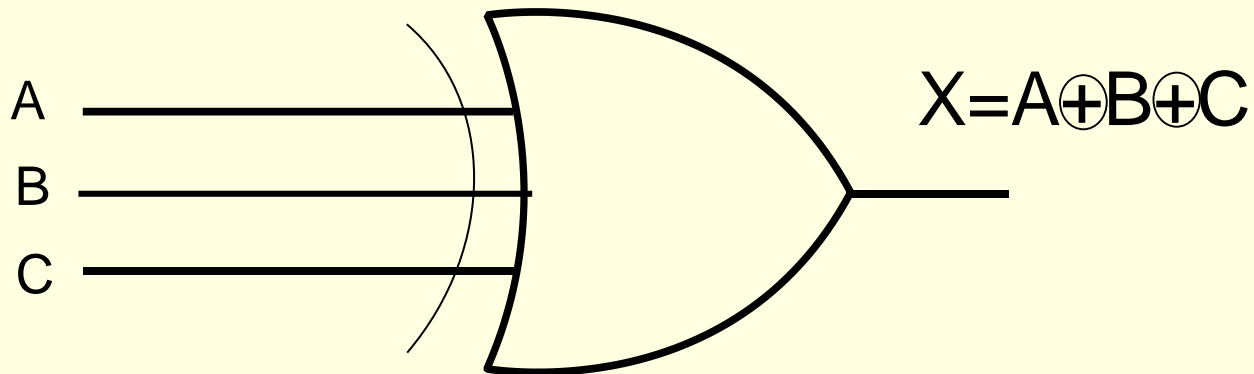
Produce 1 only if there are odd numbers of 1 is present in input. Otherwise produce always 0.

Implement X-OR by basic gate

■ $A \oplus B = \bar{A}B + A\bar{B}$



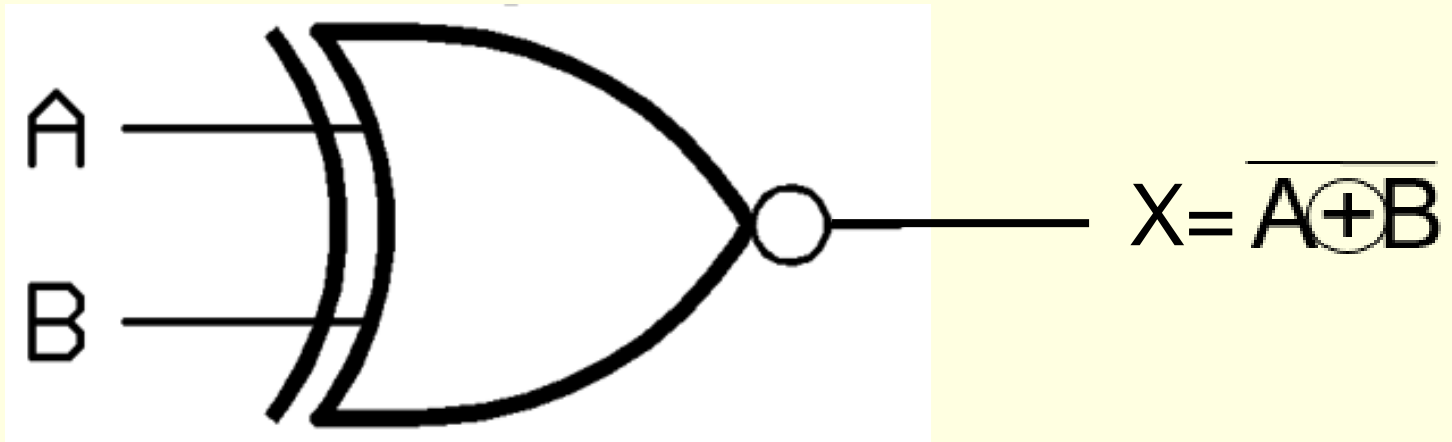
3 input X-OR gate

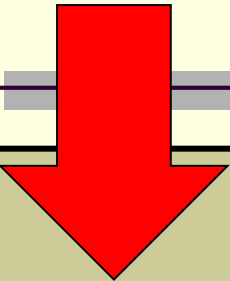


Truth table of a 3 input X-OR gate

Input			Output
A	B	C	X
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

X-NOR



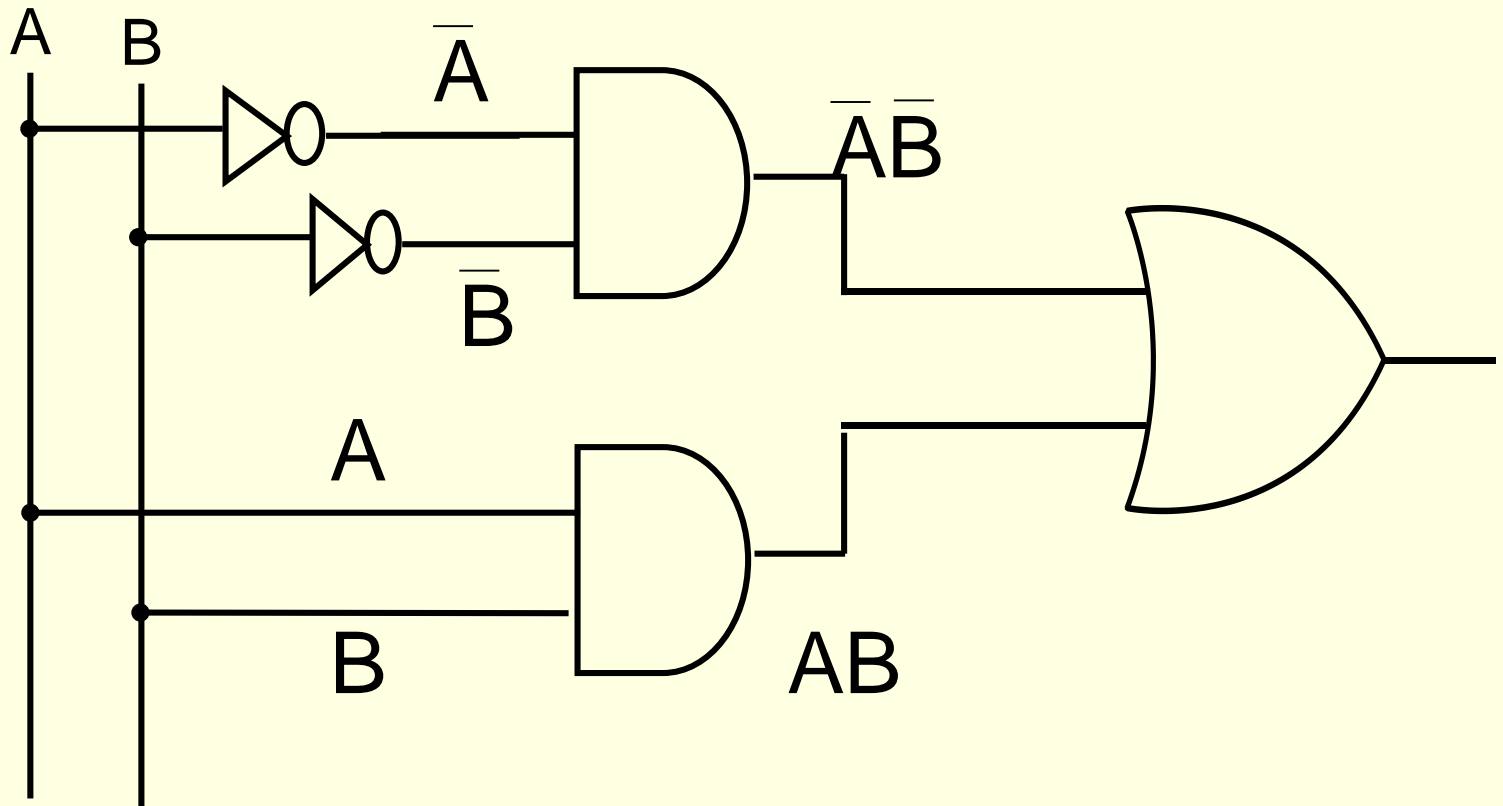


Input			
A	B	$A \oplus B$	$\overline{A \oplus B}$
0	0	0	1
0	1	1	0
1	0	1	0
1	1	0	1

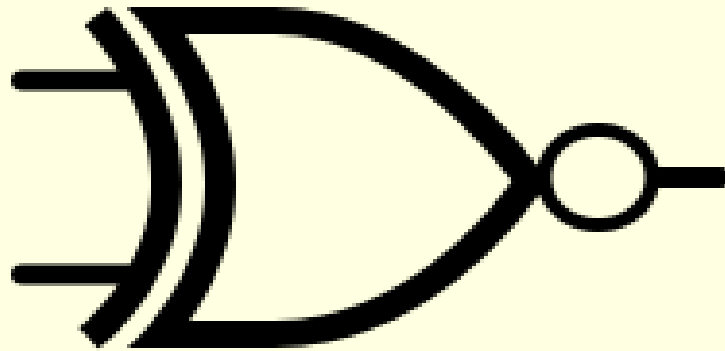
Input		Output
A	B	F
0	0	1
0	1	0
1	0	0
1	1	1

Implement X-NOR by basic gate

■ $\overline{A \oplus B} = \overline{A} \overline{B} + AB$



Implement the figure by primary gate



Stem: Draw circuit for the TT below

Input		Output	
A	B	X	Y
0	0	1	0
0	1	0	1
1	0	0	1
1	1	0	0

Stem: Draw circuit for the TT below

Input		Output	
A	B	X	Y
0	0	1	1
0	1	0	1
1	0	0	1
1	1	1	0

Define X and simplify
draw circuit for Y by Basic gate

A	B	C	X	Y
0	0	0	1	1
0	0	1	0	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	1
1	0	1	1	0
1	1	0	0	1
1	1	1	1	0

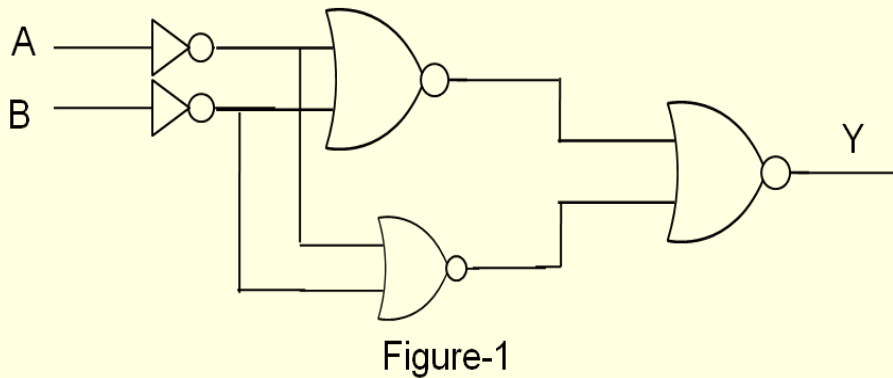
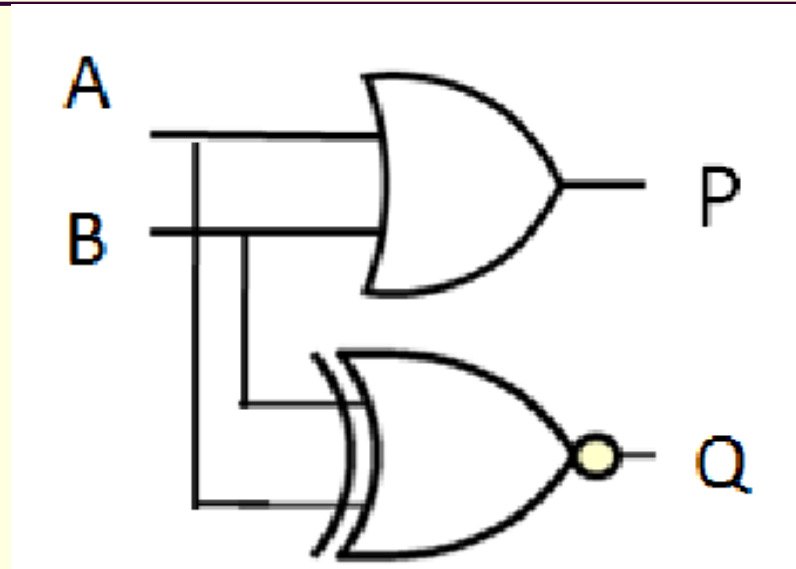


Fig-2		
P	Q	X
0	0	0
0	1	0
1	0	0
1	1	1

- C) in fig-1 , what is simplified value of Y=?
- d) Compare the gate of fig-2 with the output of fig-1



C) Draw a Truth Table for P and Q

D) proof $PQ=AB$ by Boolean simplification

Step: Output of fig2 replaces the input A of Fig 1. then analyze the simplified logic circuit.

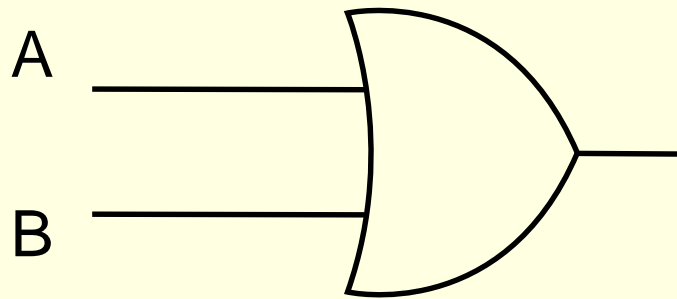


Fig1

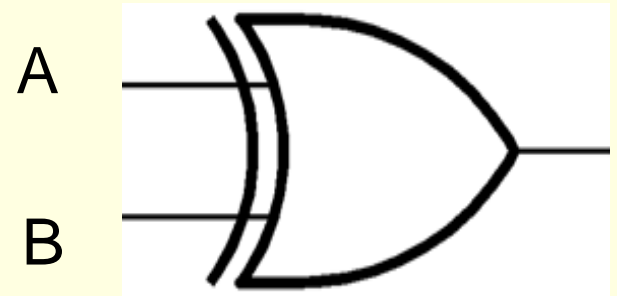
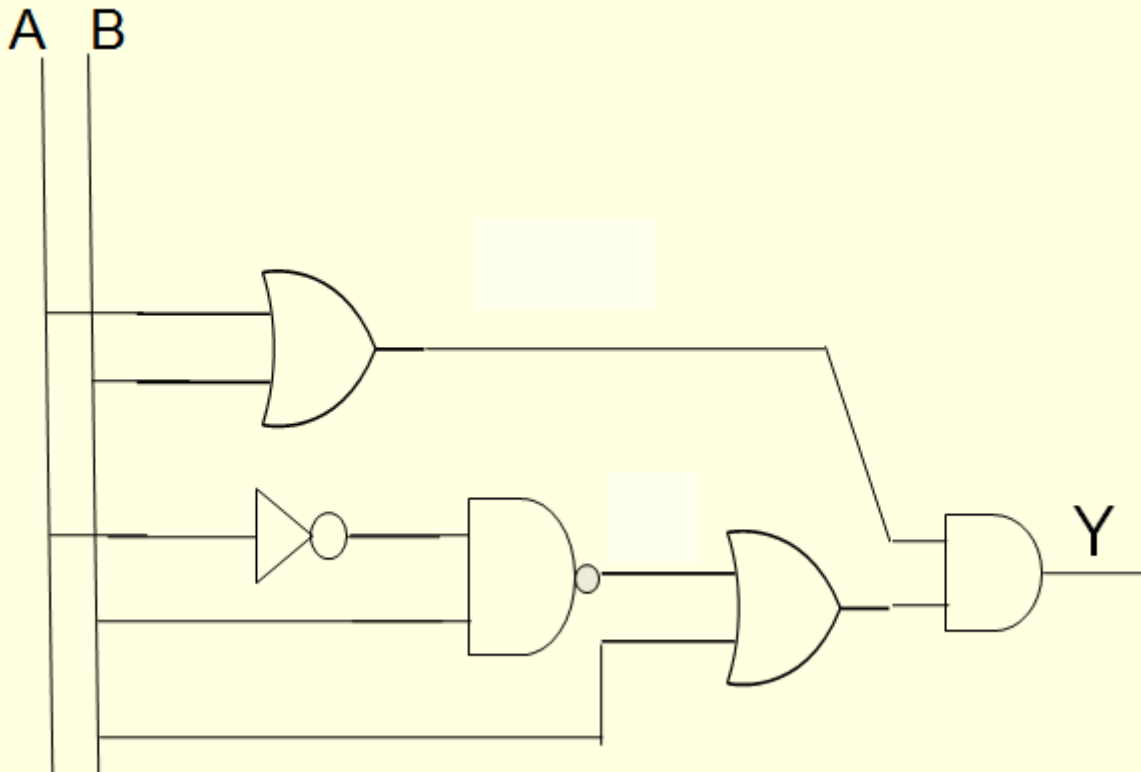


Fig2

C) Simplify Y

d) Compare R and Y



P	Q	R
0	0	1
0	1	0
1	0	0
1	1	0

Stem $F = A + \bar{A} B$

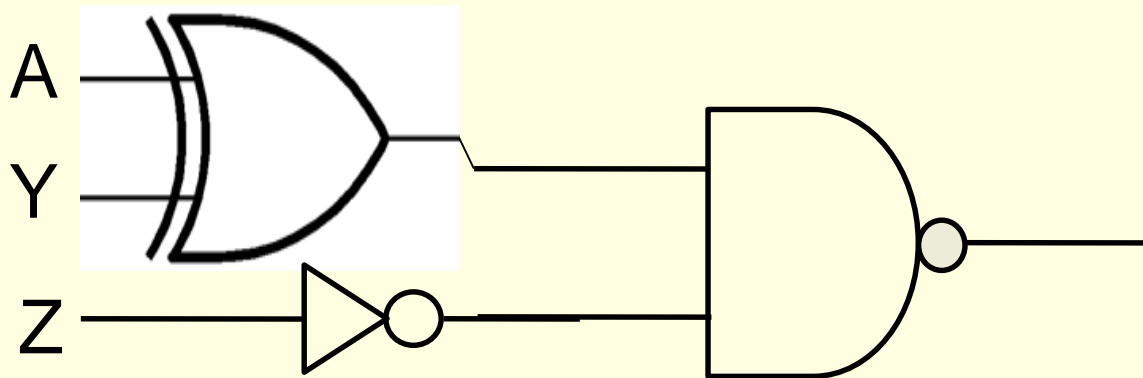
C) Draw TT for this expression

D) TT belongs to which basic gate

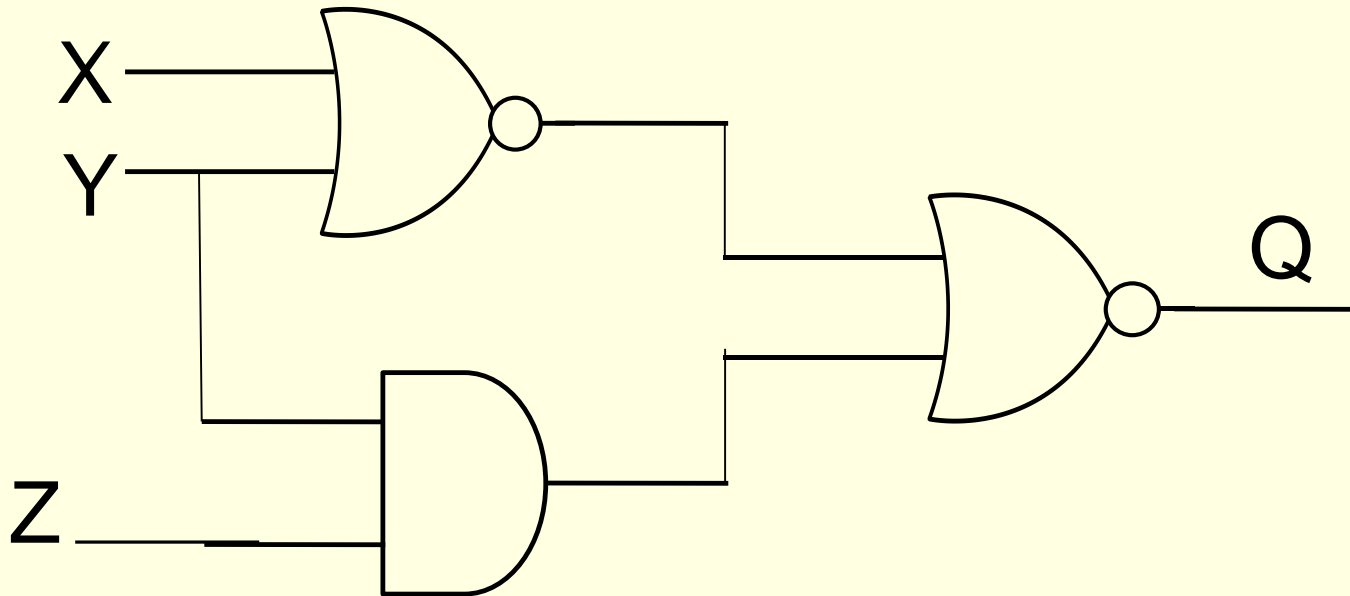
$$Y = \overline{P + \overline{Q}(\overline{P} + Q)} + PQ + \overline{Q}R$$

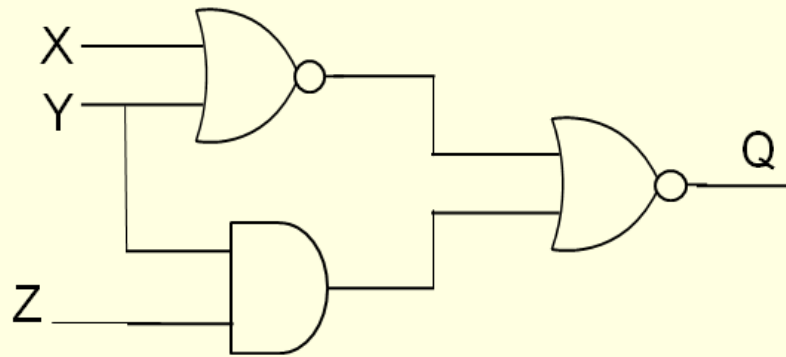
- (c) Simplify Y and draw the logic circuit of the simplified value of Y
- (d) For which values of P, Q and R, the value of Y will be 1? Analyze.

Simply the result and draw circuit by Primary gates only



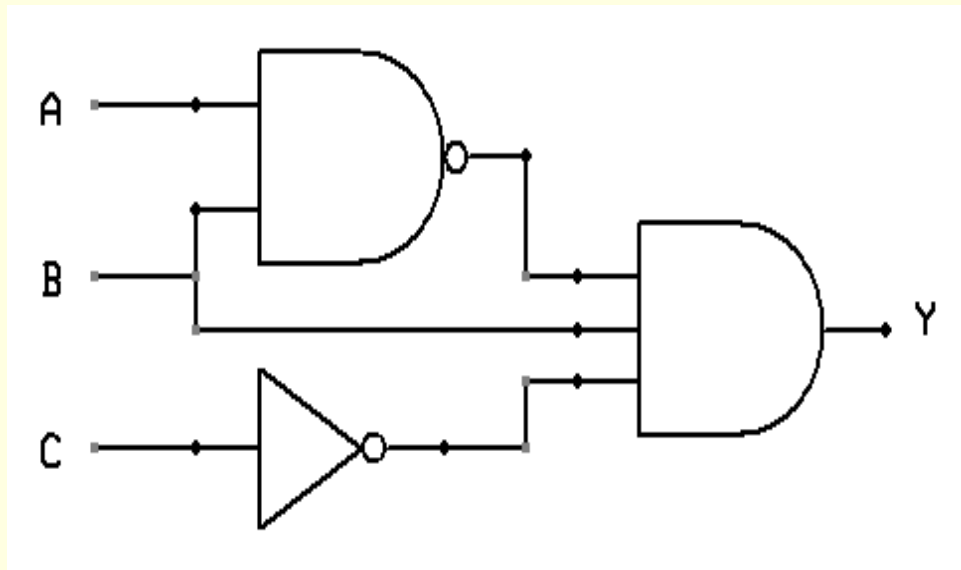
- c) Draw Truth Table for Q,
d) is it possible to implement Q by a single gate?
-





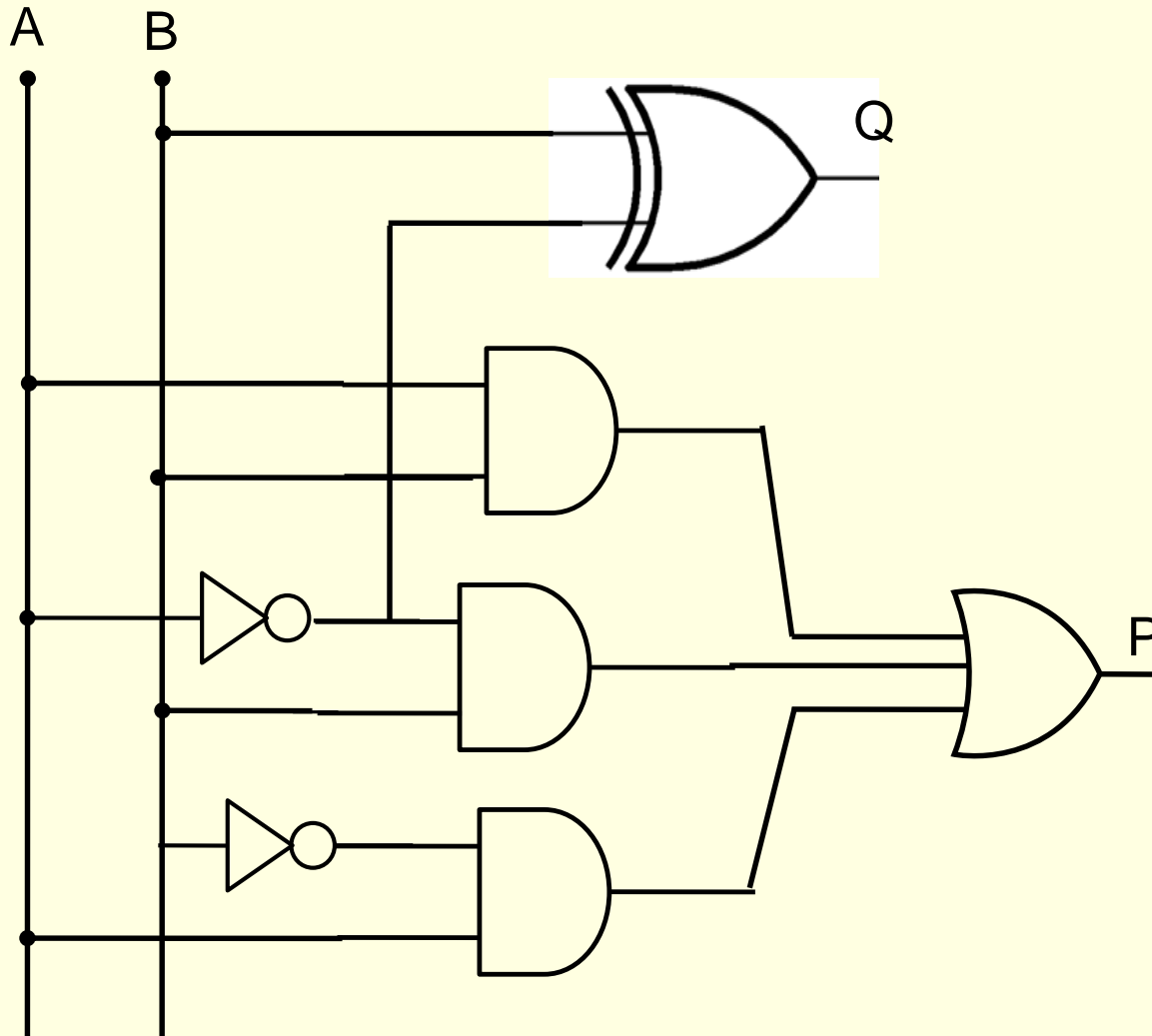
- $\overline{(\overline{X+Y}) + (\overline{YZ})}$
- $\overline{(\overline{X+Y})} \cdot \overline{(\overline{YZ})}$
- $(X+Y) (\overline{Y} + \overline{Z})$
- $X\overline{Y} + X\overline{Z} + Y\overline{Y} + Y\overline{Z}$
- $X\overline{Y} + X\overline{Z} + 0 + Y\overline{Z}$
- $X\overline{Y} + X\overline{Z} + Y\overline{Z}$

Make a truth table of output Y of the logic circuit of the stem.



C) Stem: determine P and simplify ?

D) Prove that $PQ = A.B$



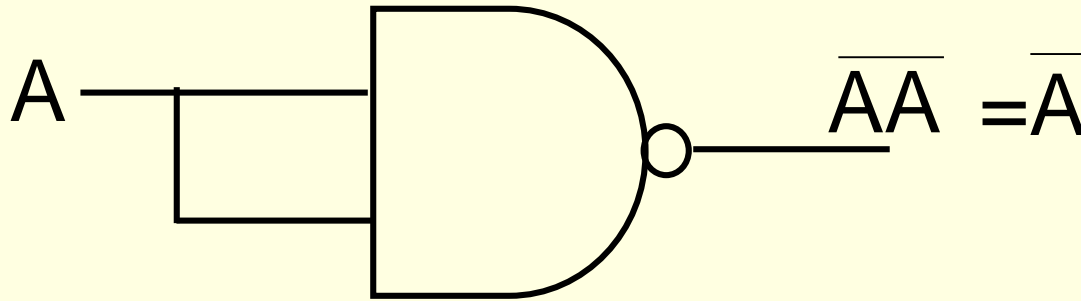
Universal logic gate

- The gate that can be used to implement all basic gates(AND,OR,NOT) called universal logic gate
- Example:
 - NAND gate
 - NOR gate

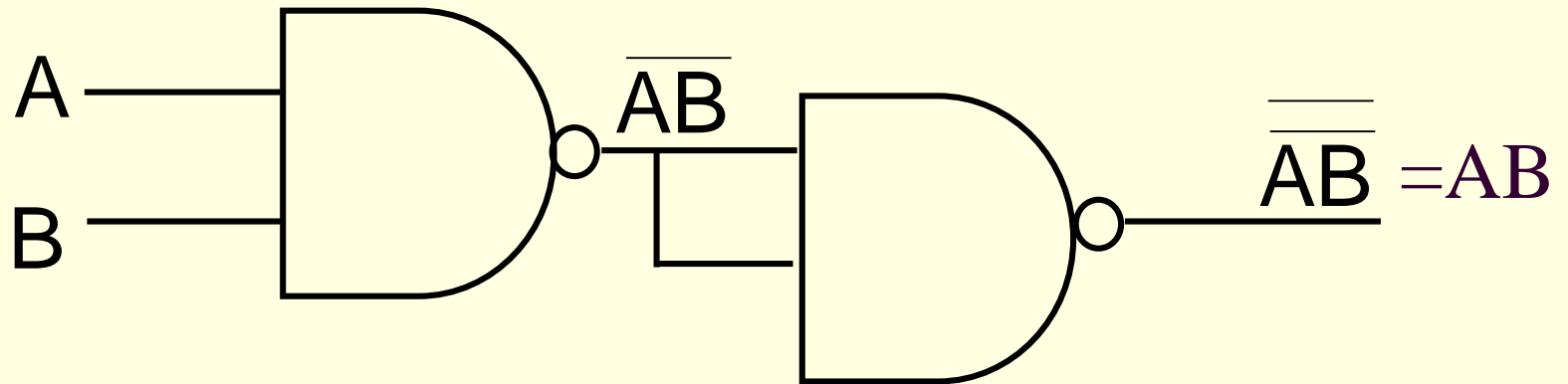
Prove that NAND is an universal gate

Prove the universality of NAND gate

1. Implementation of NOT gate by using NAND gate

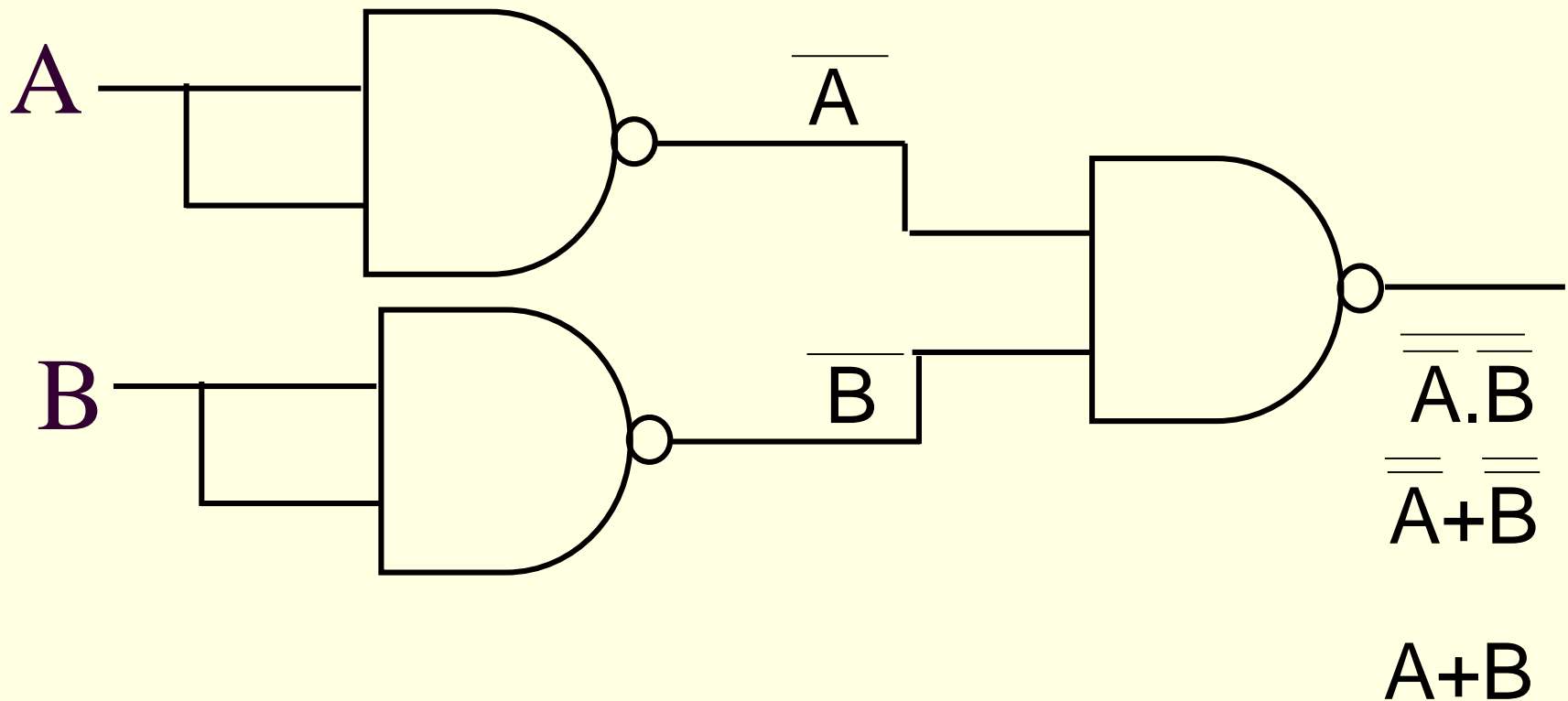


2. Implementation of AND gate by using NAND gate

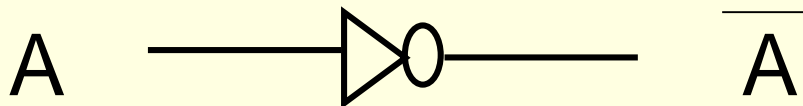
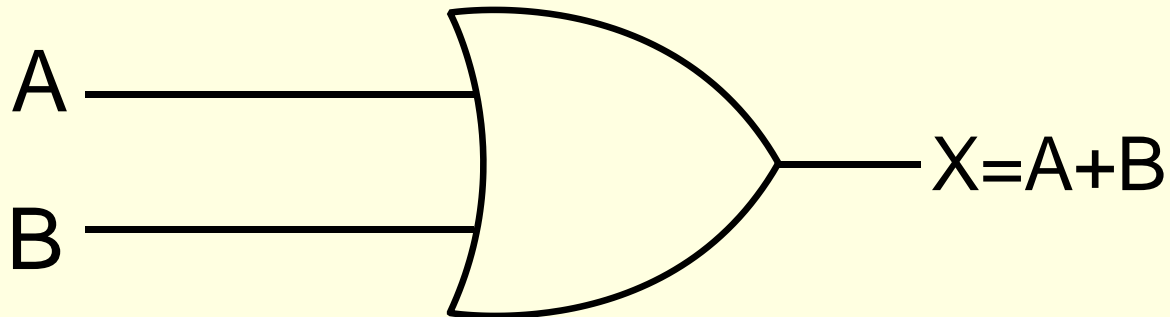
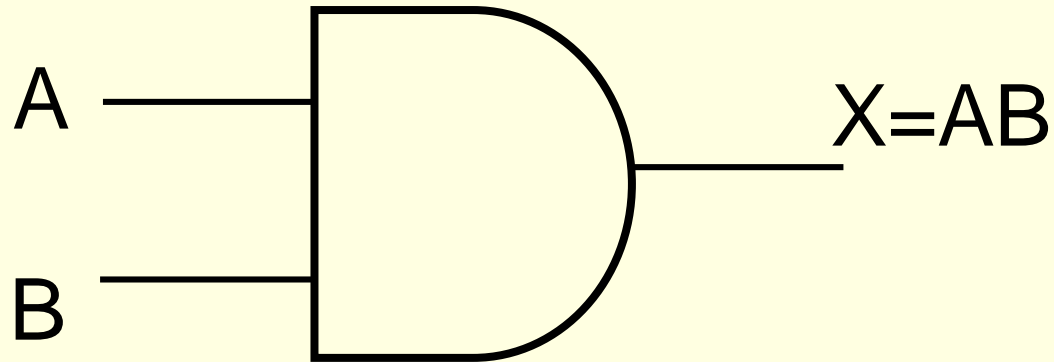


3. Implementation of OR gate by using NAND gate

•
$$= \overline{\overline{A} \cdot \overline{B}}$$



Can u implement by NAND



Implement figure 1 by figure2

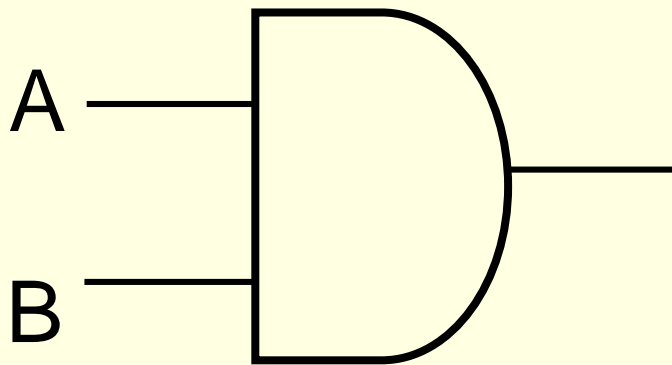


Figure1

A	B	X
0	0	1
0	1	1
1	0	1
1	1	0

Figure2

Implement figure 1 by figure2

A	B	X
0	0	0
0	1	1
1	0	1
1	1	1

Figure1

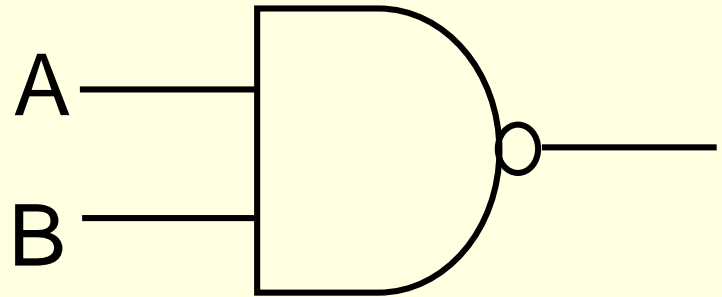


Figure2

Stem: implement Fig-2 by using fig-1

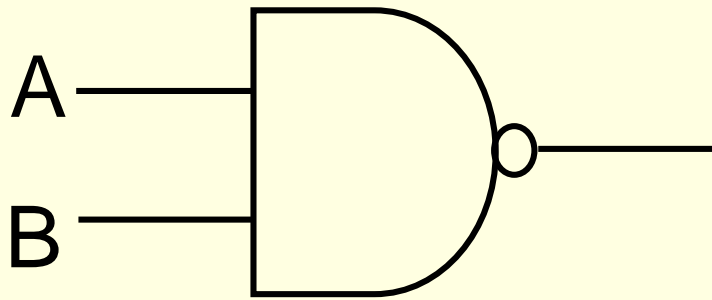


Fig-1

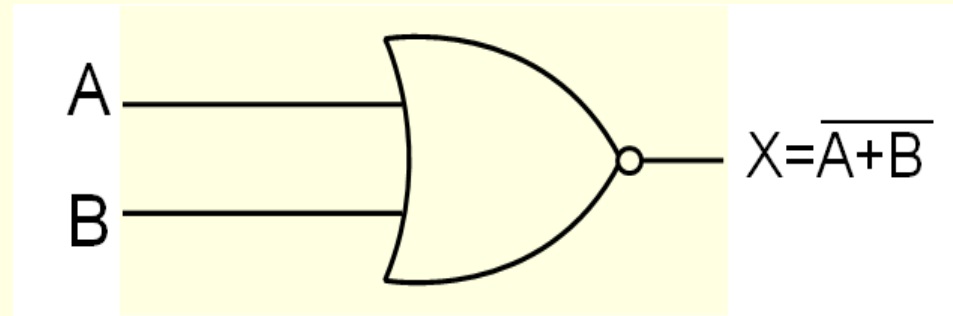


Fig-2

Implement fig1 by fig 2

■ Fig-1

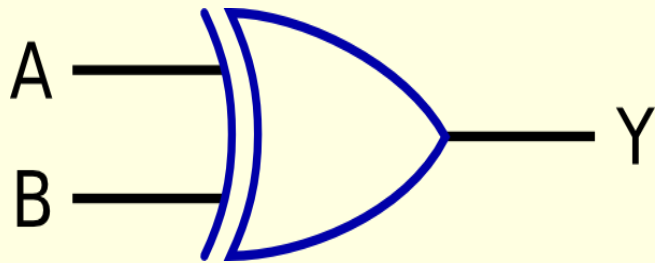
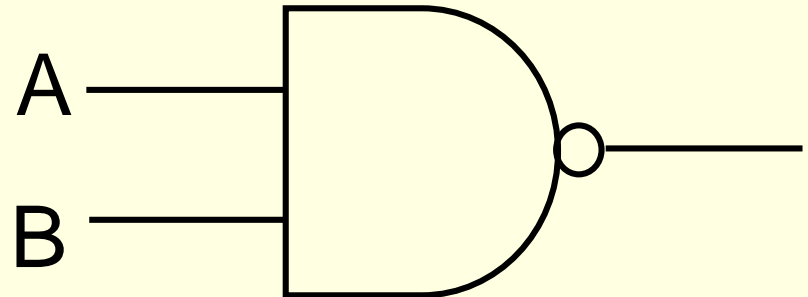


Fig-2



Implement fig1 by fig 2

■ Fig-1

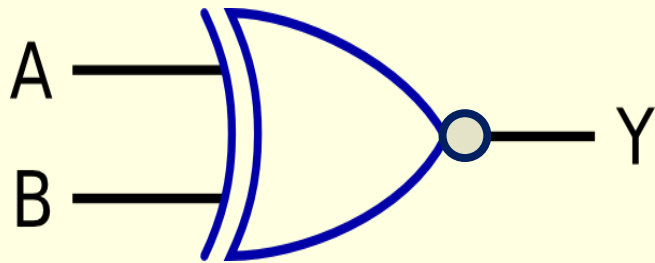
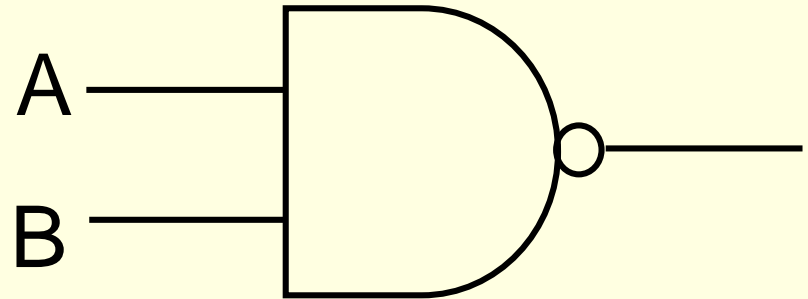


Fig-2



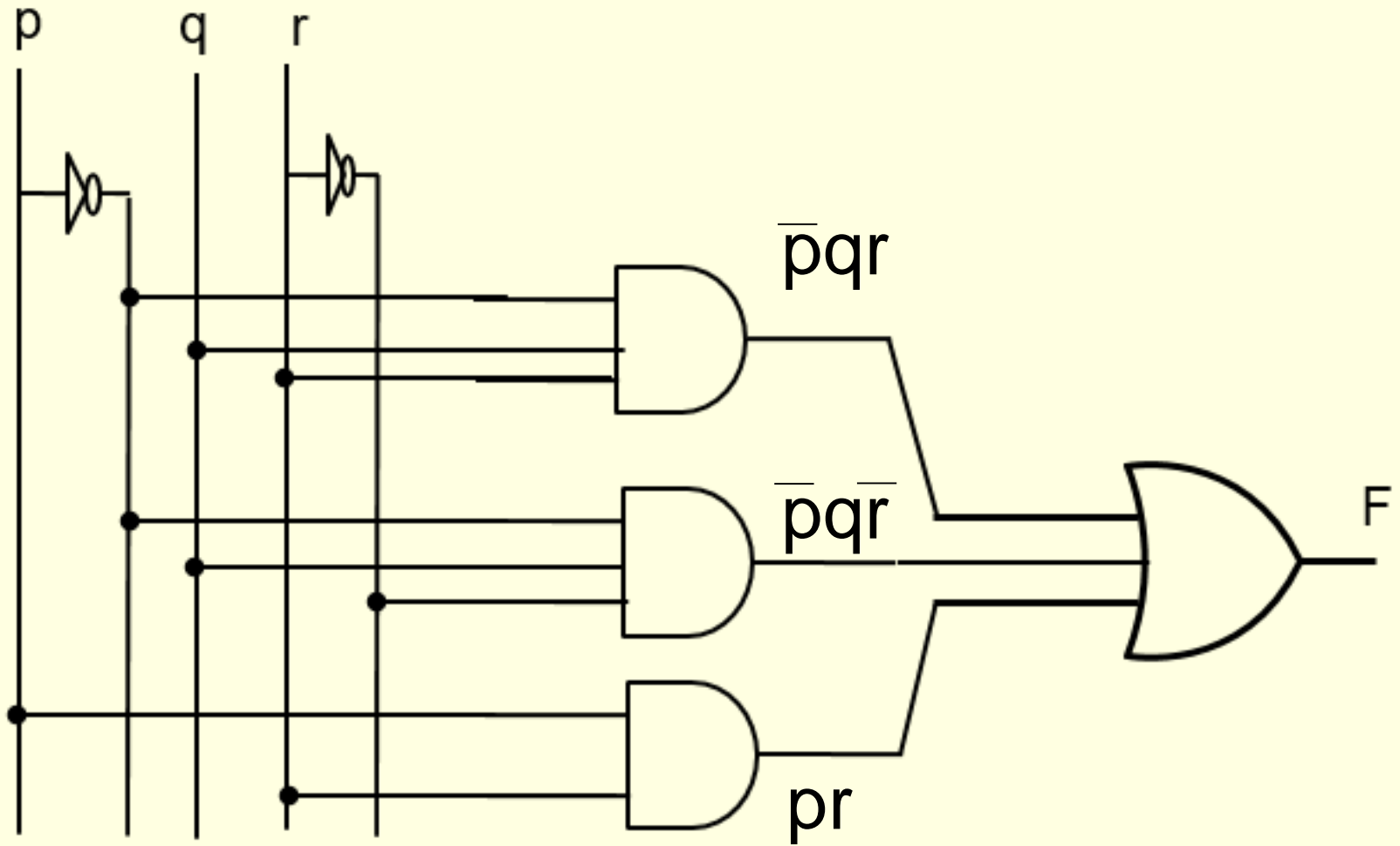
Implement fig-1 by fig-2

P	Q	T
0	0	1
0	1	0
1	0	0
1	1	1

Fig1

P	Q	T
0	0	1
0	1	0
1	0	0
1	1	0

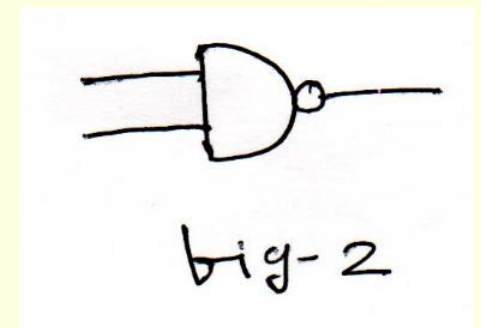
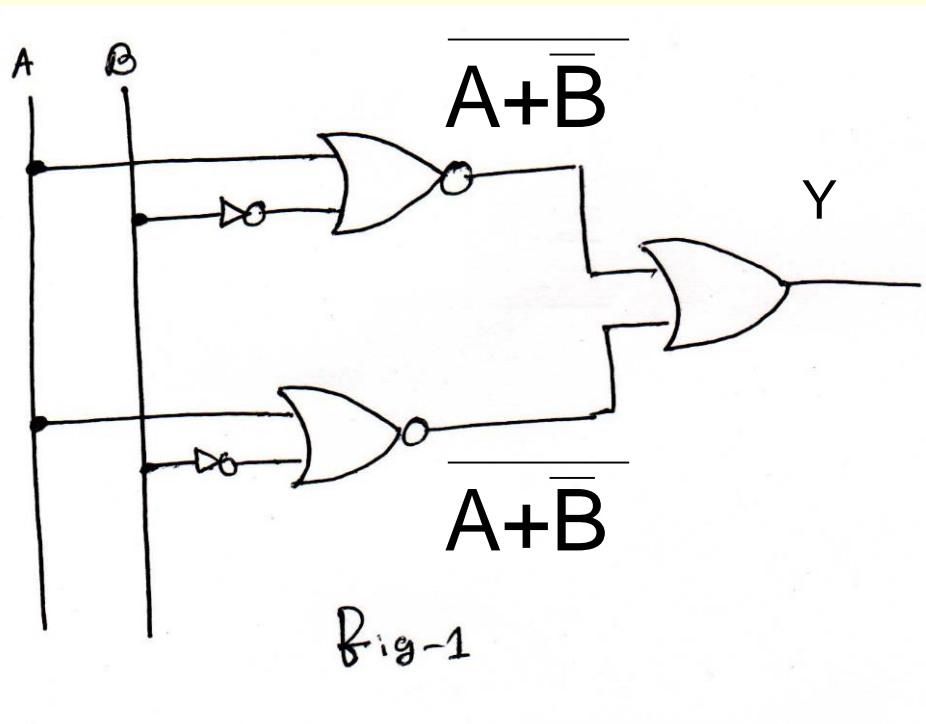
Fig2



- c) Simplify the output equation of logic circuit
- d) Enumerate the importance of NAND gate of the simplified result of 'F' by absolutely through NAND gate

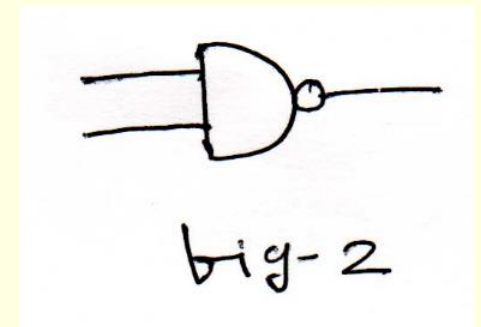
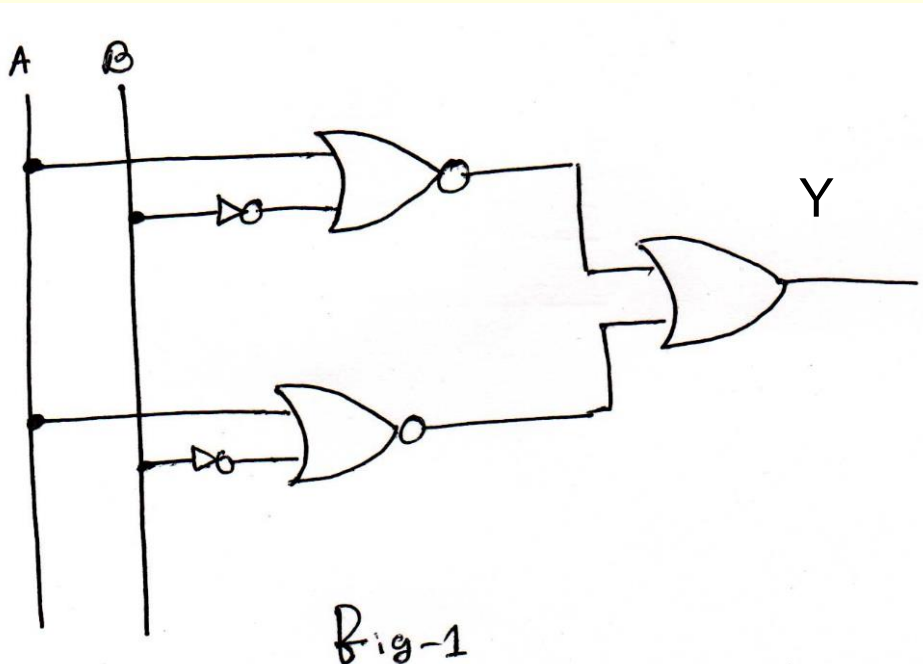
Cumilla 19

- Determine Y and Draw TT
- Is it possible to implement fig-1 by the gate represented by fig-2



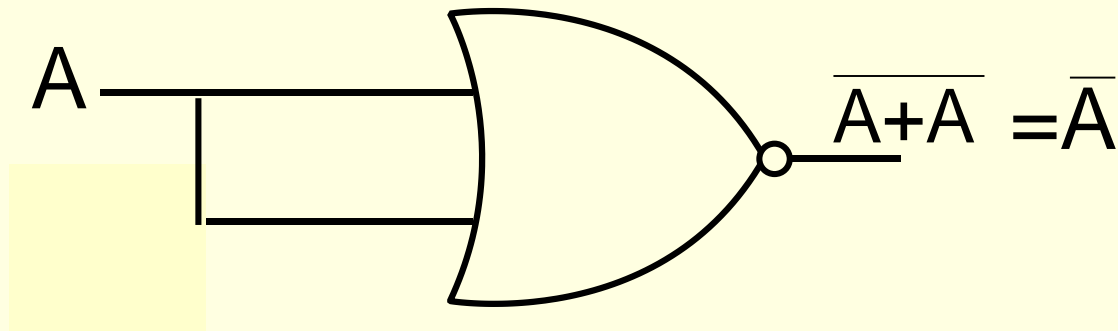
Cumilla 19

- Determine Y and Draw TT
- Is it possible to implement fig-1 by the gate represented by fig-2

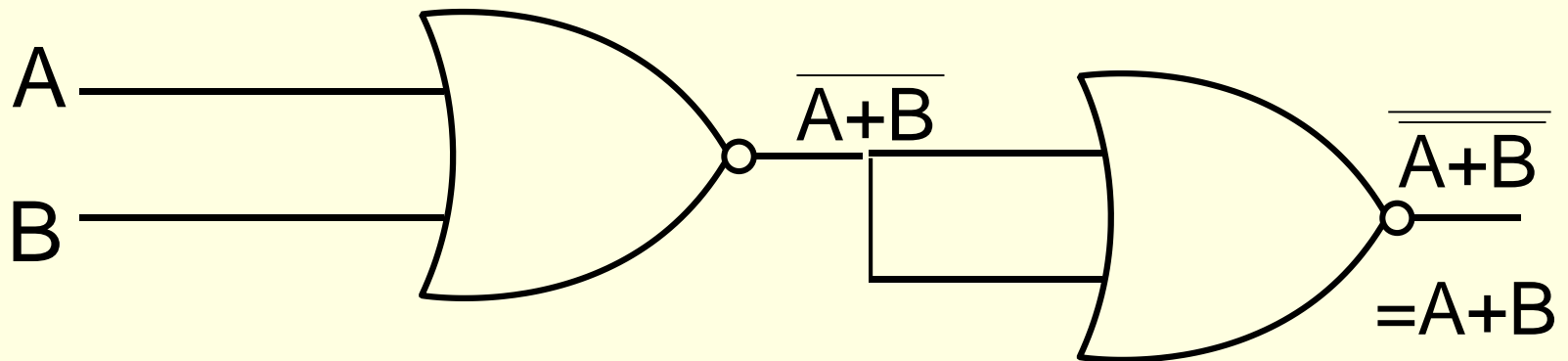


Universality of NOR

1. Implementation of NOT by NOR

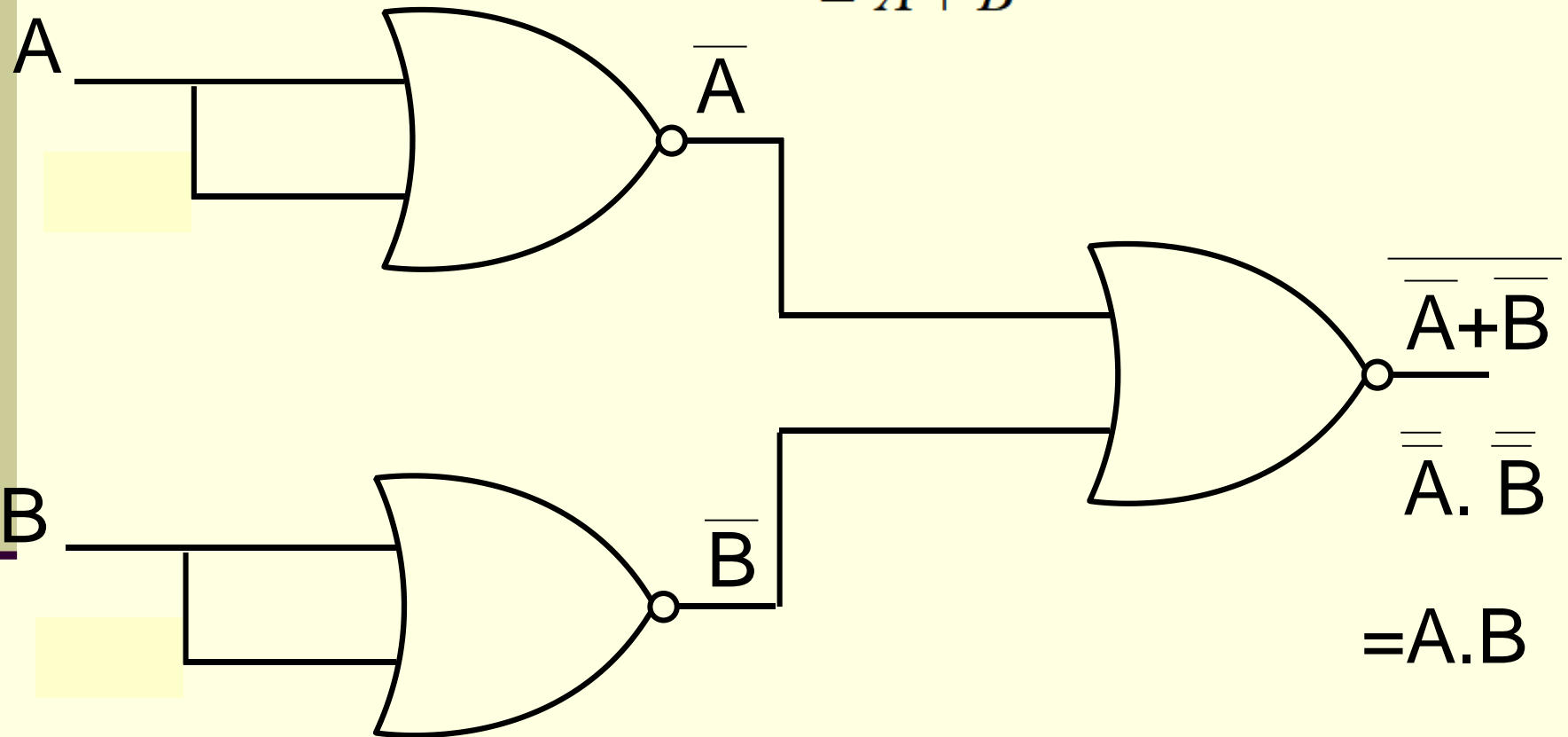


2. Implementation of OR by NOR

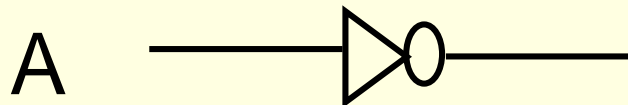
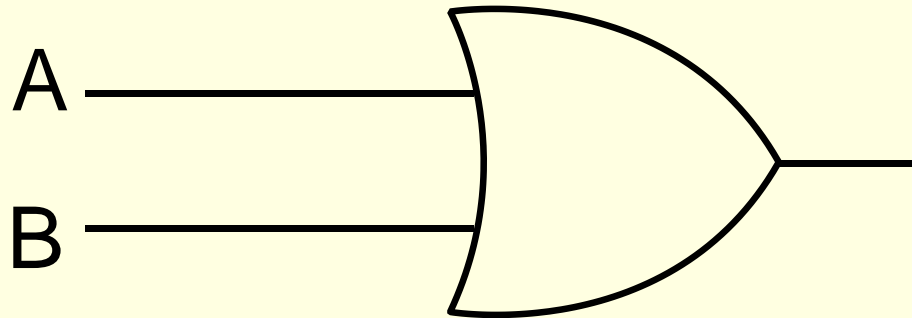
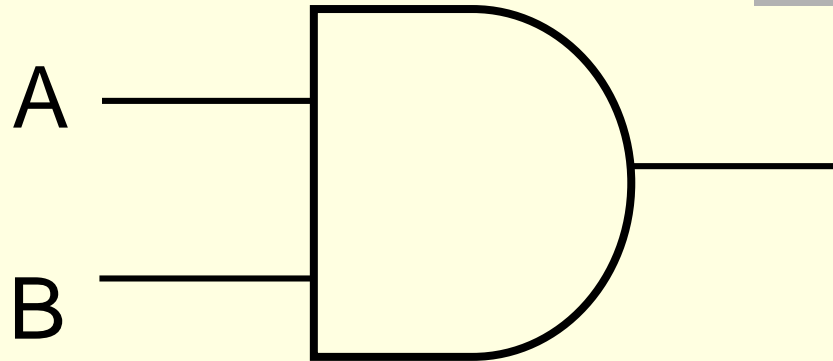


3. Implement AND by using NOR

$$= \overline{\overline{A} + \overline{B}}$$



Can u implement by NOR



Implement figure 1 by figure2

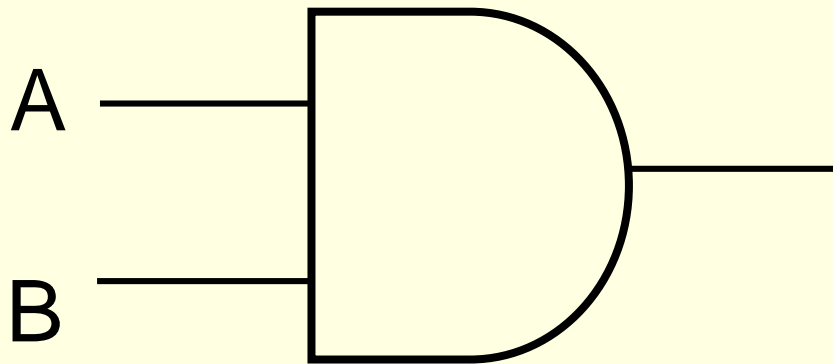


Figure1

A	B	X
0	0	1
0	1	0
1	0	0
1	1	0

Figure2

Implement figure 1 by figure2

A	B	X
0	0	0
0	1	1
1	0	1
1	1	1

Figure1

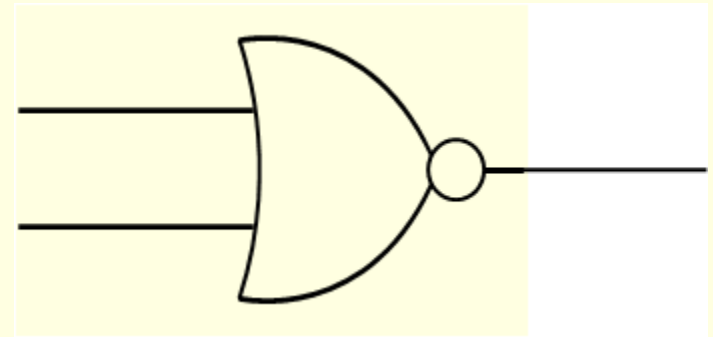


Figure2

Stem: implement Fig-1 by using fig-2

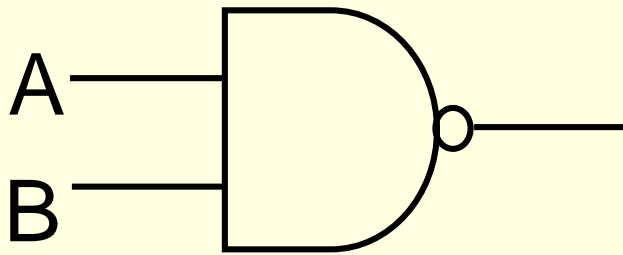


Fig-1

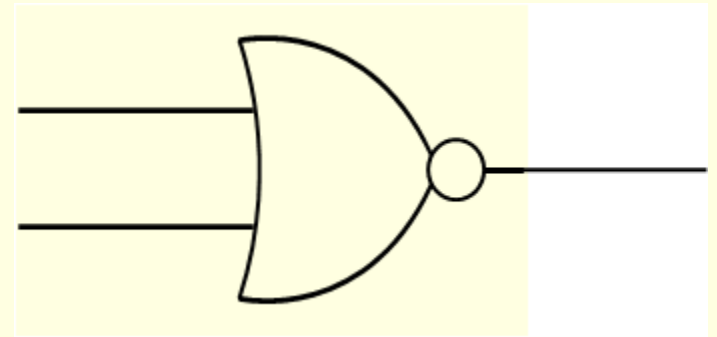


Fig-2

Implement fig1 by fig 2

■ Fig-1

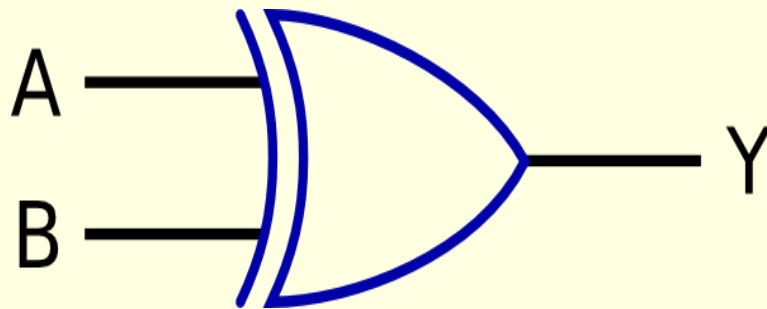
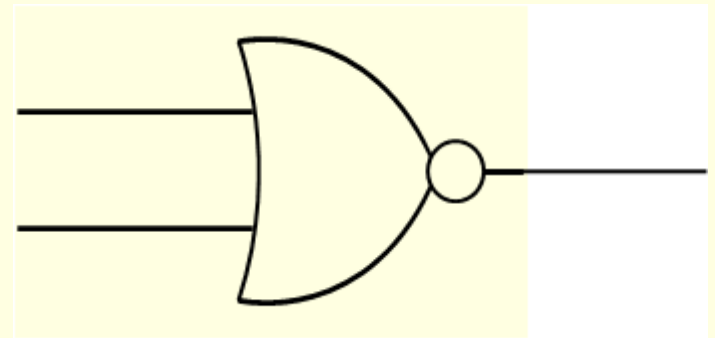


Fig-2



Implement fig1 by fig 2

■ Fig-1

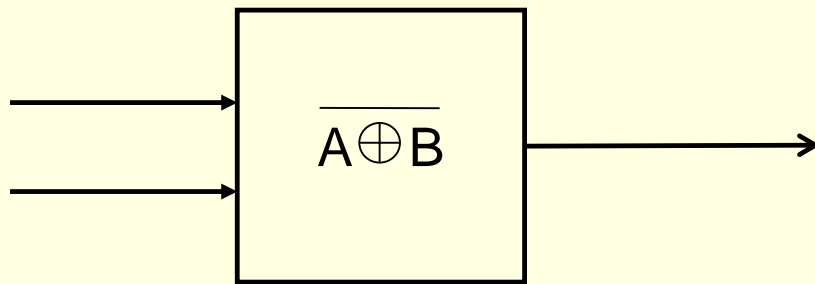
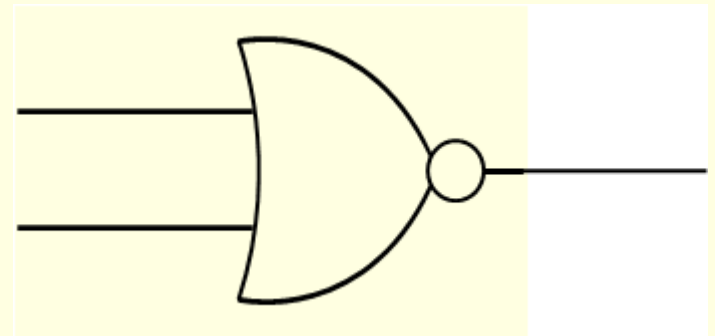
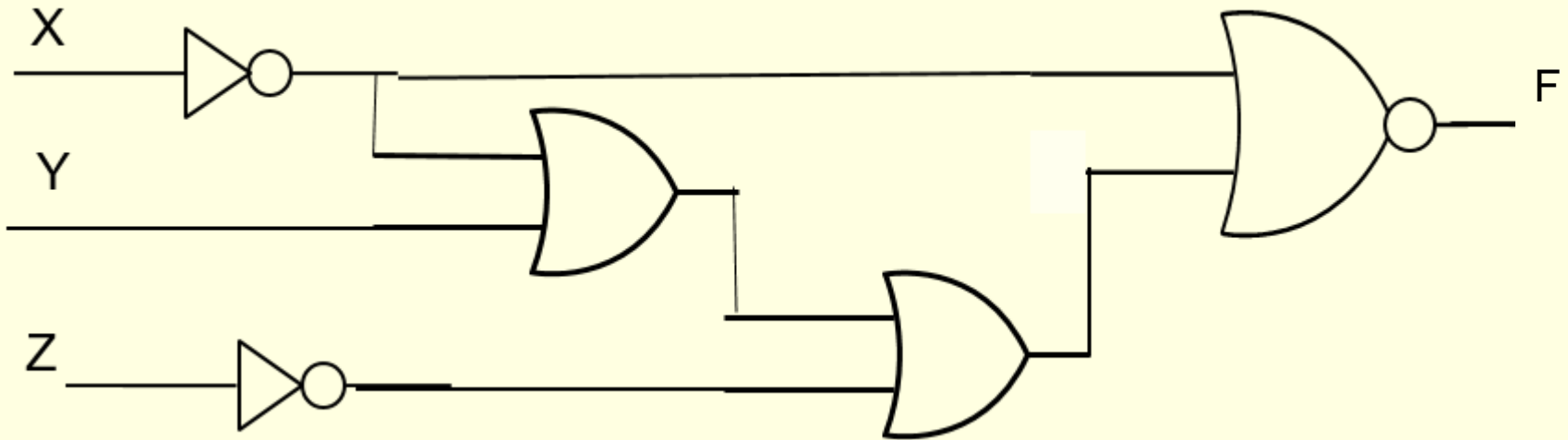


Fig-2



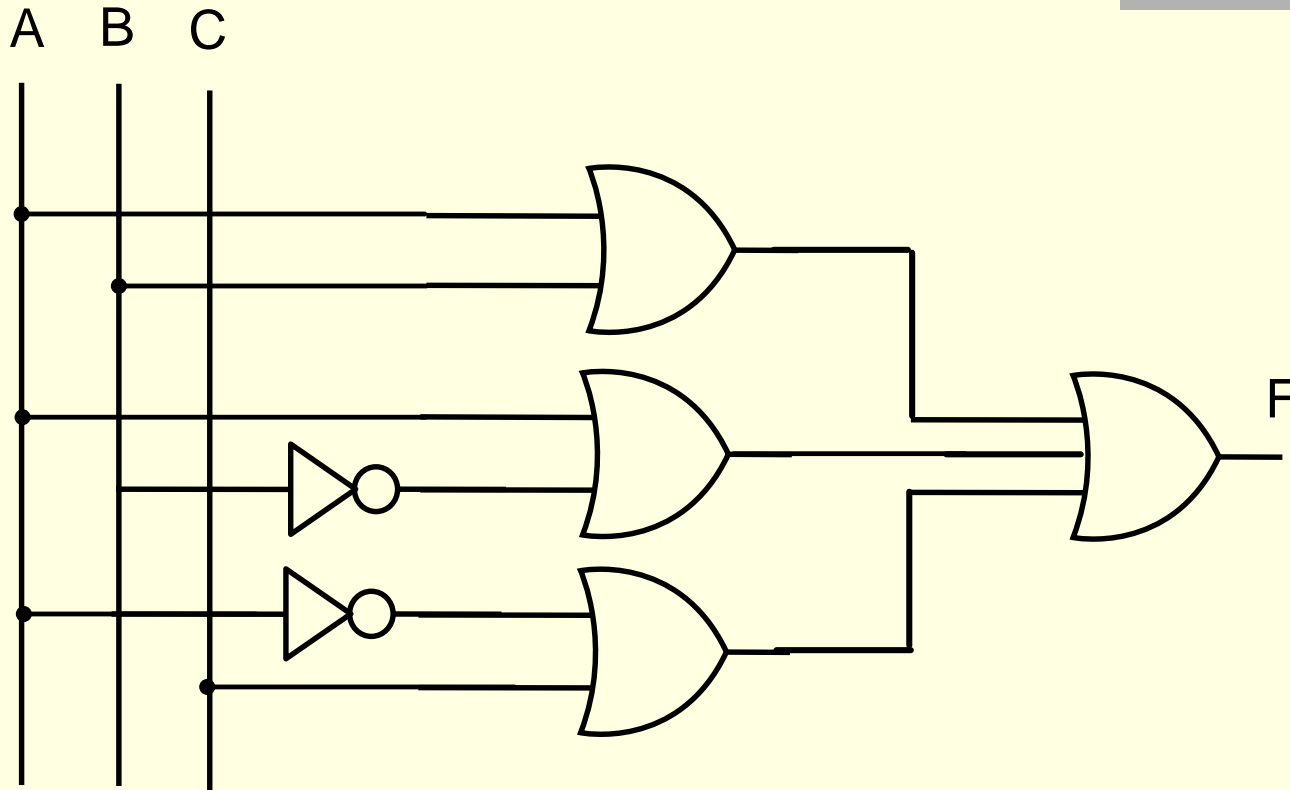


- Is it possible to implement the above circuit by NOR gate only? Analyze.

Implement F by NAND/NOR

$$F = A\bar{B} + B\bar{C}$$

Stem: DB 2017



Determine F and simplify

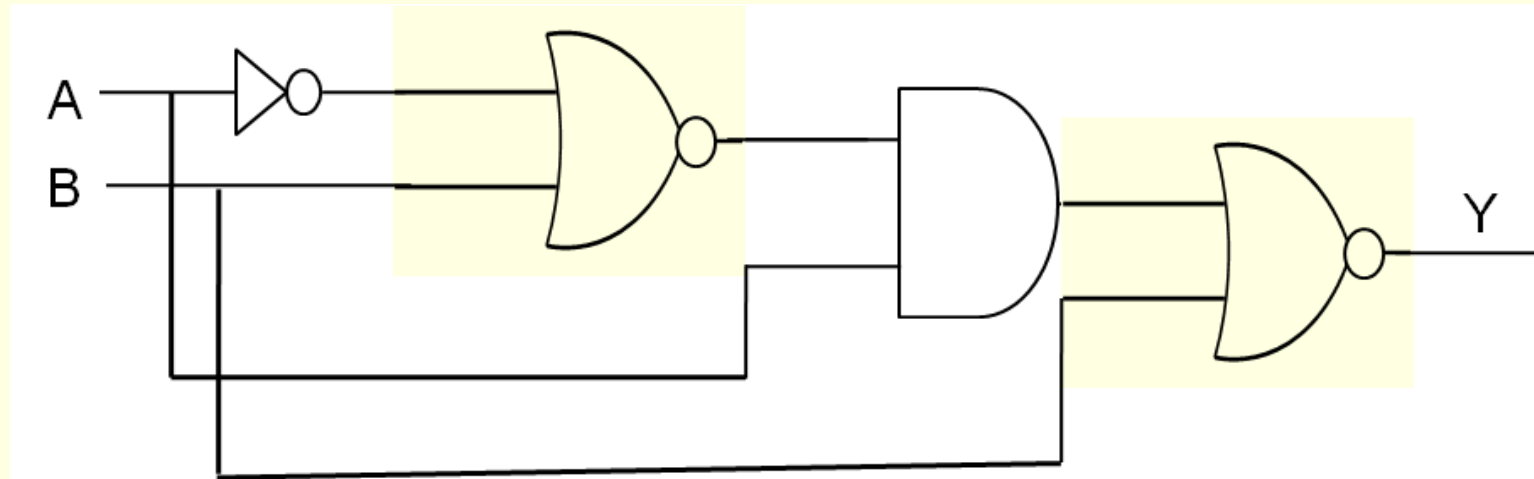
it is possible to implement simplified value of F by NOR gate only-Justify

H/W

$AB+BC+CA$ by NAND

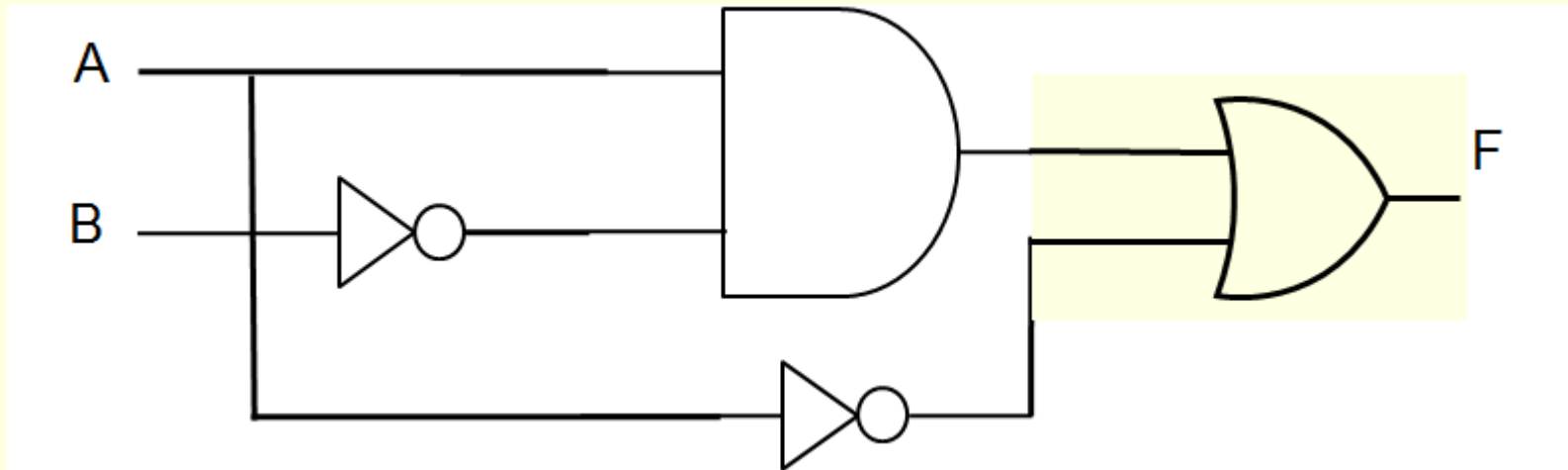
$AB+BC+CA$ by NOR

Stem: c) Find the output of the following circuit and simplify
d) proof that the output is a universal gate

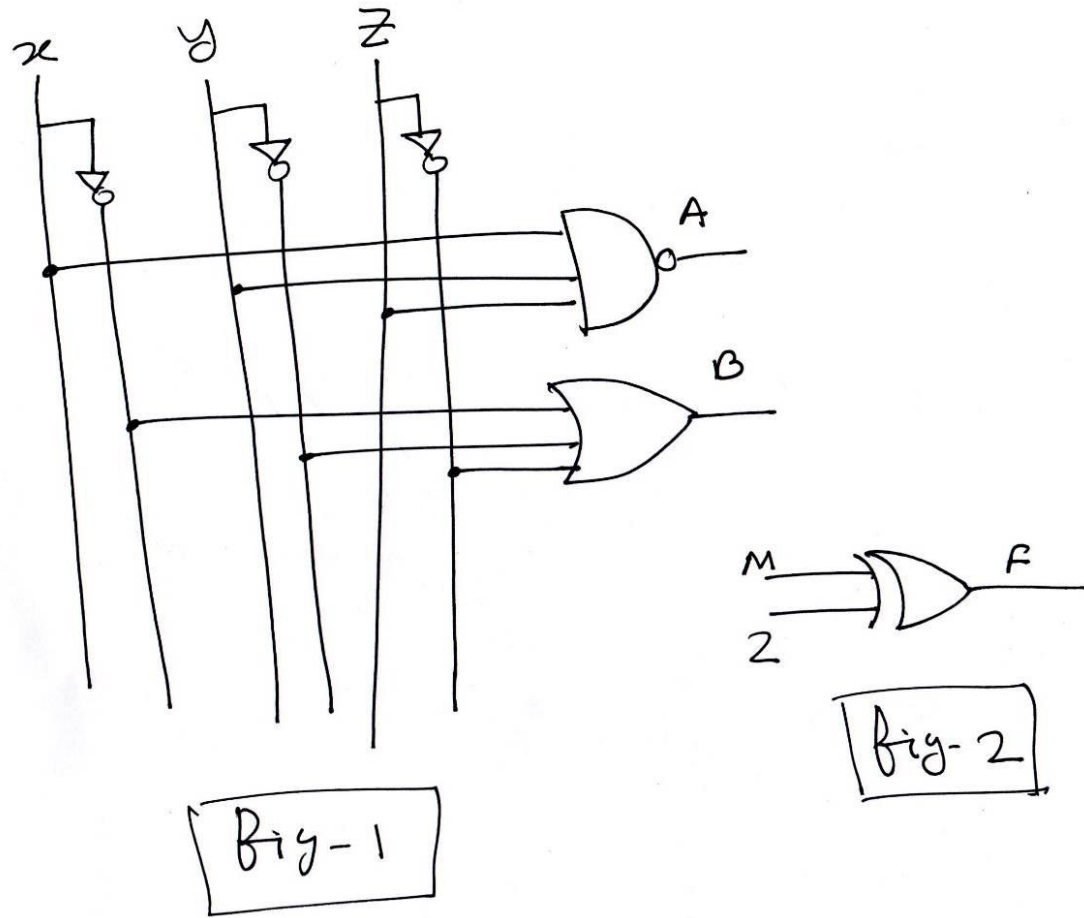


$$Ans : \overline{A}. \overline{B}$$

Stem: Stem: c) Determine the output and simplify it
d) Draw the TT after replacing the OR by NOR



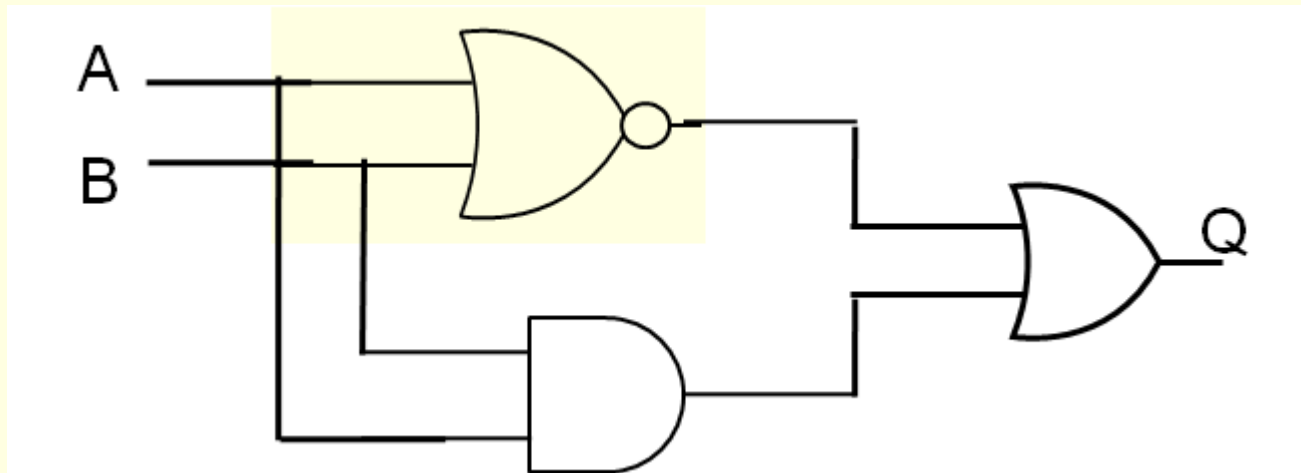
$$Ans : \bar{A} + \bar{B}$$



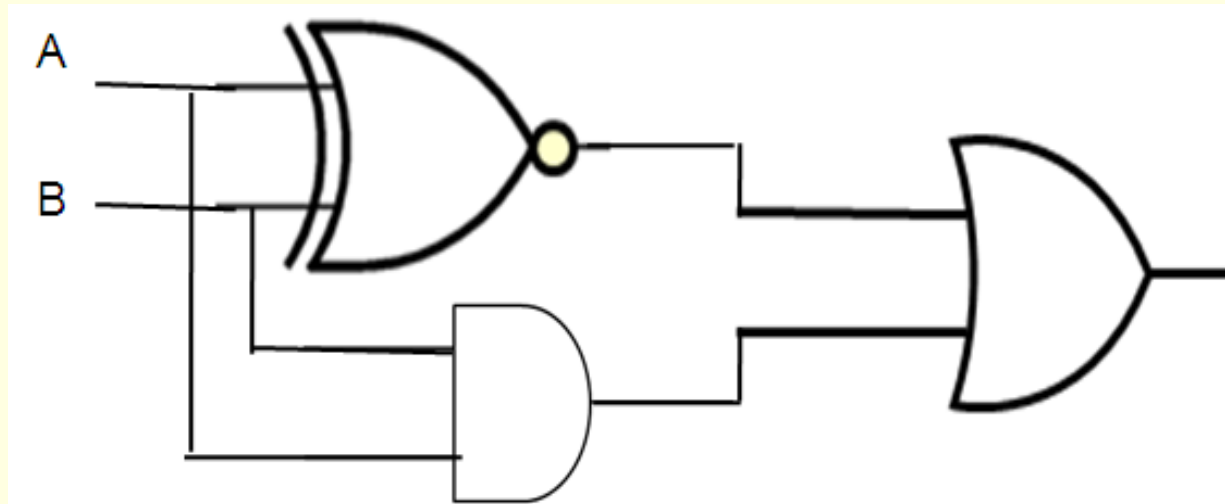
- C) Replace M of fig2 by output A then simplify
- D) proof $A=B$ by TT

Stem: C) Determine Q and simplify and compare the simplified value with X-OR gate

D) Implement Q by using NAND gate only



c) Draw the Truth table for Figure after simplifying the expression .



Stem: C) draw circuit of fig1 then Simplify
D)implement fig1 by the gate represented by fig 2

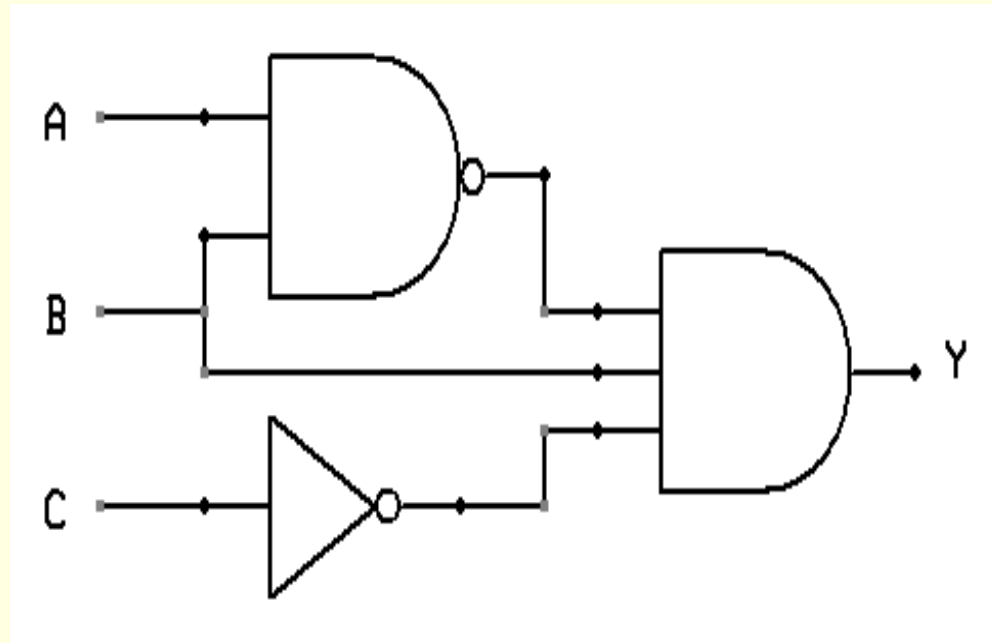
$$\overline{\overline{XY} + \overline{XYZ}}$$

Fig 1

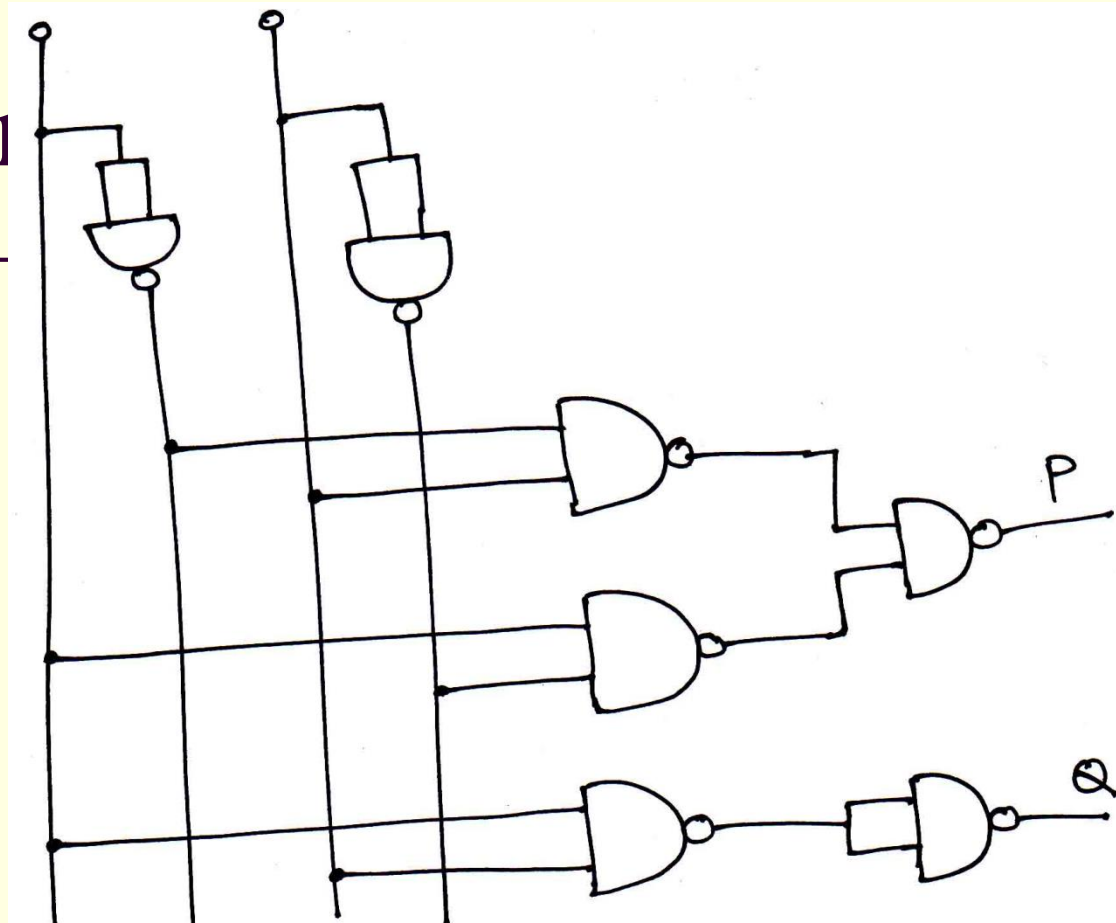
$$Ans : \overline{Y} + XZ$$

Fig-2		
A	B	X
0	0	1
0	1	0
1	0	0
1	1	0

Is it possible to implement the above logic circuit by only universal gate? Give your analytical opinion.

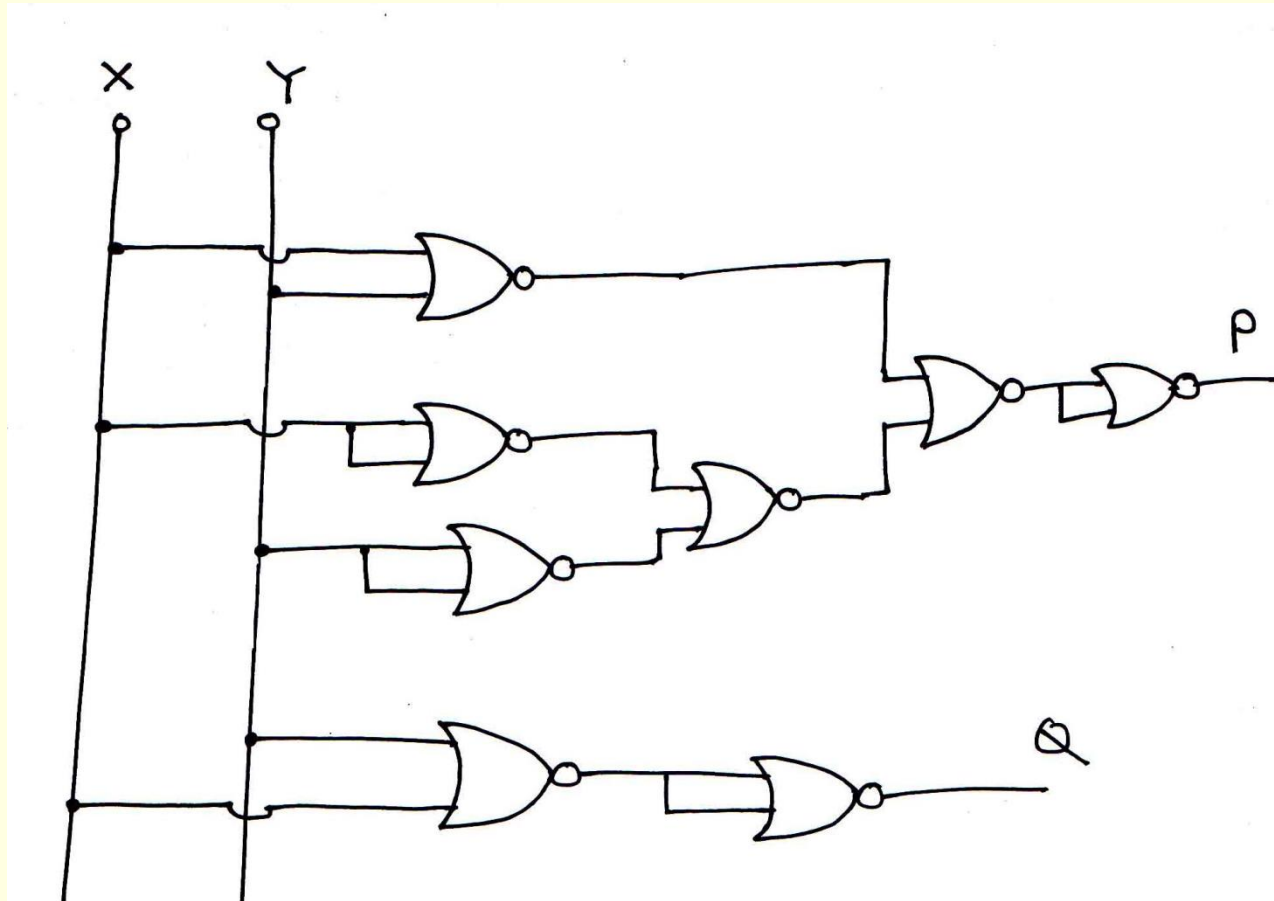


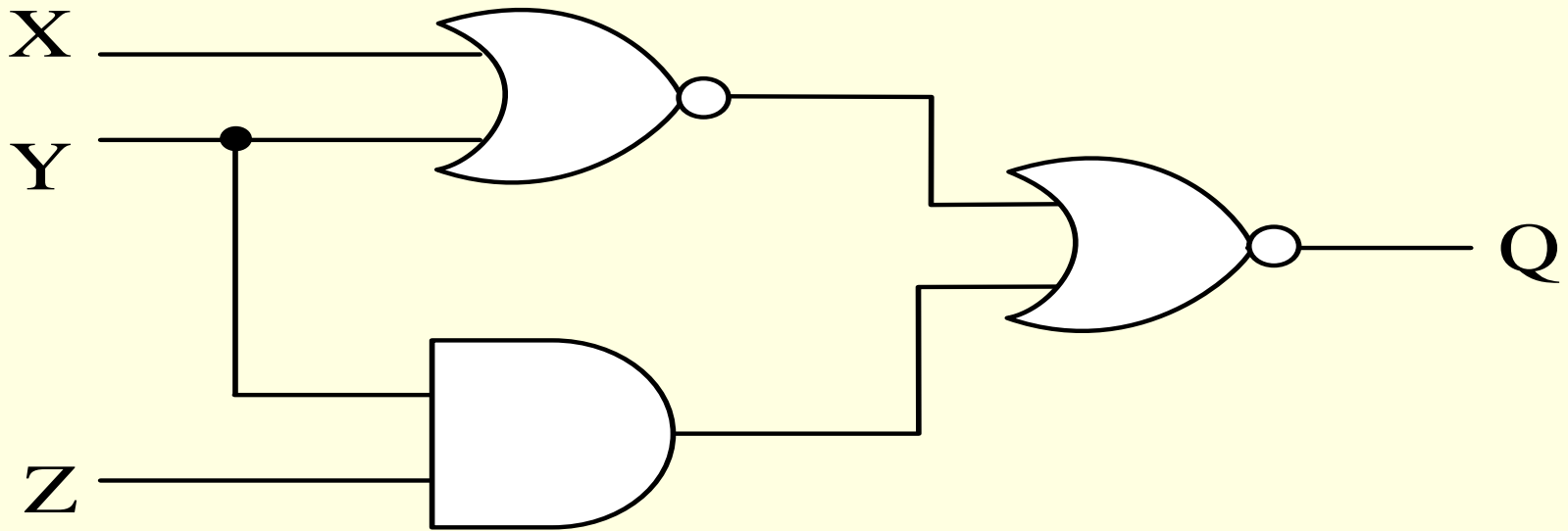
Step



- C) Implement Q by using NOR gate.
- D) use fewest number of gates to implement the circuit above

C) Determine Q and implement by NAND gate only
d) Is it possible to implement P by a single gate?
Justify your answer.





- Make a truth table of output Q of the logic circuit of the stem.
- Is it possible to implement the above logic circuit by only a **single** logic gate? Give your analytical opinion.

Stem

$$X = \overline{AB} + BC$$

$$Y = \overline{ABC} + ABC + AB + B\overline{C}$$

-
- C) Implement X by using NOR only
 - D) Show that simplification of Y leads to easy implementation of the circuit

Stem:

Figure-1

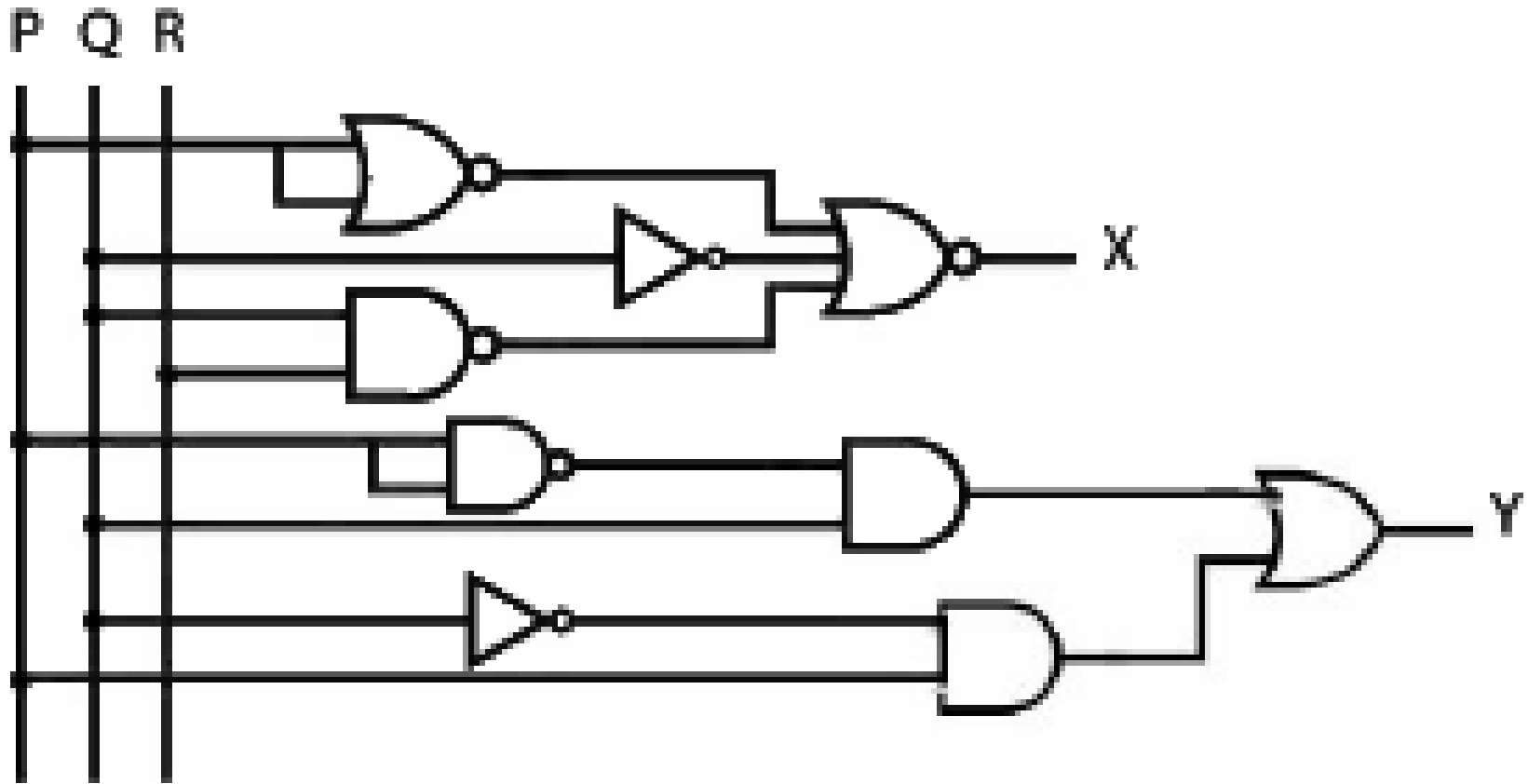
$$Q = \overline{(A + \overline{B})\overline{C}} + C$$

Figure-2

A	B	K
0	0	1
0	1	1
1	0	1
1	1	0

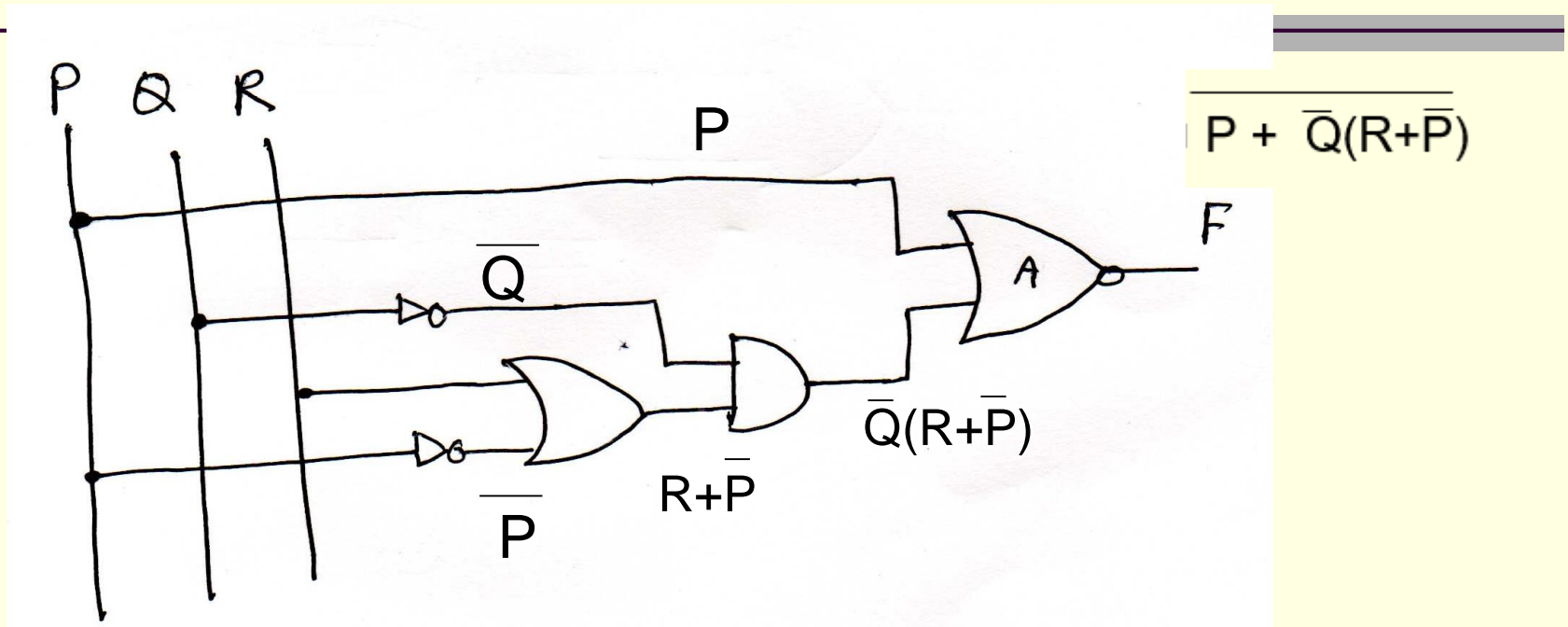
c) Draw truth table for Q

d) Is it possible to implement Figure1 by using the gate preseneted Figure-2.
justify your answer.



- C) Show the simplified value of Y in truth table.
- D) Implement value of X by NOR gate

B-19

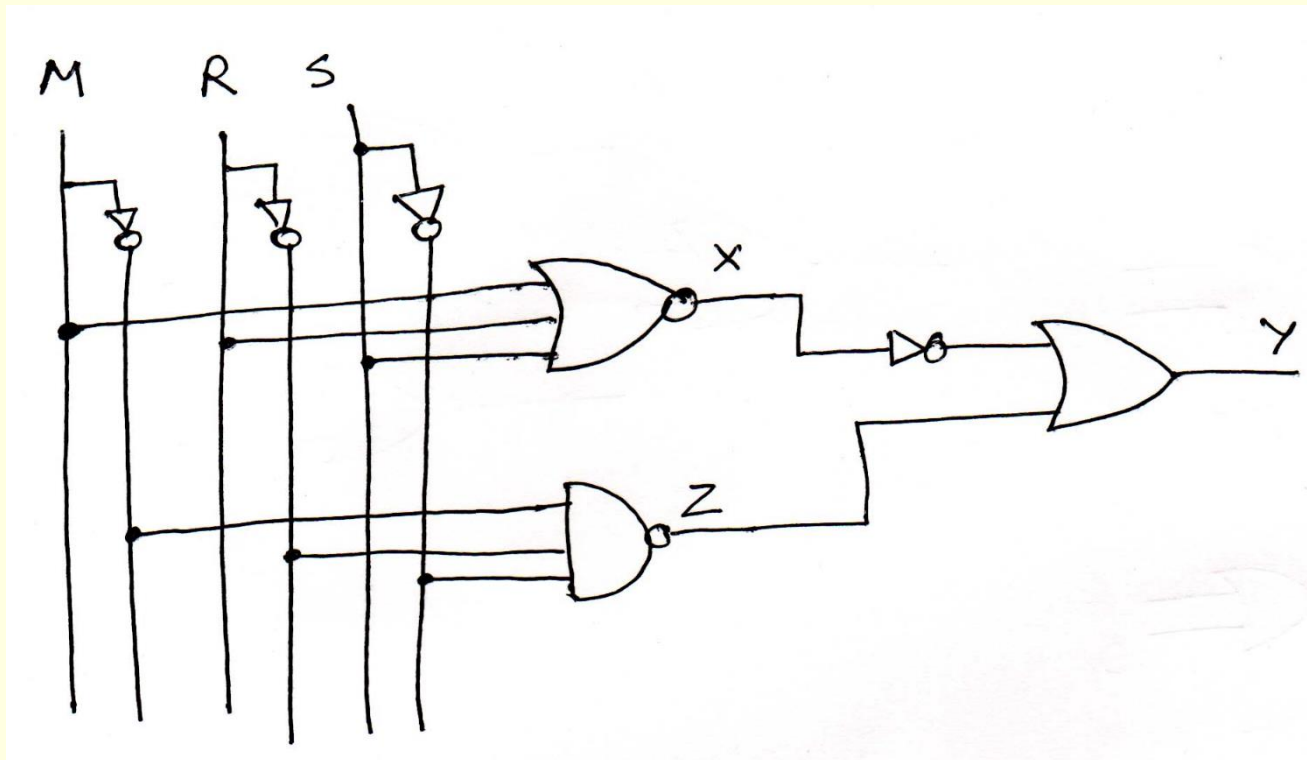


Determine F by TT

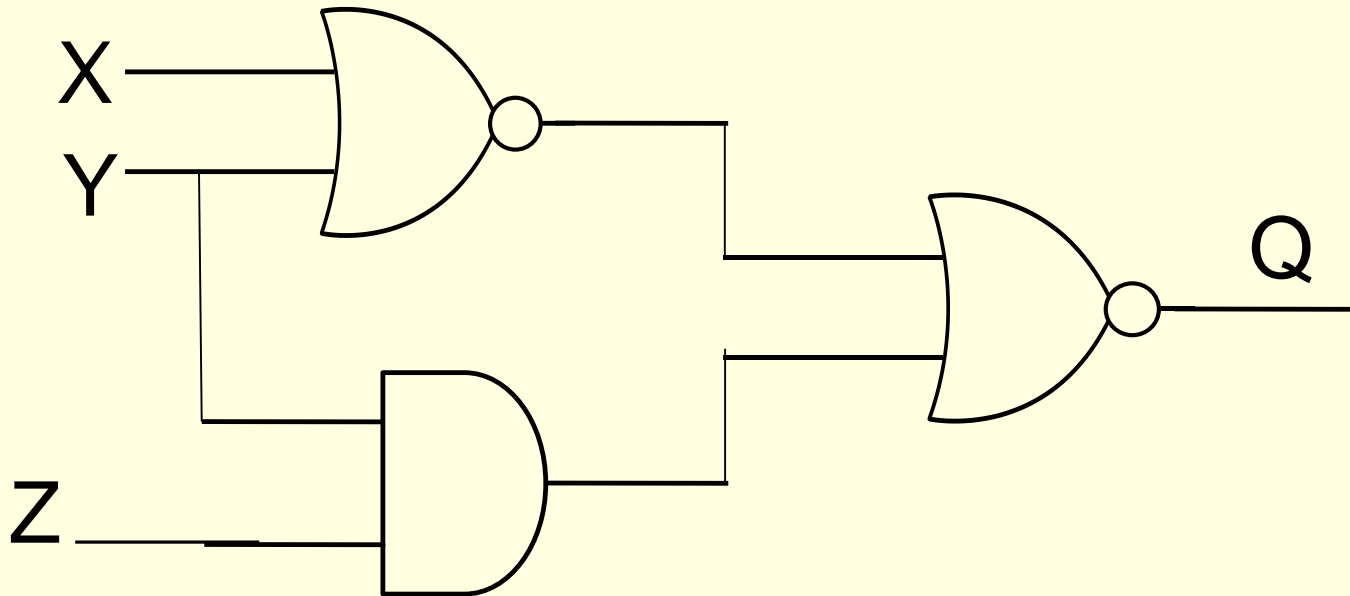
show that output F can be implemented by the gate
signed as 'A'

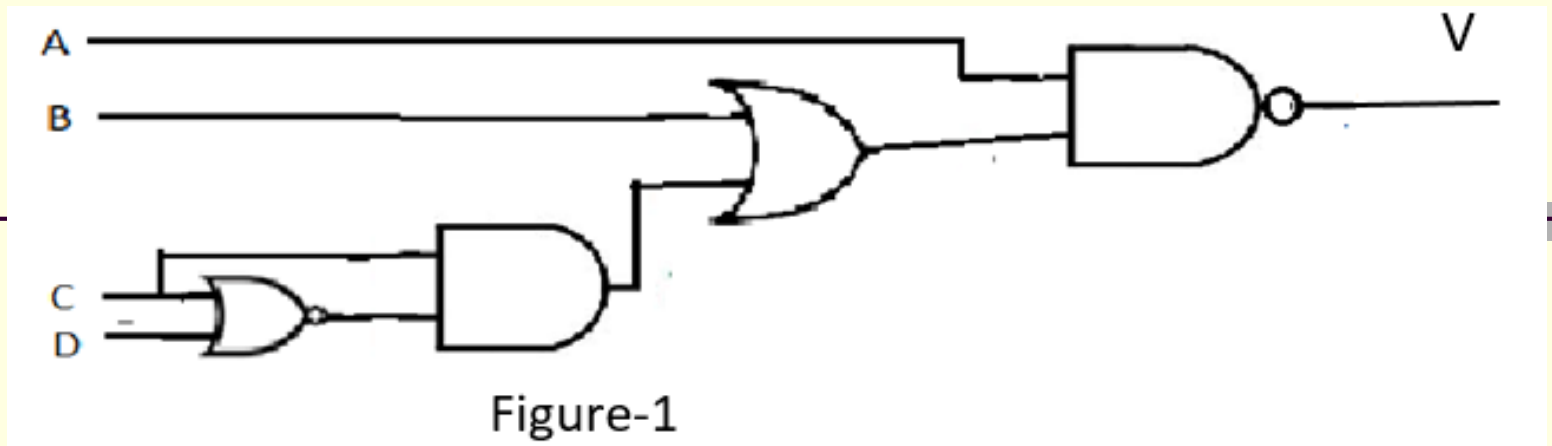
r19

- Determine Y
- Implement Y by NAND



d) is it possible to implement Q by a single gate?





- (c) Determine the value of V of figure-1 of the stem.
- (d) Replace the basic gates of figure-1 by NAND gates and show that the entire circuit can be represented by basic gates.