

Le Pendu

An exploration of Neo-Riemannian Transformations
and Euclidean Rhythms

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Euclidean Rhythms

What is a Euclidean Rhythm?

• Euclidean Algorithm

- A way to find the greatest common divisor of two numbers
- The largest number that divides two numbers without leaving a remainder

• How does this translate to music?

- Here, the numbers we are looking at are number of pulses and number of notes
- Let us take 8 pulses and 5 notes (1's are on notes and 0's are off notes)

Example: gcd(6,33)

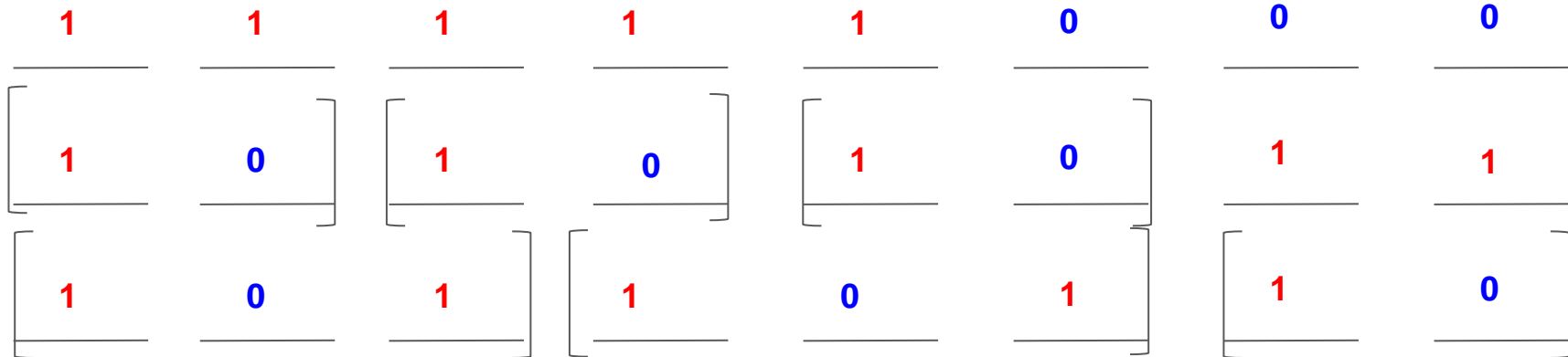
$$33 = (6)(x) + r$$

$$33 = (6)(5) + 3$$

$$6 = (3)(x) + r$$

$$6 = (3)(2) + 0$$

So, our greatest common divisor is 3



Euclidean Rhythms in Our Piece

19

1 2 3 4 5 6 7 8 9 10 11 12

1 2 3 4 5

1 0 1 0 1 0 0 1 0 1 0 0

1 1 1 1 1 0 0 0 0 0 0 0

(1 0) (1 0) (1 0) (1 0) (1 0) 0 0

(1 0 0) (1 0 0) (1 0) (1 0) (1 0)

(1 0 0 1 0) (1 0 0) { 1 0 } (1 0)

Now onto:

Neo Riemannian Transformations

Music: A mathematical interpretation

A prelude to Neo-Riemannian Transformations

Definition 1 Let $\langle a, b, c \rangle$ be a **major** chord, then $b = a + 4$, and $c = a + 7$

where $a, b, c \in \mathbb{Z}_{12}$

Definition 2 Let $\langle a, b, c \rangle$ be a **minor** chord, then $b = a + 3$, and $c = a + 7$

where $a, b, c \in \mathbb{Z}_{12}$.

Now that we have defined the elements, we will refer to them as *pitch*

class triads and will denote the set of these 24 major and minor triads.

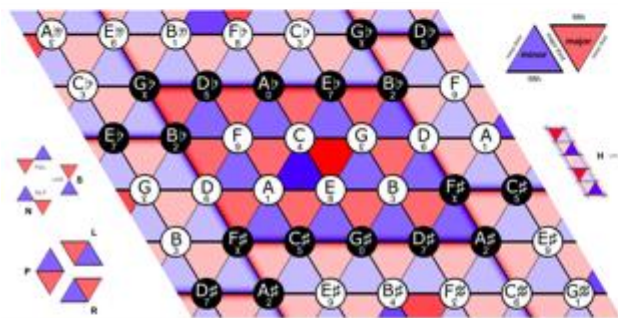
The entire set is displayed in the table.

Table: Set of all major and minor triads

Major Chords		Minor Chords	
C	$\langle 0, 4, 7 \rangle$	C	$\langle 0, 3, 7 \rangle$
C \sharp /D \flat	$\langle 1, 5, 8 \rangle$	c \sharp /d \flat	$\langle 1, 4, 8 \rangle$
D	$\langle 2, 6, 9 \rangle$	D	$\langle 2, 5, 9 \rangle$
E \flat /D \sharp	$\langle 3, 7, 10 \rangle$	e \flat /d \sharp	$\langle 3, 6, 10 \rangle$
E	$\langle 4, 8, 11 \rangle$	E	$\langle 4, 7, 11 \rangle$
F	$\langle 5, 9, 0 \rangle$	F	$\langle 5, 8, 0 \rangle$
F \sharp /G \flat	$\langle 6, 10, 1 \rangle$	f \sharp /g \flat	$\langle 6, 9, 1 \rangle$
G	$\langle 7, 11, 2 \rangle$	G	$\langle 7, 10, 2 \rangle$
A \flat /G \sharp	$\langle 8, 0, 3 \rangle$	a \flat /g \sharp	$\langle 8, 11, 3 \rangle$
A	$\langle 9, 1, 4 \rangle$	A	$\langle 9, 0, 4 \rangle$
B \flat /A \sharp	$\langle 10, 2, 5 \rangle$	b \flat /a \sharp	$\langle 10, 1, 5 \rangle$
B	$\langle 11, 3, 6 \rangle$	B	$\langle 11, 2, 6 \rangle$

Neo-Riemannian Theory - An exploration of transformations

- Harmonies directly to each other instead of invoking tonal relations
- (Purely Harmonic) Transformations



P-L-R Transformations

P - Transformation.

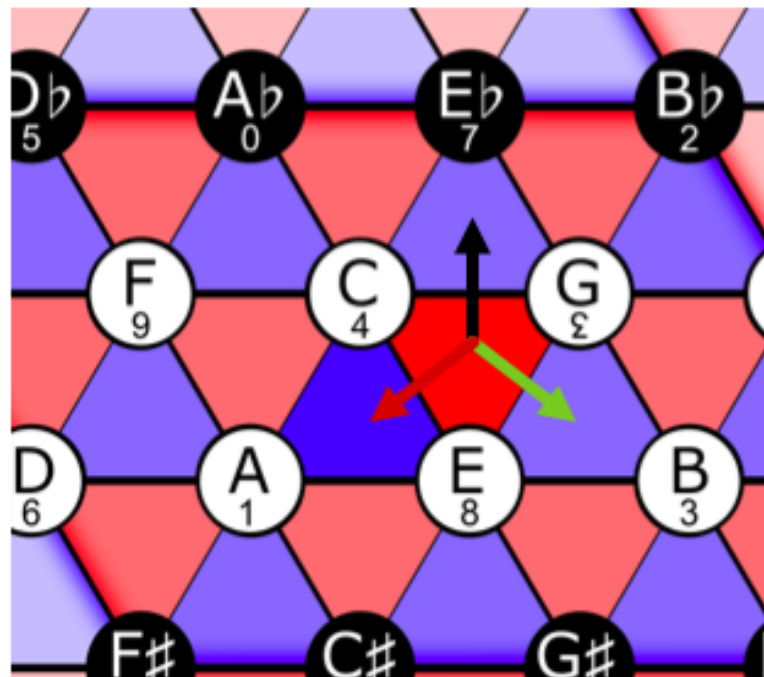
$C-E-G \rightarrow C-Eb-G$

L - Transformation.

$C-E-G \rightarrow B-E-G$

R - Transformation.

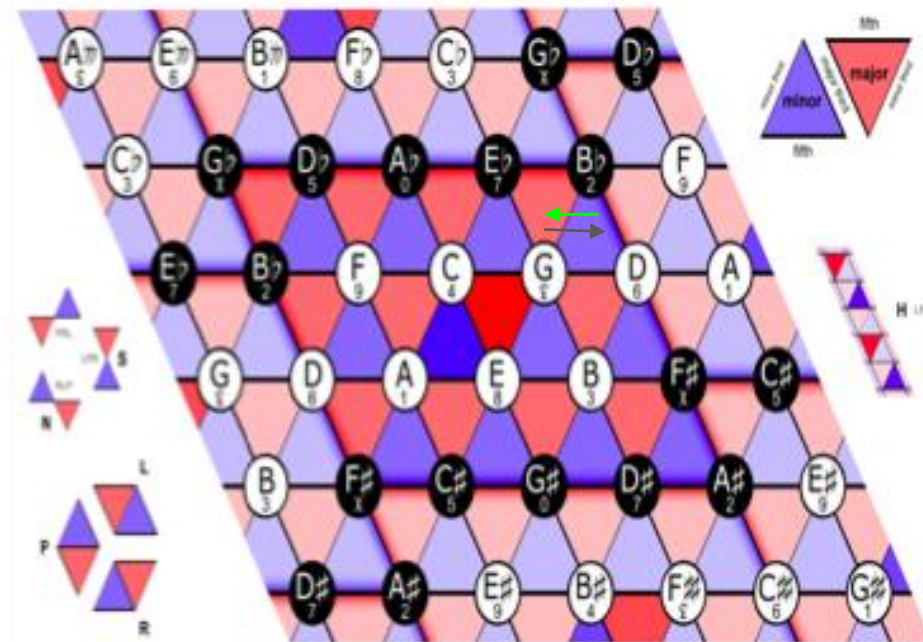
$C-E-G \rightarrow A-C-E$



Evolution of the piece in the tonnetz.

The piece: [Lependu](#)

1. A-B-A Piece
2. Prelude



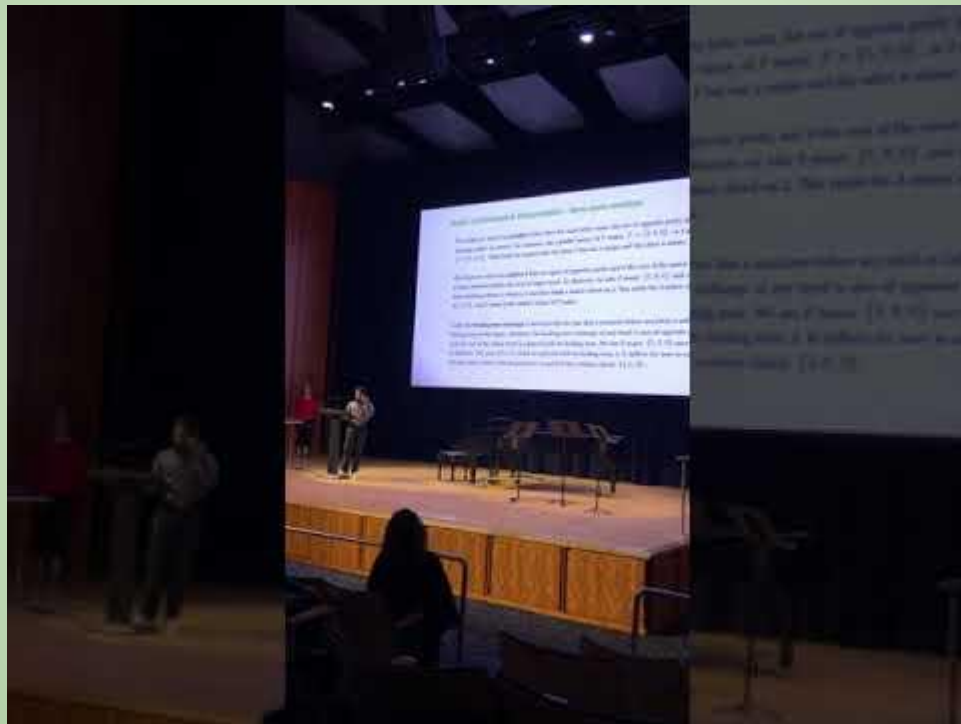
The following is an example of a transformation performed in the piece

Grave ♩ = 120

The musical score is written for piano in 8/8 time, marked 'Grave' with a tempo of 120 beats per minute. It consists of two staves: a treble staff and a bass staff. The treble staff contains chords, and the bass staff contains a continuous eighth-note pattern. A green arrow points from the first measure to the second measure, indicating a transformation.

Mathematical music composition workshop

Fall 2019



Thank you!