

Bayesian Inference for Brain Activity from Multi-Resolution Functional Magnetic Resonance Imaging

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Introduction

- **Personalized medicine:** need for patient-specific functional mapping. Surgeons want to minimize damage to healthy, functional tissue
- Variations in functional neuroanatomy [e.g. 1]
- MR imaging methods used to aid presurgical planning and neuronavigation

Why multiple resolutions?

- Surgery requires high spatial precision
- Signal-to-noise ratio (SNR) decreases as spatial resolution increases

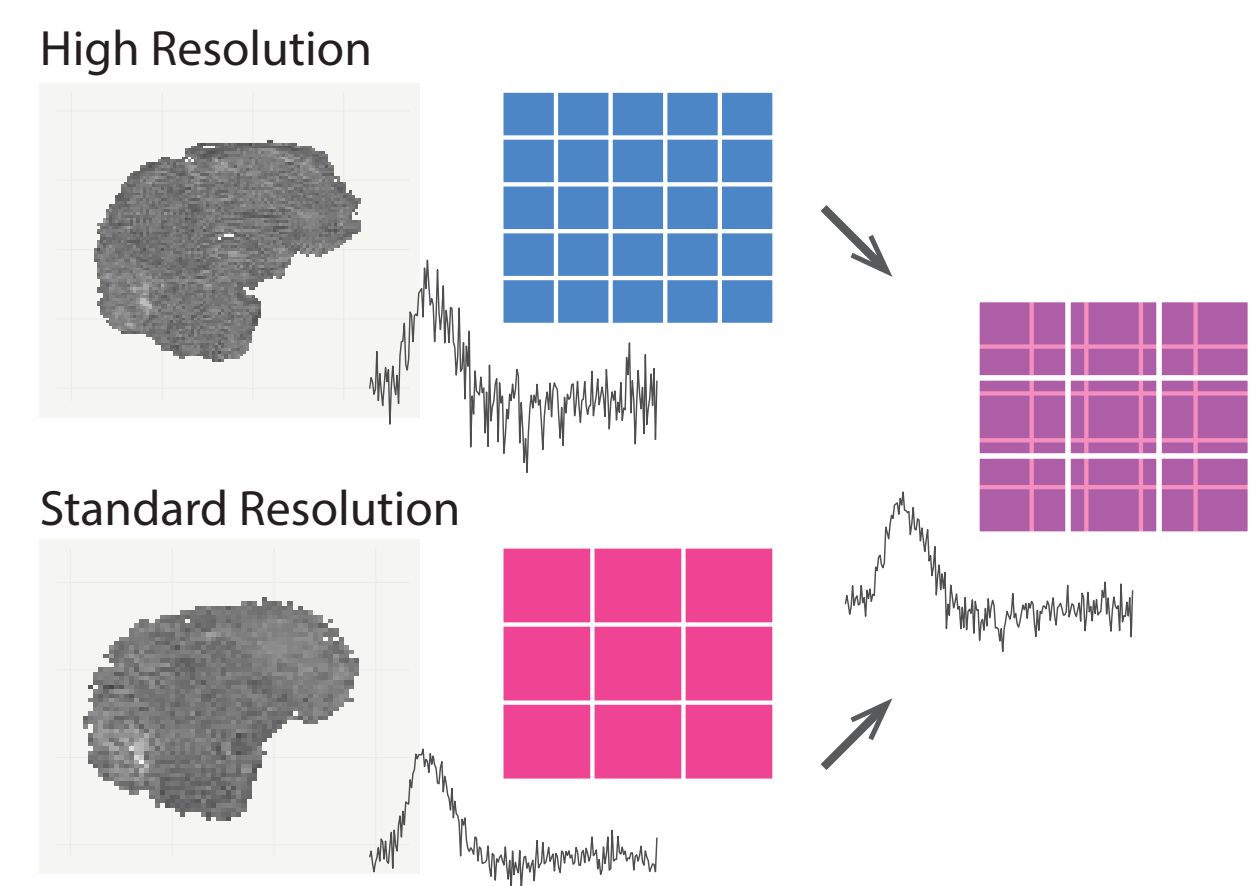


Fig 1: Unique blessing/curse of data collected at “high” and “standard” resolutions ($1.8 \times 1.8 \times 2.3 \text{ mm}^3$ and $3 \times 3 \times 3.45 \text{ mm}^3$ voxels; voxel-volumetric pixel)

Goal: to leverage spatial precision from high resolution data and SNR from standard resolution data

- Inference at high resolution voxel locations
- Utilize massive spatial information to conduct within-patient functional mapping

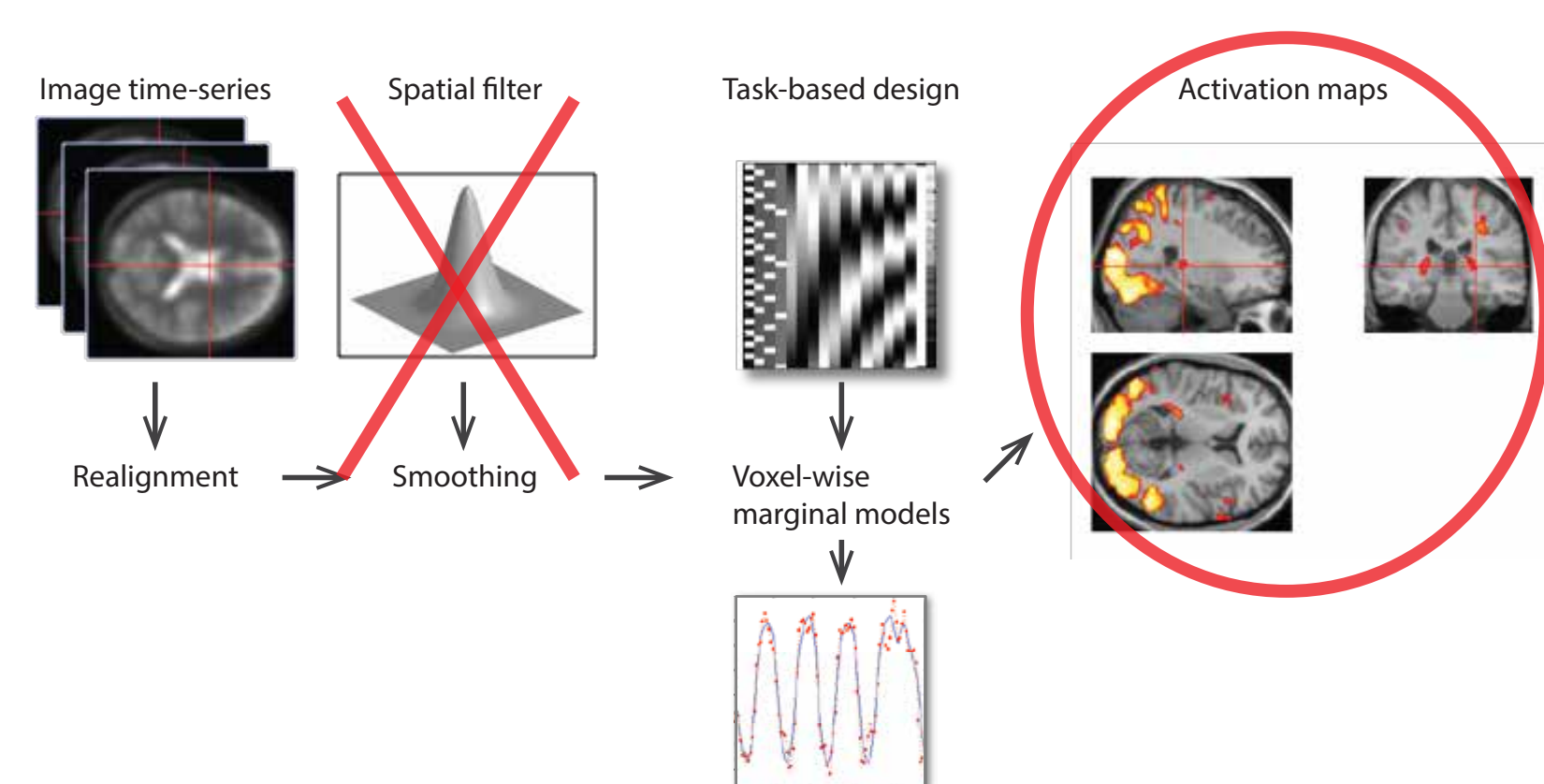


Fig 2: Typical fMRI pipeline. We received and used unsmoothed z -statistic maps as data, treating these as noisy summaries of spatial activation

Proposed Model for Dual-Resolution fMRI

$$y_h(\mathbf{v}_h) \sim \mathcal{N}(\mu(\mathbf{v}_h), \sigma_h^2) \quad y_s(\mathbf{v}_s) \sim \mathcal{N}(\mu(\mathbf{v}_s), \sigma_s^2)$$

$$\pi(\sigma_h^2, \sigma_s^2) \propto \sigma_h^{-2} \sigma_s^{-2} \mathbf{1}(\sigma_h^{-2} < \sigma_s^{-2})$$

(h —high and s —standard resolution)

$$\mu(\mathbf{v}) \sim \mathcal{GP}(0, K) \quad K(\mathbf{v}, \mathbf{v}') = \tau^2 \exp(-\psi \|\mathbf{v} - \mathbf{v}'\|^\nu), \quad \tau^2, \psi > 0; \nu \in (0, 2]$$

- Correlation between voxels and images induced by Gaussian Process prior on $\mu(\cdot)$
- Covariance parameters estimated via minimum contrast

- Assume different images \mathbf{y}_h and \mathbf{y}_s are realizations of the same spatial activation process
- Independent noise: no smoothing during preprocessing

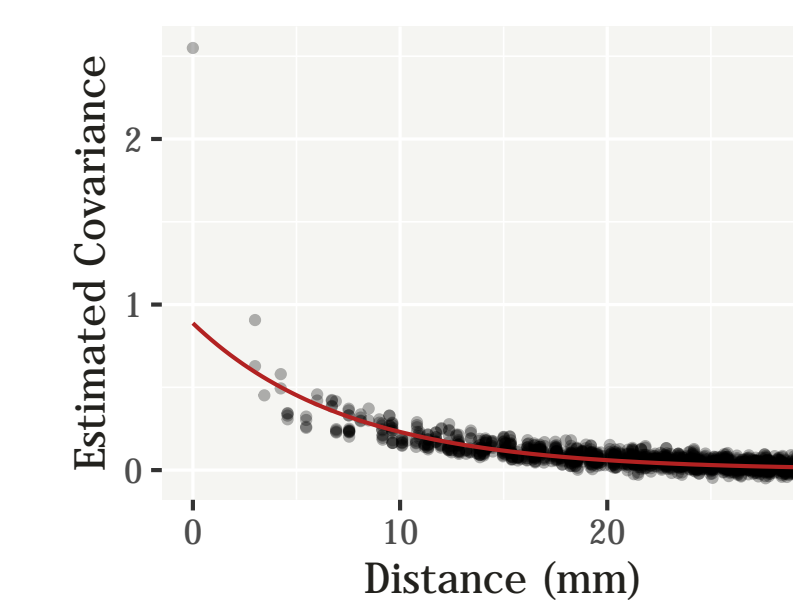
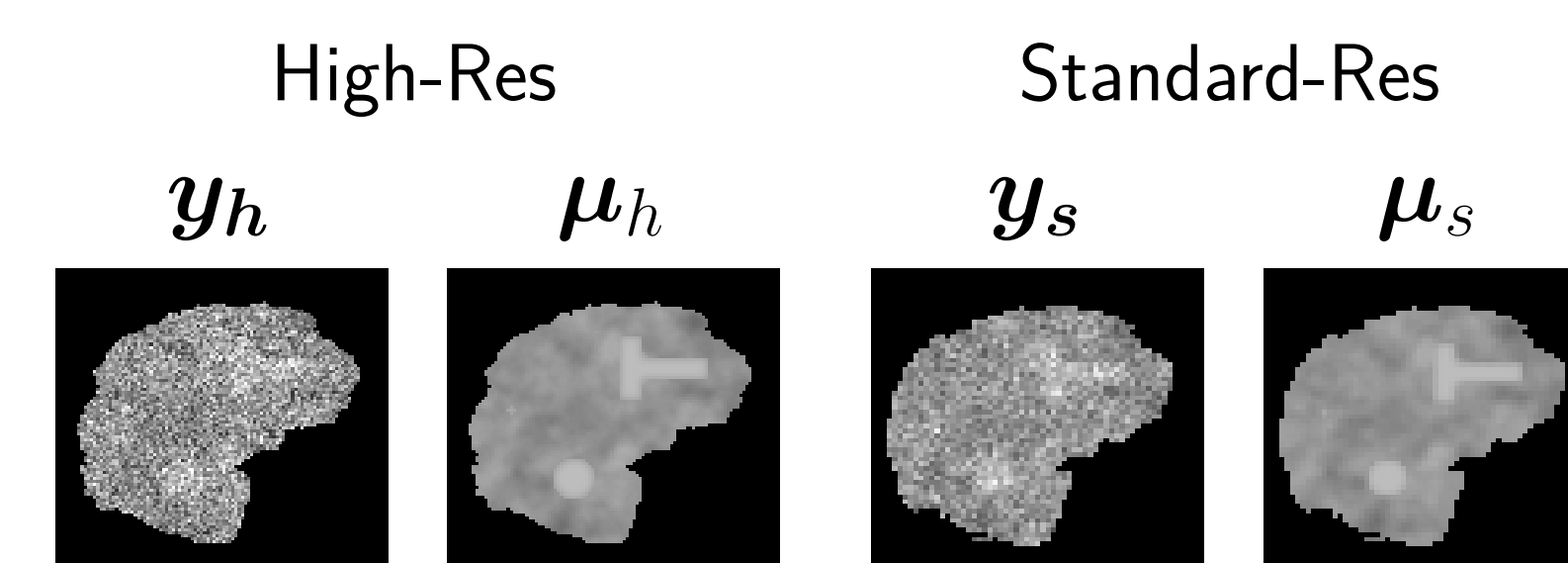


Fig 3: Empirical covariogram and fitted curve with exponential correlation function

Illustrative Example: Embedded Signal in 2D Slices



- Compare with single resolution methods
- **Naive** data combination: $\bar{\mathbf{y}}_{hs} = (\mathbf{y}_h + \mathbf{W}^\top \mathbf{y}_s)/2$
(Where $\mathbf{W}^\top \mathbf{y}_s$ is an ordinary kriging interpolation of \mathbf{y}_s)

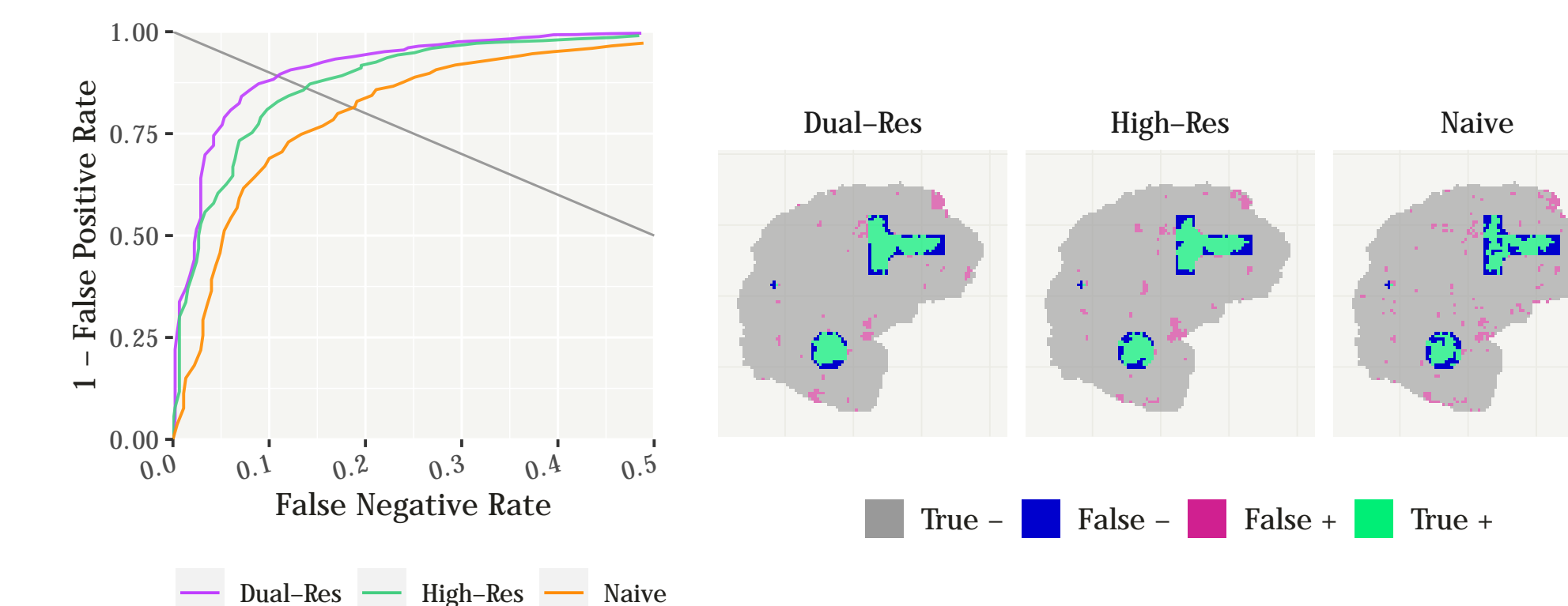


Fig 4: (Left) ROC curves show proposed method's improvement over single resolution methods. (Right) Panels show example inferential errors

Patient Data Analysis

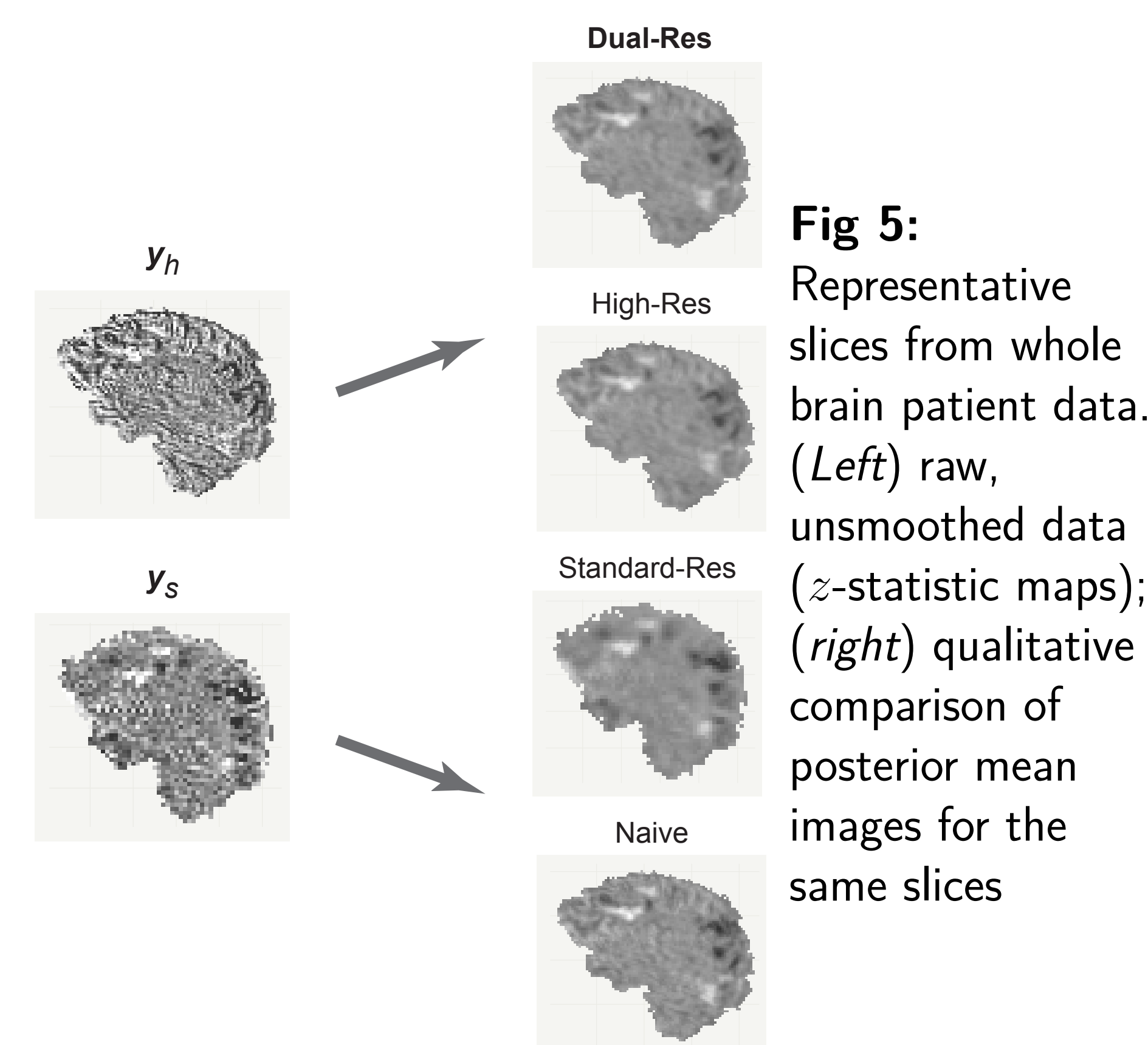


Fig 5: Representative slices from whole brain patient data. (Left) raw, unsmoothed data (z -statistic maps); (right) qualitative comparison of posterior mean images for the same slices

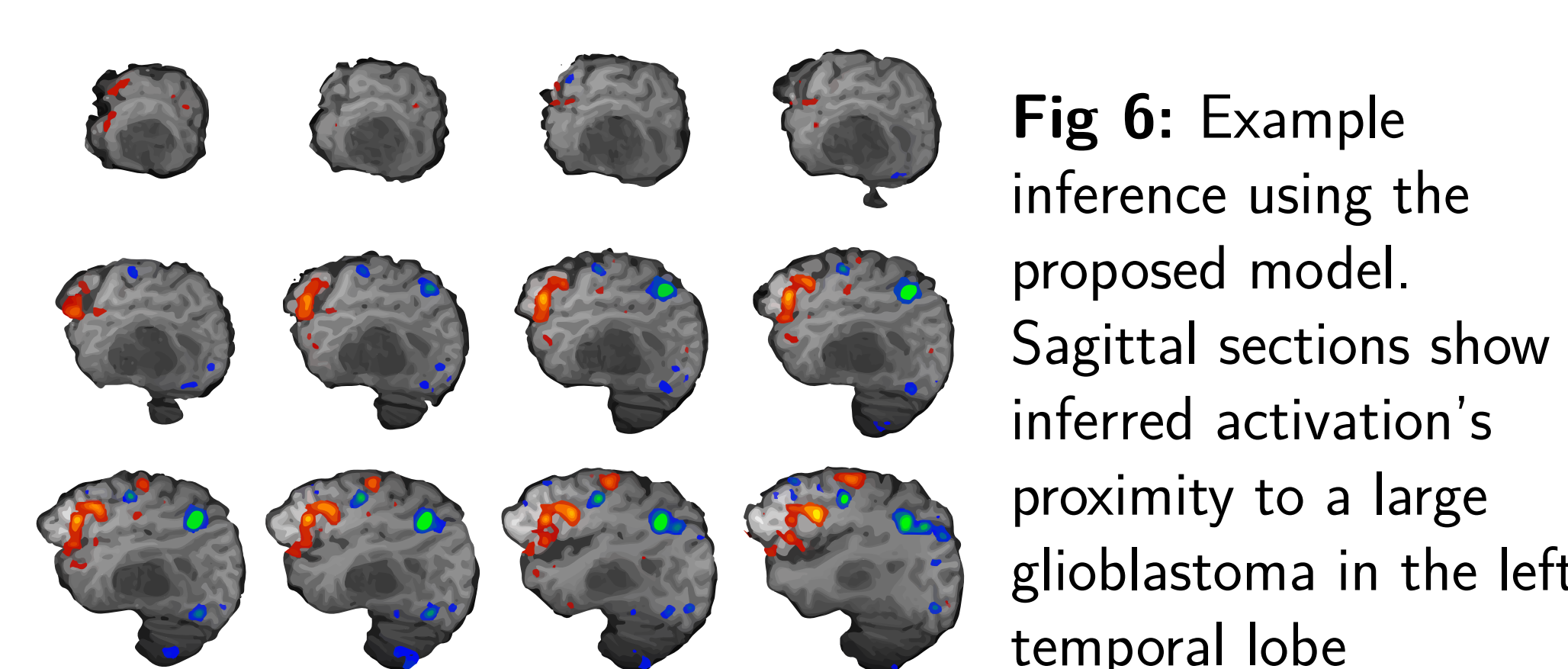


Fig 6: Example inference using the proposed model. Sagittal sections show inferred activation's proximity to a large glioblastoma in the left temporal lobe

Scanning Session Description

- Patient scanned while performing a word reading task (30 sec on/off block design)
- Two resolutions collected over separate sessions (High-Res: $120 \times 120 \times 62$ grid size; Std-Res: $64 \times 64 \times 48$ grid size)
- Siemens 3 T scanner; 32 channel head coil

Posterior Inference

- Sampling via Riemann manifold HMC [2]
- Sparse approximation with high resolution voxel locations used as the “inducing set” to maximize spatial precision

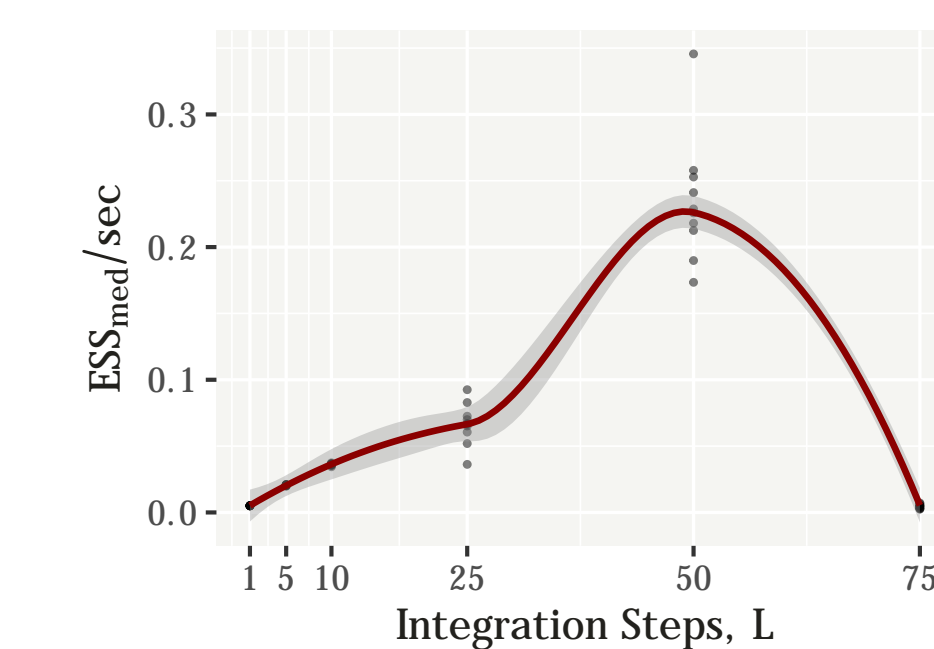


Fig 7: Computation time in analysis of real patient data. ESS_{med} denotes median effective sample size across all voxels

- Differently penalize false negative and false positive errors. Adapted from [4, 3]

$$L(\mathbf{m}, \mathbf{d}) = \sum_i \frac{-f(m_i)d_i - [1 - f(m_i)](1 - d_i)}{\underbrace{\text{Gains for correct decisions}}_{+k_1 f(m_i)(1 - d_i) + k_2 [1 - f(m_i)]d_i} + \underbrace{\text{Penalties for false } -/+}_{td_i}}$$

- k_1, k_2, t tunable parameters, e.g. t penalizes the overall number of discoveries
- $m_i = |\mathbb{E}(\mu_{hi} | \mathbf{y}_h, \mathbf{y}_s)| / \sqrt{\text{var}(\mu_{hi} | \mathbf{y}_h, \mathbf{y}_s)}$
- $f(\cdot)$ some monotone function of signal strength: e.g. $f(m_i) = m_i / \max_i m_i$
 - Proxy measure for $\pi(\text{“voxel } i \text{ is active”} | \mathbf{y}_h, \mathbf{y}_s)$
- Collaborating radiologist's advice: penalize false negatives $11 \times$ more heavily than false positives

References

- [1] Belliveau, JW et al. *Science* 254.5032 (1991), pp. 716–719.
- [2] Girolami, Mark and Calderhead, Ben. *JRSSB* 73.2 (2011), pp. 123–214.
- [3] Liu, Zhuqing et al. *Bayesian Analysis* 11.2 (2016), p. 599.
- [4] Muller, Peter, Parmigiani, Giovanni, and Rice, Kenneth. (2006).

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