



Assignment Cover Page

Name of the student :- Anjaly Jins

PRN ..V.M.I22.CS.045

Admission No....S104

Subject Name :- Soft Computing

Subject Code:- CST 444

Assignment Title/No : 1

Name of the faculty: Ashwathy TV miss

Assignment Submitted on 23/02/26.

Late submission rules : Max mark will reduced to 50% for 1-5 working day's delay, no mark will be awarded thereafter.

I am hereby confirming that this assignment is my own and I haven't adopted any unfair means in any steps of its preparation to enhance my performance in this assignment.

Date : 23/02/26

Anjaly Jins

Sign with Name


Assignment subdivision	Maximum Mark	Marks awarded	Remarks
A			
B			
C			

Feed back/suggestions :

Name and sign of the faculty

①

2. a) Using the Hebb rule find the weights required to perform the following classification: given that the vectors $(1, 1, 1, 1)$ and $(1, 1, 1, -1)$ are members of same class (target +1) and vectors $(1, 1, 1, -1)$ and $(1, -1, -1, 1)$ are not members of the class (target -1).
- b) Implement the following logical function using the M-D. Neuron. Use binary data representation:
- 1) AND
 - 2) OR
 - 3) XOR

Ans. step 1: list Inputs and Targets

vector	Input x	Target t
1	$(1, 1, 1, 1)$	+1
2	$(1, 1, 1, -1)$	+1
3	$(1, 1, 1, -1)$	-1
4	$(1, -1, -1, 1)$	-1

$$\Rightarrow \omega = (0, 0, 0, 0)$$

$$\begin{aligned} \text{1) } \omega &= \omega + 1D(1, 1, 1, 1) \\ &= (1, 1, 1, 1) \end{aligned}$$

$$\begin{aligned} \text{2) } \omega &= \omega + (-1)D(-1, 1, -1, -1) \\ &= (0, 2, 0, 0) \end{aligned}$$

$$\begin{aligned} \text{3) } \omega &= \omega + (-1)D(1, 1, 0, 1) \\ &= (-1, 1, -1, 1) \end{aligned}$$

$$\begin{aligned} \text{4) } \omega &= \omega + (-1)D(1, -1, -1, 1) \\ \text{Final weight} &= (-2, 2, 0, 0) \end{aligned}$$

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b) D AND

x_1	x_2	y
0	1	1
1	0	0
0	1	0
0	0	1

$$\textcircled{a} \quad y_{in} = x_1 w_1 + x_2 w_2$$

Assume $w_1=1, w_2=1$

$$\Rightarrow (0,0) \quad y_{in} = 0 \cdot 1 + 0 \cdot 1 = 0$$

$$\Rightarrow (0,1) \quad y_{in} = 0 \cdot 1 + 1 \cdot 1 = 1$$

$$\cancel{\Rightarrow (1,0)} \quad y_{in} = (1 \cdot 0) + 0 \cdot 1 = 1$$

$$\Rightarrow (1,1) \quad y_{in} = 1 \cdot 1 + 1 \cdot 1 = \underline{\underline{2}}$$

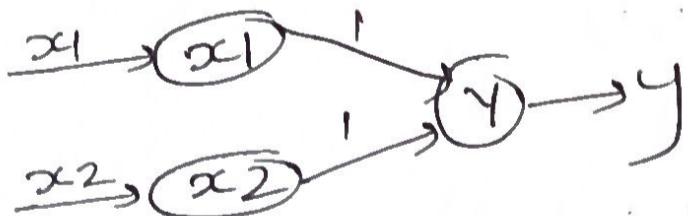
$$\theta \geq \text{max}(y_{in}) - P$$

$$n=2$$

$$w=1$$

$$P=0$$

$$\text{So } \theta = \text{max}(y_{in}) - P = 2 + 1 - 0 \\ = \underline{\underline{2}}$$



$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 0 \\ 0 & \text{if } y_{in} < 0 \end{cases}$$

2) OR

x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	1

$$w_1=w_2=1$$

(2)

$$(0,0) \Rightarrow V_{in} = x_1 w_1 + x_2 w_2 = 0x1 + 0x1 = 0$$

$$(0,1) \Rightarrow V_{in} = x_1 w_1 + x_2 w_2 = 0x1 + 1x1 = 1$$

$$(1,0) \Rightarrow V_{in} = x_1 w_1 + x_2 w_2 = 1x1 + 0x1 = 1$$

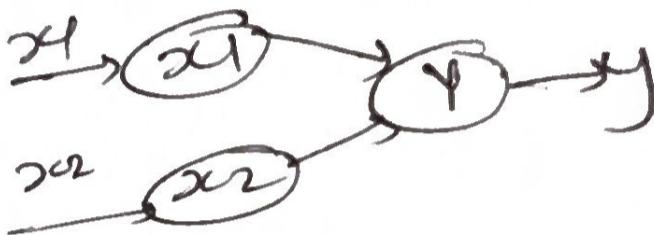
$$(1,1) \Rightarrow V_{in} = x_1 w_1 + x_2 w_2 = 1x1 + 1x1 = 2$$

$$y = f(V_{in}) = \begin{cases} 1 & \text{if } V_{in} \geq 0 \\ 0 & \text{if } V_{in} < 0 \end{cases}$$

$$= \begin{cases} 1 & \text{if } y_{in} \geq 1 \\ 0 & \text{if } y_{in} < 0 \end{cases} \quad n =$$

$$\theta = nw - p$$

$$\approx 1$$



③ XOR

x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	0

$$y = x_1 \bar{x}_2 + \bar{x}_1 x_2$$

$$y = z_1 + z_2$$

$$\text{where } x_1 \bar{x}_2 = z_1$$

$$z_2 = \bar{x}_1 x_2$$

Case 1:
Assume $w_1 = 1, w_2 = -1$

$$(0,0) \Rightarrow z_1 = 0x1 + 0x1 = 0$$

$$(0,1) \Rightarrow z_1 = 0x1 + 1x1 = 1$$

$$(1,0) \Rightarrow z_2 = 1x1 + 0x1 = 1$$

$$(1,1) \Rightarrow z_1 = 1x1 + 1x1 = 2$$

Case 2:

Assume $w_1 = 1, w_2 = -1$

$$(0,0) \Rightarrow z_1 = 0x1 + 0x1 = 0$$

$$(0,1) \Rightarrow z_1 = 0x1 + 1x1 = -1$$

$$(1,0) \Rightarrow z_1 = 1x0 + 0x1 = 0$$

$$(1,1) \Rightarrow z_1 = 1x1 + 1x1 = 0$$

So for z_1 ; $w_1 = 1, w_2 = -1, b \geq 1$

$$z_2 = \bar{x}_1 x_2$$

x_1	x_2	z_2
0	0	0
0	1	1
1	0	0
1	1	0

Case 1: Assume $w_1 = 1 = w_2$

$$(0,0) = z_2 = 0x1 + 0x1 = 0$$

$$(1,0) = z_2 = 0x0 + 0x1 = 0$$

$$(0,1) = z_2 = 0x1 + 1x1 = 1$$

$$(1,1) = z_2 = 1x1 + 1x1 = 2$$

These 3 cases are not possible.

Case 2: $w_2 = -1$ $w_1 = 1$

$$(0,0) = z_2 = 0x1 + 0x1 = 0$$

$$(0,1) = z_2 = 0x1 + 1x1 = 1$$

$$(1,0) = z_2 = 1x1 + 0x1 = -1$$

$$(1,1) = z_2 = 1x1 + 1x1 = 0$$

Thus based on this calculated, possible in

$$\begin{aligned} w_1 &= 1 \\ w_2 &= -1 \quad 0 \geq 1 \text{ for } z_2 \text{ neuron} \end{aligned}$$

$$\Rightarrow y = z_1 \text{ OR } z_2$$

x_1	x_2	y	z_1	z_2
0	0	0	0	0
0	1	0	0	1
1	0	1	1	0
1	1	0	0	0

Score the net input is calculated using

$$y = z_1 v_1 + z_2 v_2$$

$$\Rightarrow w_{11} = w_{22} = 1 \text{ (excitatory)}$$

$$w_{12} = w_{21} = -1 \text{ (inhibitory)}$$

$$\text{and } v_1 = v_2 = 1 \text{ (excitatory)}$$

Case 1: Assume both weights as excitatory i.e;

$$v_1 = v_2 = 1$$

Now

$$(0,0) y_{in} = 0x1 + 0x1 = 0$$

$$(0,1) y_{in} = 0x1 + 1x1 = 1$$

$$(1,0) y_{in} = 1x1 + 0x1 = 1$$

$$(1,1) y_{in} = 1x1 + 1x1 = 2$$

