$$p(y_{1:N}, \mathbf{x}_{1:N}) = \prod_{n=1}^{N} g(y_n | \mathbf{x}_{1:n}) f(\mathbf{x}_n | \mathbf{x}_{1:n-1})$$