$$p(\mathbf{x}_{1:N}|y_{1:N}) \approx \sum_{\ell=1}^{L} w_N^{\ell} \delta_{\mathbf{x}_{1:N}^{\ell}}(\mathbf{x}_{1:N})$$