$$\tilde{\mathbf{x}}_n^k | \tilde{\mathbf{x}}_{1:n-1}^{a_{n-1}^k} \sim p(\tilde{\mathbf{x}}_n | \tilde{\mathbf{x}}_{1:n-1}^{a_{n-1}^k})$$