$$w(\tilde{\mathbf{x}}_{1:n}^k) = p(y_n|\tilde{\mathbf{x}}_{1:n}^k) = g_n^k(y_n|\tilde{\mathbf{x}}_{1:n}^k)$$