$oldsymbol{ au}_{complex}$