PHYS 7326: Running Homework and Take-Home Exams

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We are trying something different this semester for the students that wanted more regular homework assignments. Work will still be due biweekly, but problems will be posted on a rolling basis as lectures are developed and given. It is also more natural for me, as assignment ideas come on a rolling basis.

Instructions: Due dates will be listed throughout the document in bold letters. For the first assignment, complete all problems by the first due date. For the nth assignment, complete all problems between the $(n-1)^{\text{th}}$ and n^{th} due date. Two due dates will have the words "TAKE-HOME" on the same line. The first is the take-home midterm, and the second the take-home final. These are your work alone.

I will also organize according to topic.

1   Non-abelian Gauge Theory

- 2 pts. Prove Schwartz equation (25.11).

- 3 pts. Non-abelian gauge invariance. Schwartz problem 25.1.

- 5 pts. Non-abelian gauge invariance. Consider the Lagrangian

$$\mathcal{L} = -\frac{1}{4}F^a_{\mu\nu}F^{\mu\nu a} + A^{abcd}A^a_\mu A^{\mu a}A^c_\nu A^{\nu c} + B^{abc}\partial_\mu A^{\mu a}A^b_\nu A^{\nu c} + C^{abc}\partial_\mu A^a_\nu A^{\mu b}A^{\nu c} \tag{1}$$

and the gauge transformation

$$A^a_\mu \mapsto A^a_\mu + \frac{1}{g_a}\partial_\mu \alpha^a + T^{ab}A^b_\mu. \tag{2}$$

By $F^a_{\mu\nu}$, where we mean the usual thing $F^a_{\mu\nu} = (\partial_\mu A^a_\nu - \partial_\nu A^a_\mu)$, rather than the non-abelian field strength. The latter comes naturally out of this calculation and will involve the interaction terms.

  - Compute the transformation of each term appearing in the Lagrangian.
  - From the transformed Lagrangian, compute conditions that must be satisfied for the Lagrangian to be gauge invariant. Hint: collecting terms with the same number of derivatives and vector fields is useful.
  - Determine whether or not the solution presented in class

  $$g_a = g_b =: g \ \forall a,b \qquad T^{ab} = -f^{abc}\alpha^b A^c_\mu \qquad C^{abc} = -gf^{abc} \qquad A^{abcd} = g^2 f^{kac}f^{kbd} \qquad B^{abc} = 0 \tag{3}$$

  is the only solution.

- 5 pts. Anomaly coefficients. Schwartz problem 25.4.

HOMEWORK 1. Due February 1.