

Problem

Please see the screenshots from the textbook (in order) The input format explains the modifications in the question (if any). In case of any doubt, please contact the TAs.

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Introduction

Simulation is a powerful technique for solving a wide variety of problems. To simulate is to copy the behaviour of a system or phenomenon under study. Strictly speaking, we will be dealing with only *numerical sequential simulation*; numerical because there are other forms of simulation—for example, electrical analogue or physical simulation; and sequential because the calculations proceed in a time sequence. Some of the basic ideas in simulation can be best understood by performing actual simulations. Let us, therefore, consider the following two very simple examples and see how simulation is actually done.

1-1. Simulation of a pure pursuit problem—an example

A fighter aircraft sights an enemy bomber and flies directly toward it, in order to catch up with the bomber and destroy it. The bomber (the target) continues flying (along a specified curve) so the fighter (the pursuer) has to change its direction to keep pointed toward the target. We are interested in determining the attack course of the fighter and in knowing how long it would take for it to catch up with the bomber.

If the target flies along a straight line, the problem can be solved directly with analytic techniques. (The proof of such a closed-form expression which gives the course of the pursuer, when the target flies in a straight line, is left as an exercise for you. Problem 1-2.)

However, if the path of the target is curved, the problem is much more difficult and normally cannot be solved directly. We will use simulation to solve this problem, under the following simplifying conditions:

1. The target and the pursuer are flying in the same horizontal plane when the fighter first sights the bomber, and both stay in that plane. This makes the pursuit model two-dimensional.
2. The fighter's speed VF is constant (20 kms/minute).
3. The target's path (i.e., its position as a function of time) is specified.
4. After a fixed time span Δt (every minute, in this case) the fighter changes its direction in order to point itself toward the bomber.

Let us introduce a rectangular coordinate system coincident with the horizontal plane in which the two aircraft are flying. We choose the point due south of the fighter and due west of the target (at the beginning of the pursuit) as the origin of this coordinate system. Let the distances be given

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in kilometers and the time in minutes. We start measuring the time when the fighter first sights the bomber. (See Fig. 1-1.)

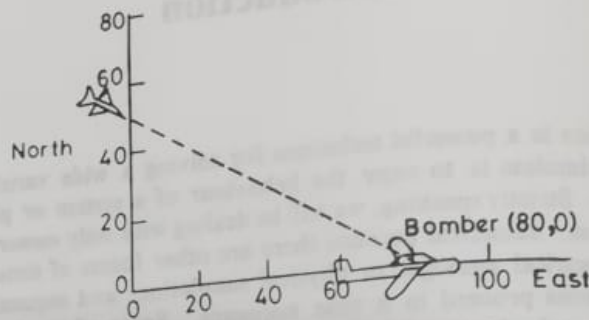


Fig. 1-1: Positions of Pursuer and Target at Time Zero.

We will represent the path of the bomber (which is known to us in advance) by two arrays, the east coordinates and the north coordinates at specified moments (each minute). We call these coordinates $XB(t)$ and $YB(t)$, respectively. They are presented in the form of a table (in kilometers) below.

Time, t	0	1	2	3	4	5	6	7	8	9	10	11	12
$XB(t)$	80	90	99	108	116	125	133	141	151	160	169	179	180
$YB(t)$	0	-2	-5	-9	-15	-18	-23	-29	-28	-25	-21	-20	-17

Table 1-1.

Likewise, we will represent the path of the fighter plane by two arrays $XF(t)$ and $YF(t)$. In this example, initially we are given

$$YF(0) = 50 \text{ kms}, \quad XF(0) = 0 \text{ kms}.$$

Our purpose is to compute the positions of the pursuer, namely, $XF(t)$, $YF(t)$ for $t = 1, 2, \dots, 12$, or until the fighter catches up with the bomber. We will assume that once the fighter is within 10 kms of the bomber, the fighter shoots down its target by firing a missile, and the pursuit is over. In case the target is not caught up within 12 minutes, the pursuit is abandoned, and the target is considered escaped. From the time $t = 0$ till the target is shot down, the attack course is determined as follows:

The fighter uses the following simple strategy: It looks at the target at instant t , aligns its velocity vector with the line of sight (i.e., points itself toward the target). It continues to fly in that direction for one minute,

till instant $(t + 1)$. At time $(t + 1)$ it looks at the target again and realigns itself.

Input Format

The first line tells the number of seconds to pursue before giving up, say n . The second line contains two numbers telling the initial position of the pursuer in a 2D cartesian plane. Now the input will contain $(n+1)$ lines to tell the position of the bomber at the end of n th second, starting from initial position (index 0). Each line has a pair of numbers telling the bomber's position on the same plane.

Constraints

None

Output Format

The output consists of two lines. The first line tells the minute when the bomber was shot down. In case of pursuit being called off, this number will be -1. The second line yells the distance when the pursuit ends (either after shooting down or calling it off).

Sample Input 0

```
12
0 50
80 0
90 -2
99 -5
108 -9
116 -15
125 -18
133 -23
141 -29
151 -28
160 -25
169 -21
179 -20
180 -17
```

Sample Output 0

```
10  
2.96
```

Explanation 0

The bomber starts from (80, 0) and the pursuer starts from (0, 50). The pursuer has a constant speed of 20km/min and rest details are as per question (see images).

The output can be read as

"The bomber was caught after 10 minutes and was shot from a distance of 2.96 kilometers (rounded off to 2 decimal places)."

