

Minimize  $\lambda x^T M x - \mu^T x$

- (1) Function 1: Generate initial feasible solution randomly
- (2) Function 2: Give  $+x$ . Function 3 and 4 are required.
- (3) Function 3: Give  $y$  (this function is unfinished in my code)

$$g = \nabla F = 2\lambda Mx - \mu$$

rearrange  $g$ , try different  $m$ , get  $y$

- (4) Function 4: Give  $s$

$$\Delta F = \lambda s^2 y^T M y - 2\lambda s x^T M y - \mu^T s y$$

$$s = -\frac{(2\lambda x^T M y - \mu^T y)}{2\lambda y^T M y}$$

$0 < s < 1$  must hold

If  $s < 0$ , then computation is wrong.

- (5) Give break condition

The  $\Delta x$  is too small; or  $\Delta F$  is too small;

Minimize  $\lambda x^T M x - \mu^T x$  with PCA

- (1) Function 1: Generate initial feasible solution randomly
- (2) Function 2: Give  $+x$ . Function 3 and 4 are required.
- (3) Function 3: Give  $y$

$$g = \nabla F = 2\lambda Mx - \mu$$

rearrange  $g$ , try different  $m$ , get  $y$ .

if  $y=0$  or  $y$  is small enough then break

$$\text{PCA CASE: } g = \nabla F = 2\lambda V C V x - \mu$$

- (4) Function 4: Give  $s$

$$\Delta F = \lambda s^2 y^T M y - 2\lambda s x^T M y - \mu^T s y$$

$$s = -\frac{(2\lambda x^T M y - \mu^T y)}{2\lambda y^T M y}$$

$0 < s < 1$  must hold

If  $s < 0$ , then computation is wrong.

if  $s$  is small enough, then break.

$$\text{PCA CASE } s = -\frac{(2\lambda x^T V C V y - \mu^T y)}{2\lambda y^T V C V y}$$

- (5) Give break condition

The  $\Delta x$  is too small; or  $\Delta F$  is too small;