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## 4. Linear Support Vector Machines

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Homework due Feb 22, 2023 08:59 -03 Past due

In this problem, we will investigate minimizing the training objective for a Support Vector Machine (with margin loss).

The training objective for the Support Vector Machine (with margin loss) can be seen as a balance between the average hinge loss over the examples and a regularization term that tries to keep the weight vector small (increase the margin). This balance is set by the regularization parameter  $\lambda > 0$ . We will consider the case without the offset parameter  $\theta_0$  (setting it to zero) so that the training objective is

$$\left[ \frac{1}{n} \sum_{i=1}^n \text{Loss}_h(y^{(i)} \theta \cdot x^{(i)}) \right] + \frac{\lambda}{2} \|\theta\|^2 = \frac{1}{n} \sum_{i=1}^n \left[ \text{Loss}_h(y^{(i)} \theta \cdot x^{(i)}) + \frac{\lambda}{2} \|\theta\|^2 \right]$$

where the hinge loss is given by

$$\text{Loss}_h(y(\theta \cdot x)) = \max\{0, 1 - y(\theta \cdot x)\}$$

$$\hat{\theta} = \text{Argmin}_{\theta} [\text{Loss}_h(y \theta \cdot x) + \frac{\lambda}{2} \|\theta\|^2]$$

**Note:** For all of the exercises on this page, assume that the training set has just  $n = 1$  example,  $x = x^{(1)}$  and  $y = y^{(1)}$  as shorthand.

**Note :** Remember also that by convention in this Unit we regard every datapoint on the boundary as misclassified.

## Minimizing Loss - Case 1

1 point possible (graded)

In this question, suppose that  $\text{Loss}_h(y(\hat{\theta} \cdot x)) > 0$ . That is, the optimal weight vector  $\hat{\theta}$  is such that the training example is misclassified. Under this hypothesis, solve the optimisation problem and express the optimal value in terms of  $\lambda$ .

Let  $w_1$  and  $w_2$ , where  $w_1$  and  $w_2$  are the first and second components of  $w$  respectively.

Solve for  $w$ .

**Hint:** For the above example, show that

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## Minimizing Loss - Numerical Example (2)

1 point possible (graded)

Now, let  $w^*$  be the solution as a function of  $x$ .

There exists exactly one number  $x^*$  such that whenever  $x < x^*$ , then no matter what the optimal weight  $w^*$  will misclassify the training example. What is  $x^*$ ?

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## Discussion



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<a href="#">✔ Numerical example 1 - does it say anywhere that the components of theta must be integers?</a>	<a href="#">Question in title</a>
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