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5. Policy and Value Functions

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Exercises due May 3, 2023 08:59 -03 Completed

Policy and Value Functions



Video

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Transcripts

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Definition of Optimal Policy

1/1 point (graded)

Given an MDP, and a utility function $U[s_0, s_1, \dots, s_n]$, our goal is to find an optimal policy that maximizes the expectation of the utility. Here, a **policy** is a function $\pi : \mathcal{S} \rightarrow \mathcal{A}$ that takes any state s . We denote the optimal policy by π^* .

Which of the following option is correct about the optimal policy function?

☐ The optimal policy function would only depend on the state and action space but not on the reward structure.

☒ The optimal policy assigns an action at every state that maximizes the expected utility.

☐ For any given state, the optimal policy function should always take an action that maximizes the expected utility.

		-1
		Agent's starting state

Recall the MDP example in the lecture. An AI agent navigates in the 3×3 grid depicted above. The top right square is not accessible (and hence is greyed out).

The MDP is defined as follows. As before, every state is defined by the current position in the grid. The actions are the 4 directions "up", "down", "left", "right".

Now, The transition probabilities from state via action to state is given by

Reward structure:

As before, the agent receives a reward of 1 for arriving at the top right cell, and a reward of -1 for the cell immediately below it. It does not receive any non-zero reward at the other cells. The following figure.

However, this time, the agent also receives a reward (or penalty) of -0.1 for every action taken. For any action that leads the agent into the top or bottom cells.

Transition Probabilities:

For simplicity, assume that all the transitions are deterministic. That is, given any state and action, the next state reached is completely predictable.

For instance, taking the action "left" from the bottom right cell will always take the agent to its left. Any action pointing off the grid would lead the agent to remain in its current cell.

Initial State:

Also, assume that the agent always starts off from the bottom right corner of the grid. It takes an action until it reaches the top right corner, at which point it stops and does not act any more.

Optimal policy - Numerical Example

2/2 points (graded)

Recall that in this setup, the agent receives a reward (or penalty) of 1 for every action taken. For the top and bottom cells when it reached the corresponding cells. Since the agent always starts from the bottom right corner, the outcome of each action is deterministic, the discounted reward depends only on the action taken. It can be written as:

Maximum discounted reward: 

You have used 1 of 3 attempts

Value Function

0/1 point (graded)

As above, we are working with the grid example with reward at the top right cell below it. The agent also gets a reward of for every action that it takes. The action is deterministic. The agent continues to act until it reaches the cell, when it stops.

The following figures show states in which the letter "A" marks the current location of the agent.

		+1
		-1
		A

 s_1

A		+1
		-1

 s_2

		+1
		-1
A		

 s_3

A **value function** of a given state is the expected reward (i.e the expectation of the reward) if the agent acts optimally starting at state . In the given MDP, since the action outcome is deterministic, the expected reward simply equals the utility function.

Which of the following should hold true for a good value function under the reward function of the given MDP?

Note: You may want to watch the video on the next page before submitting this question.



	<u>I believe that the equation in the second part is not mathematically correct. Why does the left side depend</u>
?	<u>Value Function - is gamma assumed to be 1 in the last question?</u> <u>* didn't see gamma in the answer for that question</u>
?	<u>[STAFF] - Optimal policy - Numerical Example - last step</u> <u>This is a critical for my understanding. Why we do not count last step as $\gamma^2 R(s_2, a_3)$, $a_3=0$????? If</u>
💬	<u>Better example needed</u> <u>The study example needs to be refined or even better replaced with a more intuitive one. It is not a good one</u>
?	<u>Formal definition of R for the numerical problem</u> <u>How does one define R? The description doesn't really define it formally. Specifically, does the $R(s(n), a(n+1))$</u>
💬	<u>s_0</u>
💬	<u>awful notation and word choice</u>
?	<u>Optimal policy - ambiguity in question</u> <u>The question clearly states: "For the cases $(\gamma=0)$ and $(\gamma=0.5)$, what is the maximum discounted r</u>
?	<u>Confusion about what step the +1/-1 rewards apply</u> <u>Based on the discounted rewards function, I am not clear at which term the destination rewards of +1 and -1</u>
?	<u>Answer for $\gamma = 0.5$ does not seem correct</u> <u>The answer for $\gamma = 0.5$ does not seem correct, as it didn't factor in $R(s_2, a_3)$.</u>

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