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## 6. Perceptron Updates

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Homework due Feb 22, 2023 08:59 -03 Past due

In this problem, we will try to understand the convergence of perceptron algorithm and ordering of the training samples for the following simple example.

Consider a set of  $n = d$  labeled  $d$ -dimensional feature vectors,  $\{(x^{(t)}, y^{(t)})\}, t = 1, \dots, n$ , follows:

$$x_i^{(t)} = \cos(\pi t) \quad \text{if } i = t$$

$$x_i^{(t)} = 0 \quad \text{otherwise,}$$

Recall the no-offset perceptron algorithm, and assume that  $\theta \cdot x = 0$  is treated as a margin label. Assume that in all of the following problems, we initialize  $\theta = 0$  and when we refer to the perceptron algorithm we only consider the no-offset variant of it.

## Working out Perceptron Algorithm

3 points possible (graded)

Consider the  $d = 2$  case. Let  $y^{(1)} = 1, y^{(2)} = -1$ . Assume that the feature vector  $x^{(1)}$  is used by the perceptron algorithm before  $x^{(2)}$ .

For this particular assignment of labels, work out the perceptron algorithm until convergence.

Let  $\hat{\theta}$  be the resulting  $\theta$  value after convergence. Note that for  $d = 2$ ,  $\hat{\theta}$  would be a two-dimensional vector. Let's denote the first and second components of  $\hat{\theta}$  by  $\hat{\theta}_1$  and  $\hat{\theta}_2$  respectively.

Please enter the total number of updates made to  $\theta$  by perceptron algorithm:

Please enter the numerical value of  $\hat{\theta}_1$ :

Please enter the numerical value of  $\hat{\theta}_2$ :

- ☐ Perceptron algorithm will make at least updates to with the exact number of the ordering of the feature vectors presented to it and their labeling
- ☐ Perceptron algorithm will make at most updates to with the exact number of the ordering of the feature vectors presented to it and their labeling

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You have used 0 of 3 attempts

## Sketching convergence

1 point possible (graded)

Consider the case with . Also assume that all the feature vectors are positively labeled. Let  $P$  be the plane through the three points in a 3-d space whose vector representations are given by  $\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3$ .

Let  $w$  denote the value of  $w$  after perceptron algorithm converges for this example. Let  $\mathbf{w}$  be the vector connecting the origin and  $\mathbf{w}$ . Which of the following options is true regarding the vector  $\mathbf{w}$ ?

- ☐  $\mathbf{w}$  is parallel to the plane
- ☐  $\mathbf{w}$  is perpendicular to the plane and pointing towards it

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[💬 Working out Perceptron Algorithm](#)

[Should clarify that  \$x\_i^{\(d\)}\$  is  \$\[x\_1, x\_2, \dots, x\_d\]^{\(d\)}\$  vector. When I saw "i" I thought that was the "i" of the perce](#)

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