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5. Planes

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Homework0 due Feb 8, 2023 08:59 -03 Completed

A hyperplane in n dimensions is a $n - 1$ dimensional subspace. For instance, a hyperplane in 2-dimensional space can be any line in that space and a hyperplane in 3-dimensional space can be any plane. A hyperplane separates a space into two sides.

In general, a hyperplane in n -dimensional space can be written as $\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n = 0$. For example, a hyperplane in two dimensions, which is a line, can be expressed as $Ax_1 + Bx_2 = C$.

Using this representation of a plane, we can define a plane given an n -dimensional vector θ and a scalar offset θ_0 .

This vector and offset combination would define the plane $\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n = 0$. One feature of this representation is that the vector θ is normal to the plane.

Number of Representations

1/1 point (graded)

Given a d -dimensional vector θ and a scalar offset θ_0 which describe a hyperplane \mathcal{P} , how many alternative descriptions θ' and θ'_0 are there for this plane \mathcal{P} ?

☐ 0

☐ 1

☒ ∞



? STANDARD NOTATION

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You have used 1 of 1 attempt

Orthogonality Check

0/1 point (graded)

To check if a vector x is orthogonal to a plane \mathcal{P} characterized by θ and θ_0 , we check if $\theta \cdot x = 0$.

Perpendicular Distance to Plane

1.0/1 point (graded)

Given a point \mathbf{x} in n -dimensional space and a hyperplane described by \mathbf{a} and θ_0 find the perpendicular distance **between the hyperplane and \mathbf{x}** . This is equal to the perpendicular distance between the point \mathbf{x} and the hyperplane and is positive when \mathbf{x} is on the same side of the plane as \mathbf{a} points and negative when \mathbf{x} is on the opposite side.

(Enter **theta_0** for the offset θ_0 .)

Enter **norm(theta)** for the norm of a vector θ .

Use * to denote the dot product of two vectors, e.g. enter **v*w** for the dot product $\mathbf{v} \cdot \mathbf{w}$.)

$(\mathbf{x} \cdot \theta + \theta_0) / \text{norm}(\theta)$



? STANDARD NOTATION

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You have used 1 of 5 attempts

Orthogonal Projection onto Plane

1.0/1 point (graded)

Find an expression for the **orthogonal projection** of a point \mathbf{v} onto a plane that is characterized by \mathbf{a} and θ_0 . Write your answer in terms of \mathbf{v} , \mathbf{a} , and θ_0 .

(Enter **theta_0** for the offset θ_0 .)

Enter **norm(theta)** for the norm of a vector θ .

Use * to denote the dot product of two vectors, e.g. enter **v*w** for the dot product $\mathbf{v} \cdot \mathbf{w}$.)

$\mathbf{v} - (\mathbf{a} \cdot \mathbf{v} + \theta_0) / \text{norm}(\mathbf{a})^2 \cdot \mathbf{a}$



? STANDARD NOTATION

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You have used 2 of 5 attempts

Perpendicular Distance to Plane



Second coordinate:



? STANDARD NOTATION

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You have used 3 of 3 attempts

2. (f)

0/1 point (graded)

Consider a hyperplane in a d -dimensional space. If we project a point onto the plane, can we recover the original point from this projection?

(More precisely: is there a function from the points on the plane to points in the d -dimensional space that always exactly undoes the projection operation?)



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You have used 1 of 1 attempt

Discussion

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when trying to enter a response to "Orthogonal Projection on a plane" I am getting the following error: Invalid

💬 some hint may help you

For Orthogonal Projection onto Plane, make sure you are using the Perpendicular Distance to Plane times the

? Format of answer to Perpendicular Distance to Plane

Hi, what's the correct format to answer the 2 first questions: "What is the signed perpendicular distance..."

? Last question

Good morning, I find the last question a bit misleading. Do I have to assume that I have no more than a descr

? For Question Perpendicular Distance to Plane, What is the answer format for the last two que

For First coordinate and Second coordinate, I put my answers in a format of (X, Y) and [X, Y]. Both of these d

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