

CPSC 335 - Project 1

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Project 1

CPSC 335 - Algorithm Engineering

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Implementing algorithms

- The lawnmower algorithm
- The alternate algorithm

The lawnmower algorithm

```
192
193 // Algorithm that sorts disks using the lawnmower algorithm.
194 sorted_disks sort_lawnmower(const disk_state& before) {
195
196     unsigned count = 0; // type that it wants returned
197     disk_state place = before;
198     size_t n = before.total_count()/2; // Count of DISK_DARK and DISK_LIGHT
199
200     for(size_t j = 1; j <= ceil(n/2); j++)
201     {
202         // iterate from left to right
203         for(size_t i = 0; i < 2*n-1; i++)
204         {
205             // swap condition
206             if(place.get(i) > place.get(i+1))
207             {
208                 place.swap(i);
209                 count ++;
210             }
211         }
212         // iterate from right to left
213         for(size_t i = 2*n-1; i > 1; --i)
214         {
215             // swap condition
216             if(place.get(i) < place.get(i-1))
217             {
218                 place.swap(i-1);
219                 count ++;
220             }
221         }
222     }
223     // return the count
224     return sorted_disks(place, count);
225 }
```

The alternate algorithm

```
153
154 // Algorithm that sorts disks using the alternate algorithm.
155 sorted_disks sort_alternate(const disk_state& before) {
156     unsigned count = 0;
157     size_t n = before.total_count()/2; // total count is _colors.size();
158     disk_state place = before;
159
160     for(size_t i = 0; i < n+1; i++) // before._colors.size()+1 is same as n+1
161     {
162         // iterate through even disks
163         if(i % 2 == 0)
164         {
165             for(size_t j = 0; j <= 2*n-1; j+=2)
166             {
167                 // swap condition
168                 if(place.get(j) > place.get(j+1))
169                 {
170                     place.swap(j);
171                     count ++;
172                 }
173             }
174         }
175         // iterate through odd disks
176         else
177         {
178             for(size_t j = 1; j < 2*n-2; j+=2)
179             {
180                 // swap condition
181                 if(place.get(j) > place.get(j+1))
182                 {
183                     place.swap(j);
184                     count ++;
185                 }
186             }
187         }
188     }
189     // return count
190     return sorted_disks(place, count);
191 }
192
```

Code execution

The screenshot shows a macOS IDE window titled "disks.hpp - project-1-struggling". The editor displays the file "disks.hpp" with the following C++ code:

```
154 // Algorithm that sorts disks using the alternate algorithm.
155 sorted_disks sort_alternate(const disk_state& before) {
156     unsigned count = 0;
157     size_t n = before.total_count()/2; // total count is _colors.size();
158     disk_state place = before;
159
160     for(size_t i = 0; i < n; i++) // before._colors.size()+1 is same as n+1
161     {
162         // iterate through even disks
163         if(i % 2 == 0)
164         {
165             for(size_t j = 0; j <= 2*n-1; j+=2)
166             {
167                 // swap condition
168                 if(place.get(j) > place.get(j+1))
169                 {
170                     place.swap(j);
171                     count++;
172                 }
173             }
174         }
175         // iterate through odd disks
176         else
177         {
178             for(size_t i = 1; i <= 2*n-2; i+=2)
```

The bottom panel shows the "TERMINAL" output:

```
alitanani@MacBook-Pro project-1-struggling % make
g++ -std=c++11 -Wall disks_test.cpp -o disks_test
./disks_test
disk_state still works: passed, score 1/1
sorted_disks still works: passed, score 1/1
disk_state::is_initialized: passed, score 3/3
disk_state::is_sorted: passed, score 3/3
alternate, n=4: passed, score 1/1
alternate, n=3: passed, score 1/1
alternate, other values: passed, score 1/1
lawmower, n=4: passed, score 1/1
lawmower, n=3: passed, score 1/1
lawmower, other values: passed, score 1/1
TOTAL SCORE = 14 / 14

alitanani@MacBook-Pro project-1-struggling %
```

The status bar at the bottom indicates "Ln 157, Col 38 Spaces: 2 UTF-8 LF C++".

Pseudocode

The alternate algorithm (Pseudocode)

Set count to 0

for $i = 1$ to $n+1$ do

 if $i \bmod 2 = 0$ then do

 for $j = 0$ to $2n-1$ step 2 do

 if $\text{Disk}[j]$ is greater than $\text{Disk}[j+1]$ do

 swap ($\text{Disk}[j]$, $\text{Disk}[j+1]$)

 increment count

 end if

 end for

 end if

else

 for $j = 1$ to $2n-2$ step 2 do

 if $\text{Disk}[j]$ is greater than $\text{Disk}[j+1]$ do

 swap ($\text{Disk}[j]$, $\text{Disk}[j+1]$)

 increment count

 end if

 end for

end else

end for

return count

lawnmower algorithm (pseudocode)

```
Set count to 0
for i = 1 to ceiling of  $\frac{n}{2}$  do
  for j = 0 to  $2n-1$  do
    if Disk[j] is greater than Disk[j+1] do
      Swap(Disk[j], Disk[j+1])
      increment count
    end if
  end for
  for j =  $2n-1$  to 1 down 1 do
    if Disk[j] is less than Disk[j-1] do
      Swap(Disk[j], Disk[j-1])
      increment count
    end if
  end for
end for
return count
```

Step Count's and proof for lawnmower

lawnmower stepcount & proof

Set count to 0 //1

for i=1 to ceiling of $\frac{n}{2}$ do $\frac{n}{2} - 1 + 1 = \boxed{\frac{n}{2}}$

for j=0 to 2n-1 do

if Disk[j] is greater than Disk[j+1] do

Swap(Disk[j], Disk[j+1]) //2

increment count //1

end if

end for

for j=2n-1 to 1 down 1 do

if Disk[j] is less than Disk[j-1] do

Swap(Disk[j], Disk[j-1]) //2

increment count //1

end if

end for

return count //1

$$2n - 1 - 0 + 1 = 2n$$

$$2 + \max(3, 0)$$

$$= 5$$

$$= 2n \times 5 = \boxed{10n}$$

$$\frac{1 - 2n - 1}{-1} + 1 = \boxed{2n + 1}$$

$$2 + \max(3, 0)$$

$$2 + 3 = 5$$

$$(2n + 1)5 = \boxed{10n + 5}$$

$$2 + (10n + 5 + 10n) \frac{n}{2}$$

$$2 + \frac{10n^2}{2} + \frac{5n}{2} + \frac{10n^2}{2}$$

$$2 + \frac{20n^2 + 5n}{2}$$

$$S.C. = \frac{20n^2 + 5n + 4}{2}$$

$$O(n^2)$$

Prove

$$\lim_{n \rightarrow \infty} = \frac{20n^2 + 5n + 4}{2}$$

$$\lim_{n \rightarrow \infty} = \frac{20n^2 + 5n + 4}{2n^2}$$

$$\lim_{n \rightarrow \infty} = \frac{40n + 5}{4n}$$

$$\lim_{n \rightarrow \infty} = \frac{40}{4} = \boxed{10} \checkmark$$

Does belong to $O(n^2)$

Step count and proof for alternate

Alternate Stepcount & Proof

Set count to 0 // 1

for i=1 to n+1 do // $n+1-1+1 = n+1$

if i mod 2 = 0 then do

for j=0 to 2n-1 step 2 do

if Disk[j] is greater than Disk[j+1] do

Swap (Disk[j], Disk[j+1]) // 2

increment count // 1

end if

end for

end if

else

for j=1 to 2n-2 step 2 do

if Disk[j] is greater than Disk[j+1] do

Swap (Disk[j], Disk[j+1]) // 2

increment count // 1

end if

end for

end else

end for

return count // 1

$$\left(\frac{10n+9}{2} \right) (n+1) + 2$$

$$= \frac{10n^2 + 10n + 9n + 9}{2} + 2$$

$$= \frac{10n^2 + 19n + 9}{2} + 2$$

$$= \frac{10n^2 + 19n + 13}{2}$$

$$\frac{10n^2 + 19n + 13}{2} = S.C$$

$$O(n^2)$$

$$2 + \max\left(\frac{10n+5}{2}, \frac{10n-5}{2}\right) = \frac{10n+9}{2}$$

$$\frac{2n-1}{2} + \frac{2}{2} = \frac{2n+1}{2}$$

$$2 + \max(3, 0) = 5$$

$$\frac{2n+1}{2} \times 5$$

$$\frac{10n+5}{2}$$

$$\frac{2n-2-1}{2} + 1 = \frac{2n-1}{2}$$

$$2 + \max(3, 0) = 5$$

$$\left(\frac{2n-1}{2} \right) 5$$

$$\frac{10n-5}{2}$$

Proof

$$\lim_{n \rightarrow \infty} \frac{10n^2 + 19n + 13}{2n^2}$$

$$\lim_{n \rightarrow \infty} = \frac{10n^2 + 19n + 13}{2n^2}$$

$$\lim_{n \rightarrow \infty} = \frac{20n + 19}{4n}$$

$$\lim_{n \rightarrow \infty} = \frac{20}{4}$$

= 5 ✓ does belong To $O(n^2)$

images posted by mistake on Discord

$1 + 2 + n(2n+4)$
 $3 + n(2n+4)$
 $int\ count = 0$ // 1 // 1
 $for(i=0; i < n+1; i++)$ // $n+2$
 $\{$
 $\quad if(i \% 2 == 0)$ // $2 + \max(2n+2, 2n-2) = 2n+4$
 $\quad \{$
 $\quad \quad for(int j=0; j < n-1; j+=2)$ // $\frac{n-1-0}{2} + 1 = \frac{n-1}{2} + \frac{2}{2} = \frac{n+1}{2}$
 $\quad \quad \{$
 $\quad \quad \quad if(d[j] > d[j+1])$ // $2 + \max(2, 0) = 4$
 $\quad \quad \quad \{$
 $\quad \quad \quad \quad swap$
 $\quad \quad \quad \quad count++$
 $\quad \quad \quad \}$
 $\quad \quad \}$
 $\quad \}$
 $\}$
 $return count;$ // 1 // 1

$\frac{n+1}{2} \cdot \frac{4}{1} = (n+1)2 = 2n+2$

$\frac{n-1}{2} + 1 = \frac{n-3}{2} + 1 = \frac{n-3}{2} + \frac{2}{2} = \frac{n-1}{2}$

$2 + \max(2, 0) = 4$

$\frac{n-1}{2} \cdot \frac{4}{1} = 2n-2$

Alternate S.C
 $1 + 1 + 2 + n(2n+4)$
 $4 + n(2n+4)$
 $4 + 2n^2 + 4n$
 S.C = $2n^2 + 4n + 4$

