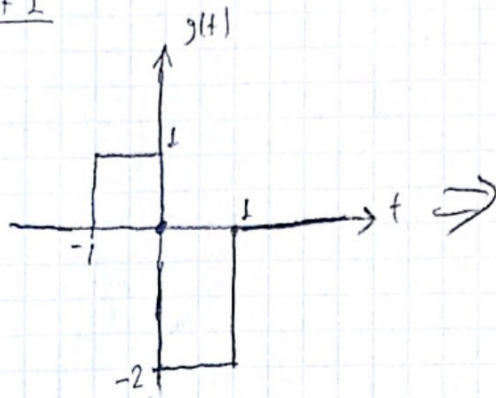


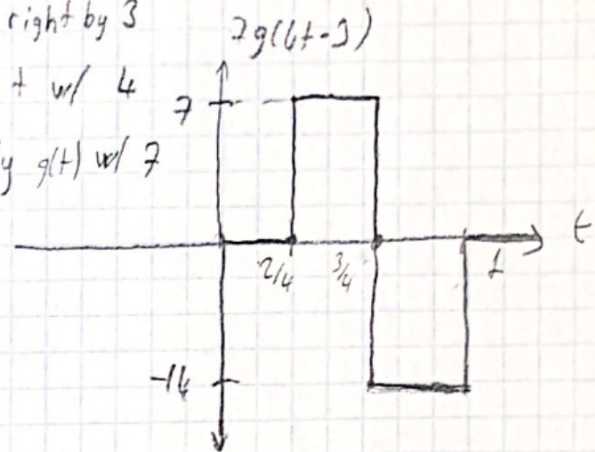
Part 1



Shift right by 3

Scale + w/ 4

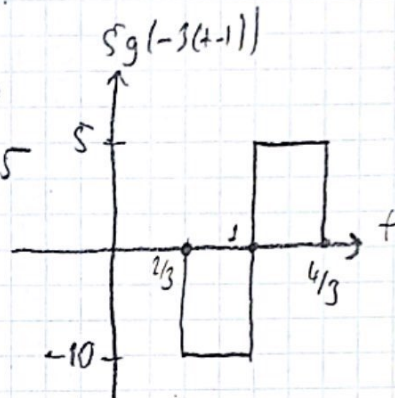
Multiply  $g(t)$  w/ 7



Shift right by 1

Scale + w/ -3

$\Rightarrow$  Multiply  $g(t)$  w/ 5



$g(t)$  can't be recovered when it is sampled. I cannot be recovered because  $g(j\omega)$  is a sinc function. Sinc function is not band limited function.

Therefore, it is not possible to find a  $T_s$  value to satisfy Nyquist Criteria.

Part 2

$$X_{\text{sampled}}(t) = x(t) \sum_{n=-\infty}^{\infty} \delta(t - nT_s) \quad \begin{matrix} \text{sampled} \\ \text{Signal} \end{matrix}$$

$$= \sum_{n=-\infty}^{\infty} x(nT_s) \delta(t - nT_s) \rightarrow x(nT_s) = \tilde{x}[n] \quad \begin{matrix} \text{Discrete} \\ \text{time} \\ \text{function} \end{matrix}$$

$\tilde{x}[n] \xrightarrow{\text{from interpolation}} x_R(t)$  AS we want  $x(t) = x_R(t)$  this equals  $x(t)$   $\Rightarrow x_R(t) = X_{\text{sampled}}(t) * p(t)$

$$\text{Thus, } x_R(t) = \int_{-\infty}^{\infty} \underbrace{\sum_{n=-\infty}^{\infty} x(nT_s) \delta(t' - nT_s)}_{X_{\text{sampled}}(t)} p(t - t') dt' = \sum_{n=-\infty}^{\infty} x(nT_s) \int_{-\infty}^{\infty} \delta(t' - nT_s) p(t - t') dt'$$

$$= \sum_{n=-\infty}^{\infty} x(nT_s) p(t - nT_s) \Rightarrow x[nT_s] = \tilde{x}[n]$$

$$p(0) = 1, p(kT_s) = 0 \rightarrow x_R(nT_s) = \sum_{k=-\infty}^{\infty} x(kT_s) p(nT_s - kT_s), \quad x(kT_s) = x_R(nT_s) \text{ when } p(0) = 1$$

$x_R(nT_s) = 0$  when  $p(kT_s) = 0$  because  $(p(nT_s - kT_s) = 0)$ . Thus,  $x_R(nT_s) = x(nT_s)$  when  $p(0) = 1$  and  $p(kT_s) = 0 \quad \forall k \in \mathbb{Z}^+ \quad \checkmark$

a)  $p_z(0) = 1, p_L(kT_s) = p_I(kT_s) = 0$ , b)  $p_z(kT_s) = p_L(kT_s) = p_I(kT_s) = 0$

c) All of them are consistent as they satisfy  $p(0) = 1$  and  $p(kT_s) = 0$



## Part 5

\* Zero-Order Hold interpolation recovery looks <sup>almost</sup> exactly same as the original signal

\* Likewise in the first one, in linear interpolation recovery looks <sup>almost</sup> exactly same as the original signal.

\* Ideal Band Limited interpolation is not as efficient as expected.

There are some oscillations after jumps.

\* The most efficient one is zero-order hold interpolation. Also, it can be said that zero-order hold interpolation is the best interpolation compared to others. When  $T_s$  is increased, recovery process seems like becoming less efficient compared to others. This might be because of we get less sample points when  $T_s$  increases.

## Part 6

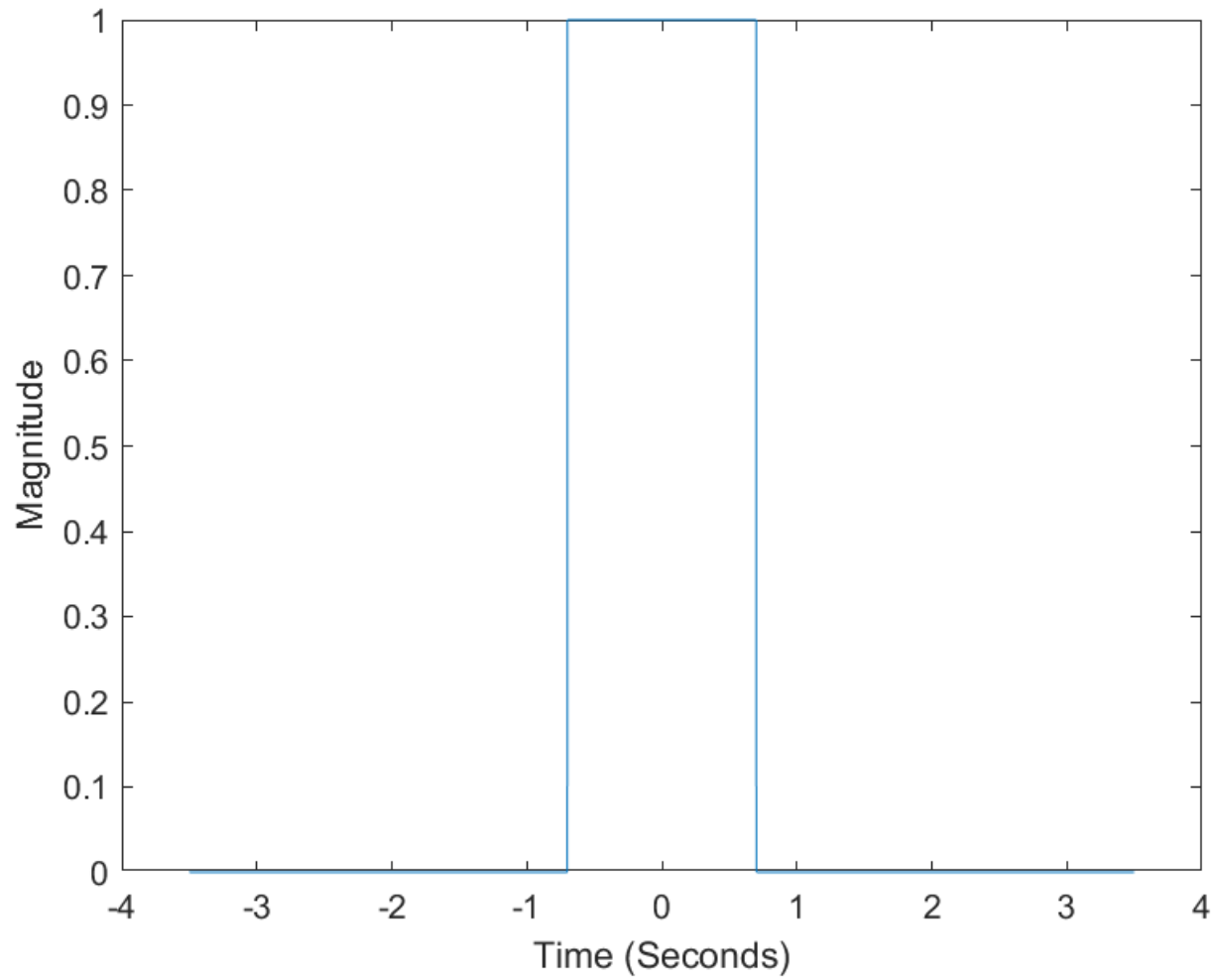
\* Ideal Band Limited interpolation is the most efficient recovery in this part. Original signal can obtained by this interpolation. In the other ones, it is not efficient as in ideal band limited interpolation because there is loss of data and some incorrect data occurs.

\* When  $T_s = 0.01$ , where  $0.1 \leq T_s \leq 0.2$ , the most efficient recovery is done. The sketch is similar to <sup>the graph of</sup> the sum of weighted sine function which repeats itself periodically.

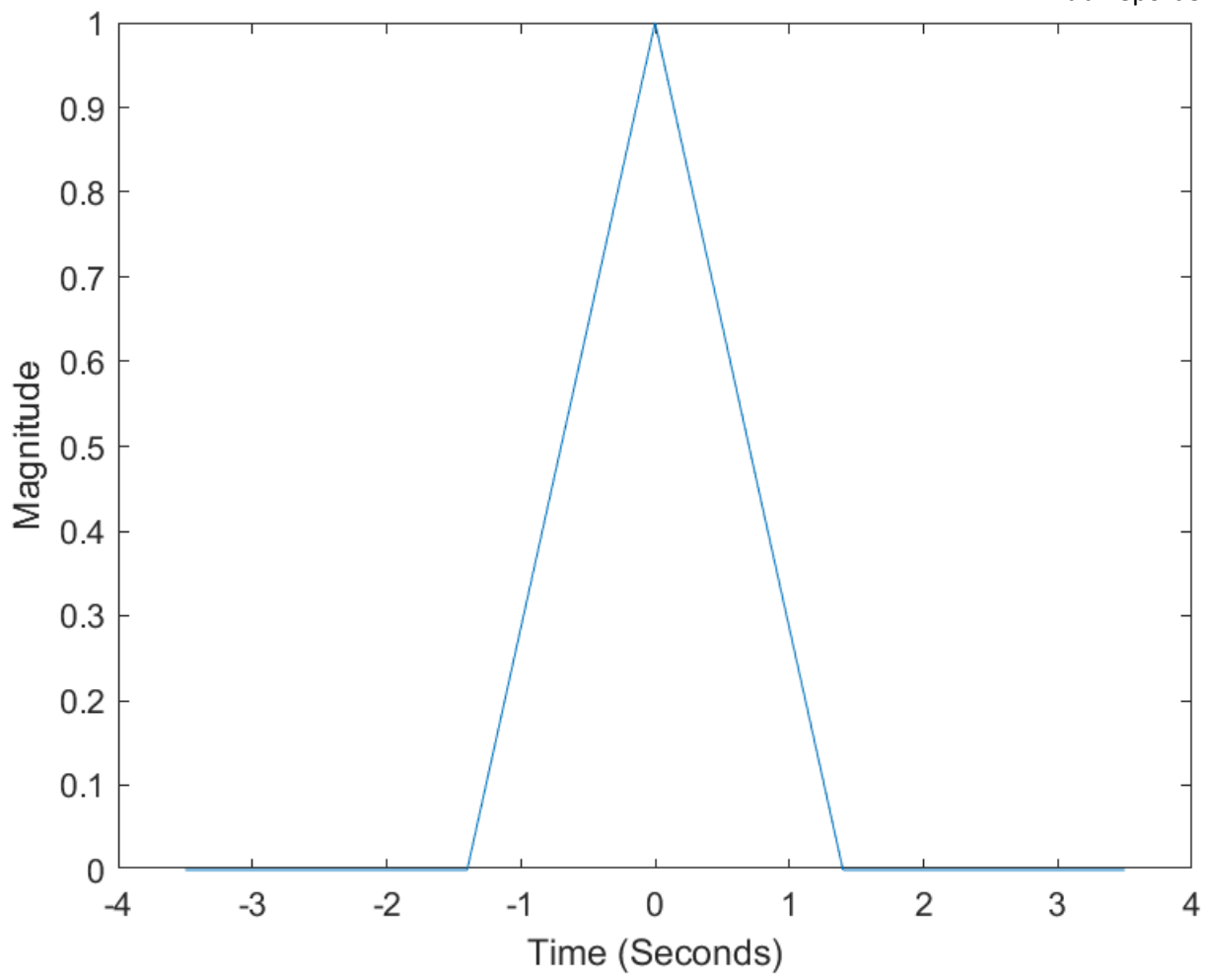
\* If there is more data, or, more sample points the recovery process would be more efficient and the signals obtained (recovery signals) would be much closer to the original signal.

### EEE321 Lab Report 5

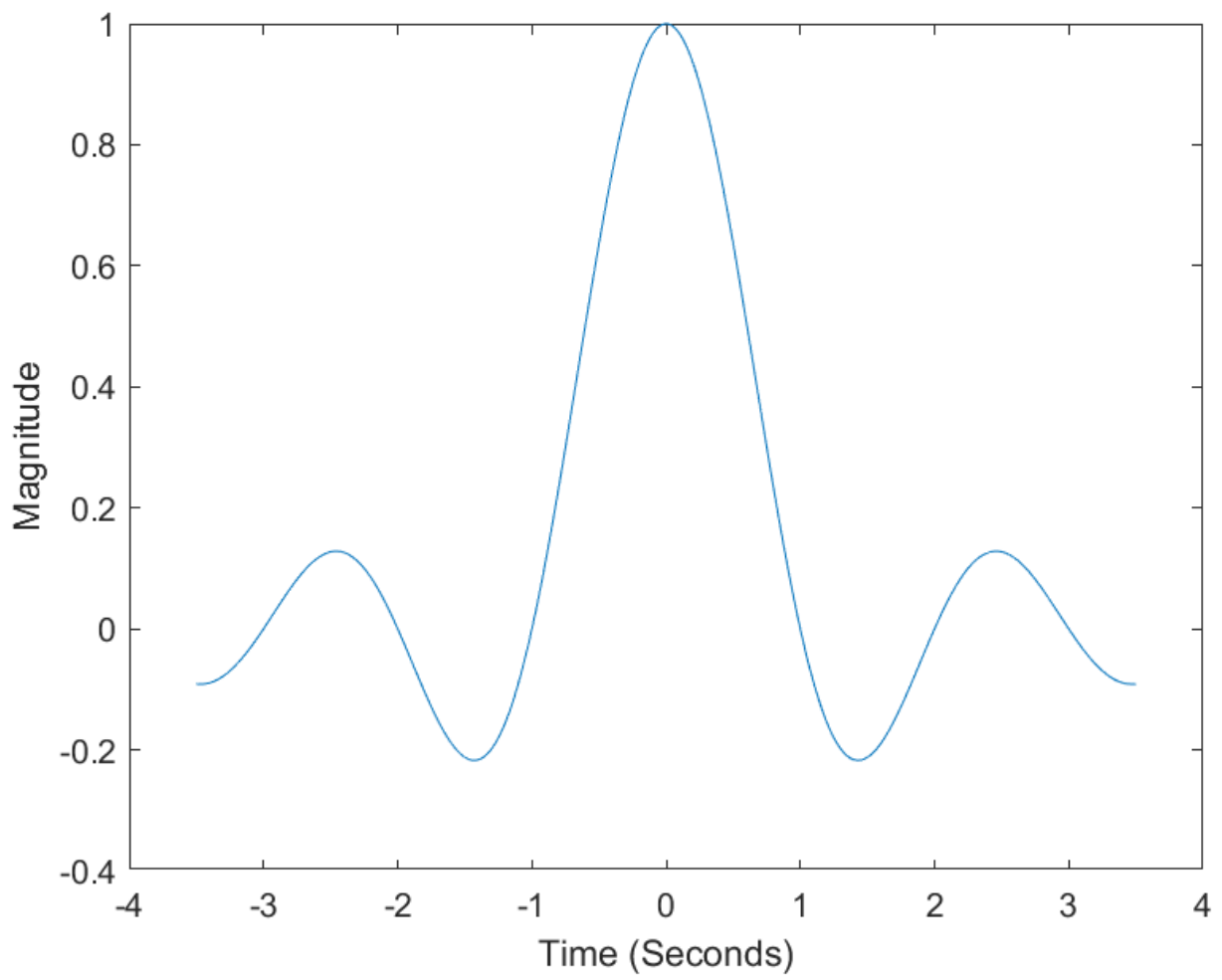
#### Part 3



**Figure 1:** Plot of  $p_{\text{rect}}$  function

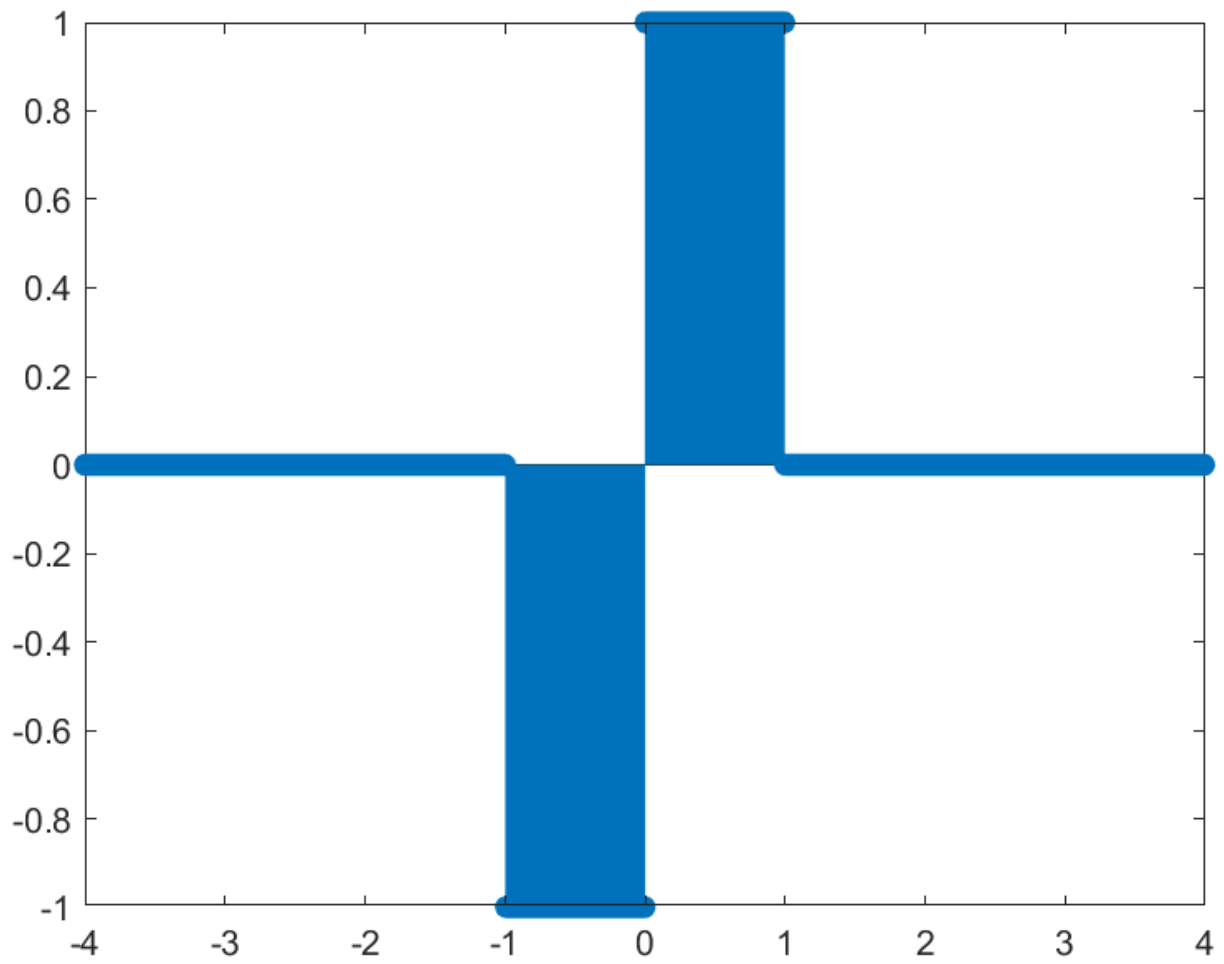


**Figure 2:** Plot of  $p_{tri}$  function

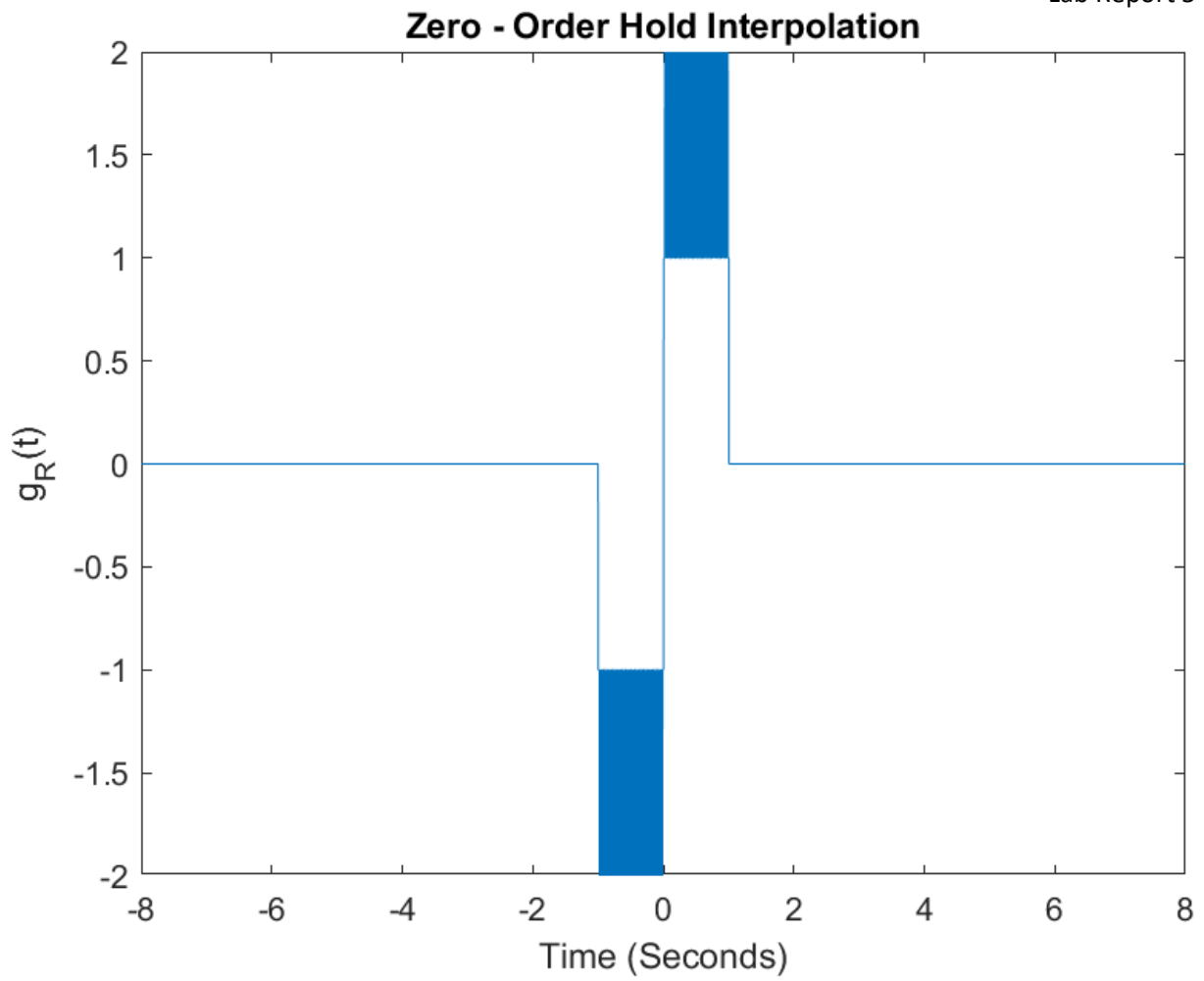


**Figure 3:** Plot of  $p_{\text{sinc}}$  function

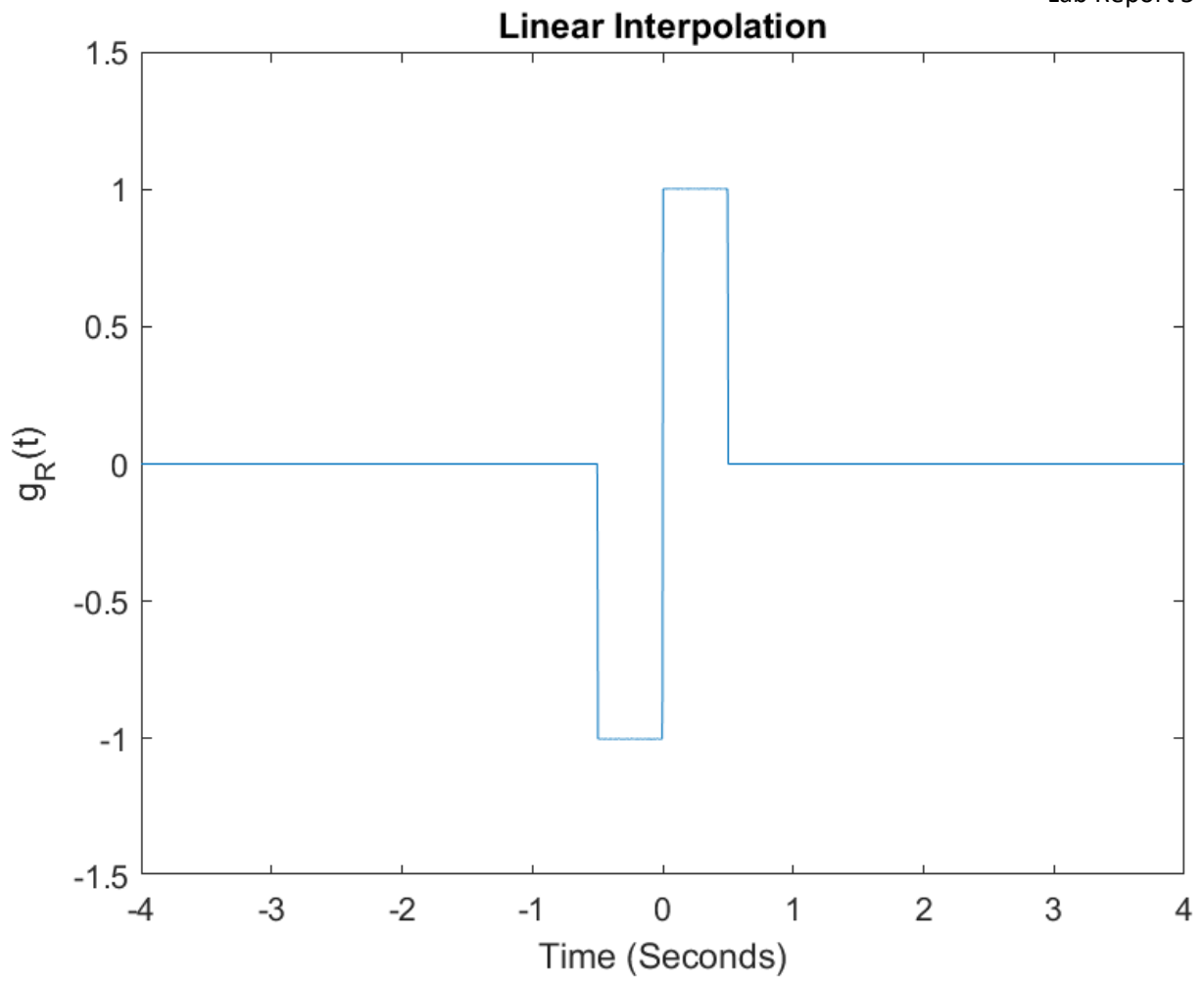
**Part 5**



**Figure 4:** Plot of  $g_R(t)$



**Figure 5:** Zero-Order Hold Interpolation plot of  $g_R(t)$



**Figure 6:** Linear Interpolation plot of  $g_R(t)$



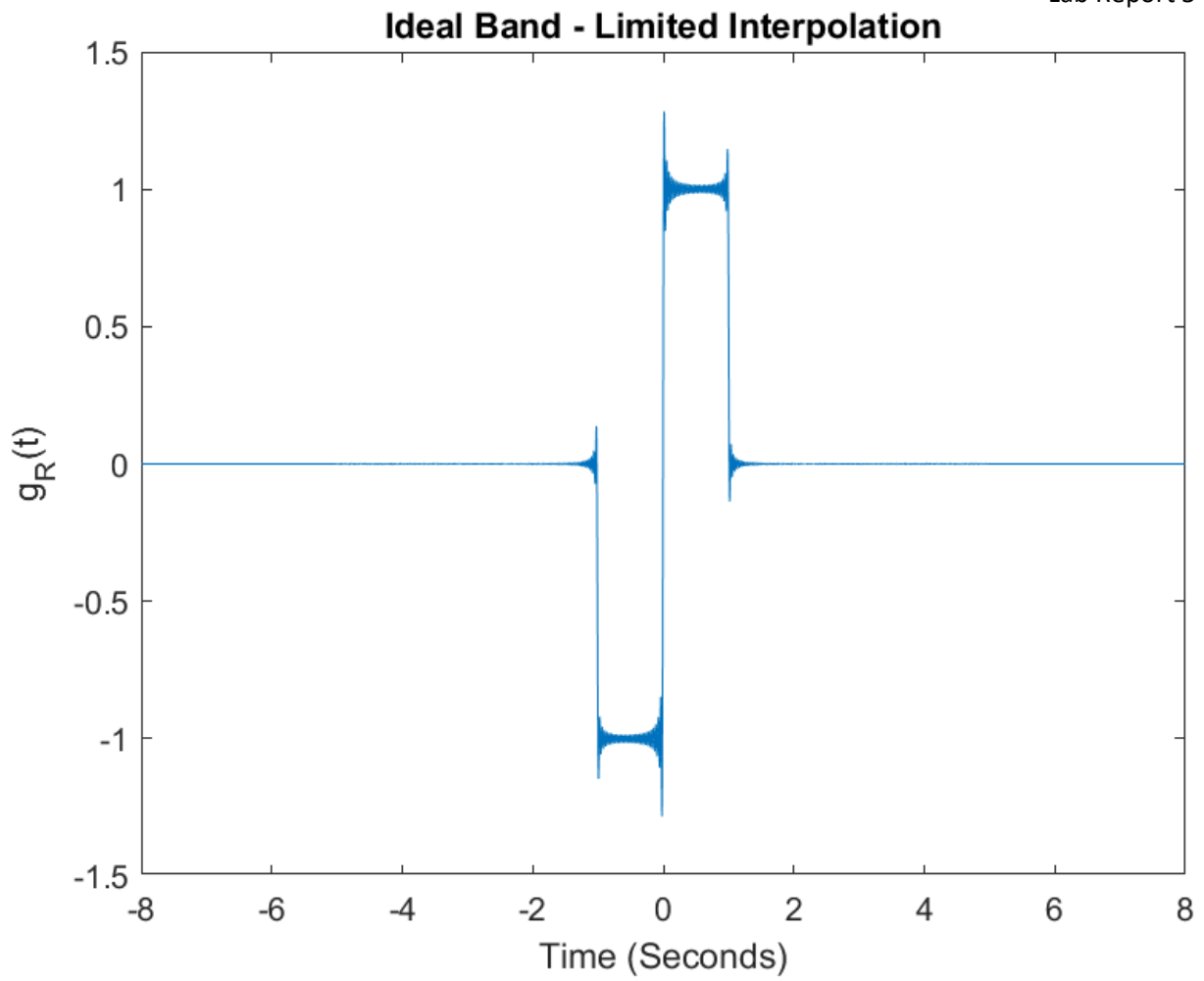


Figure 7: Ideal band – Limited Interpolation plot of  $g_R(t)$

#### Part 6

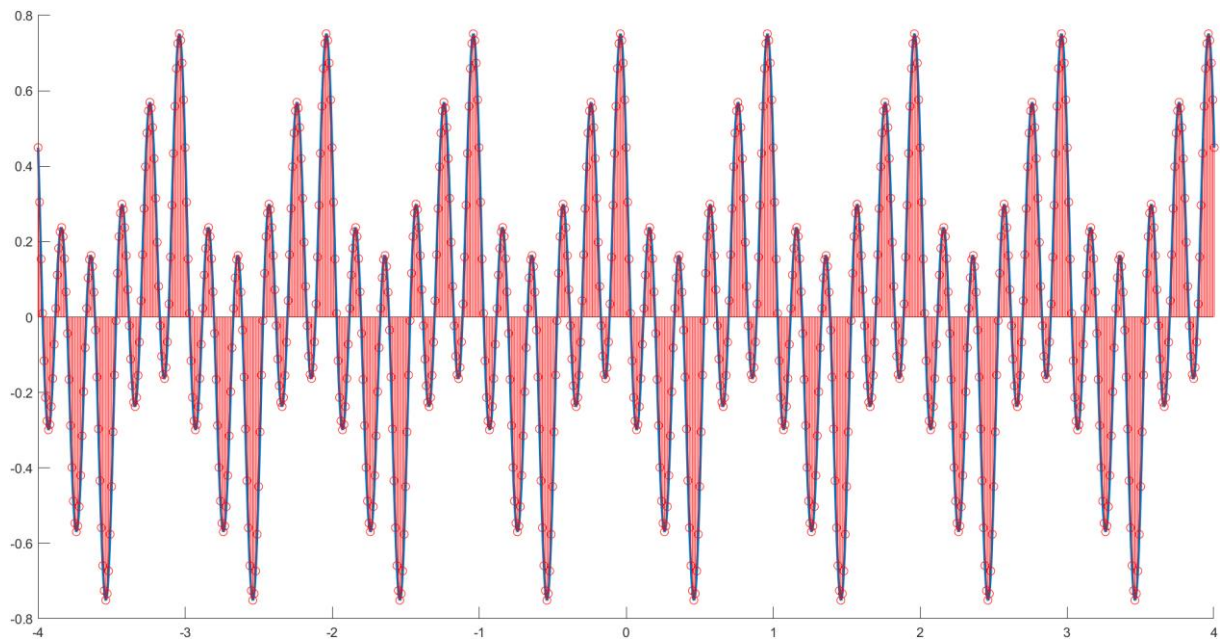
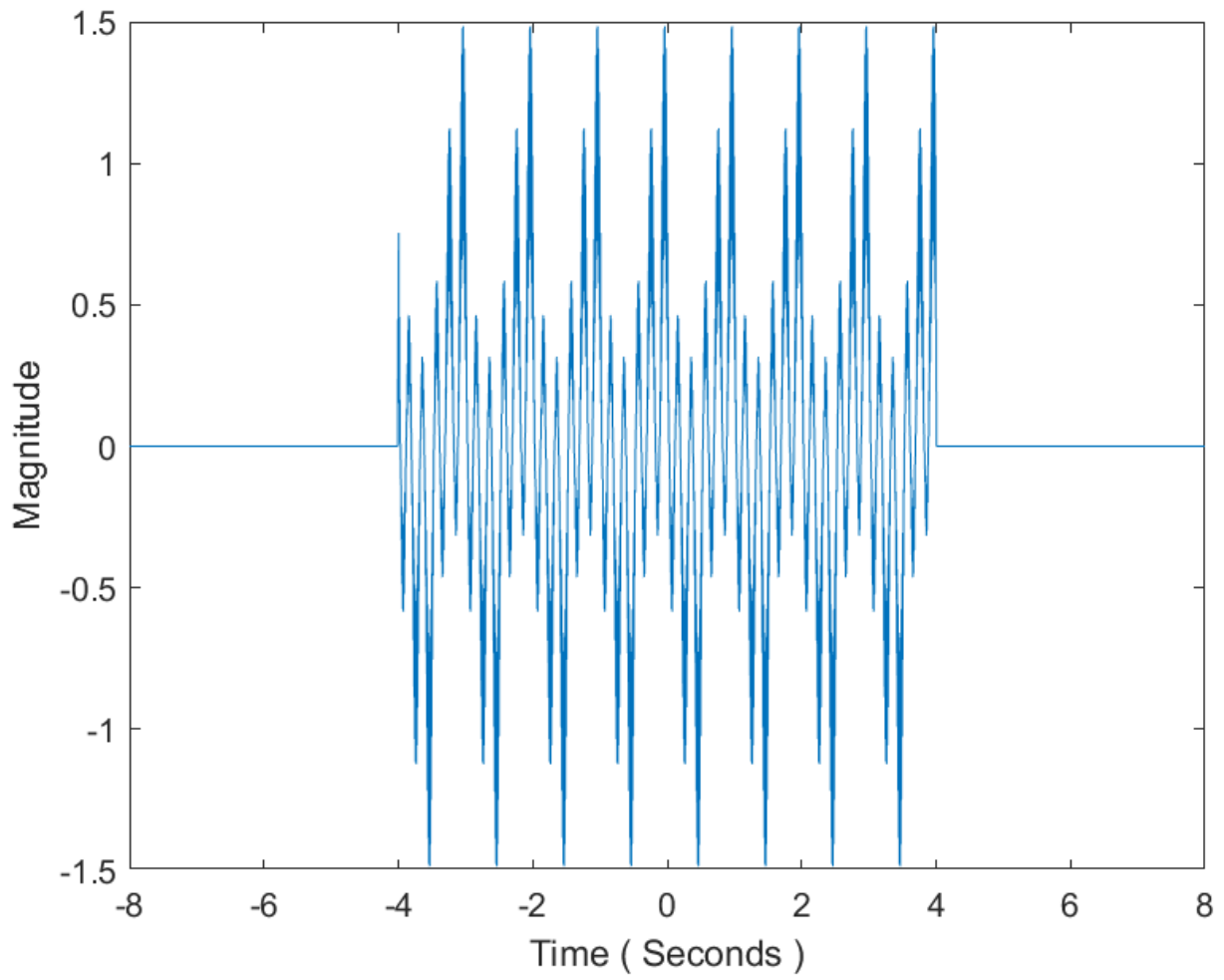
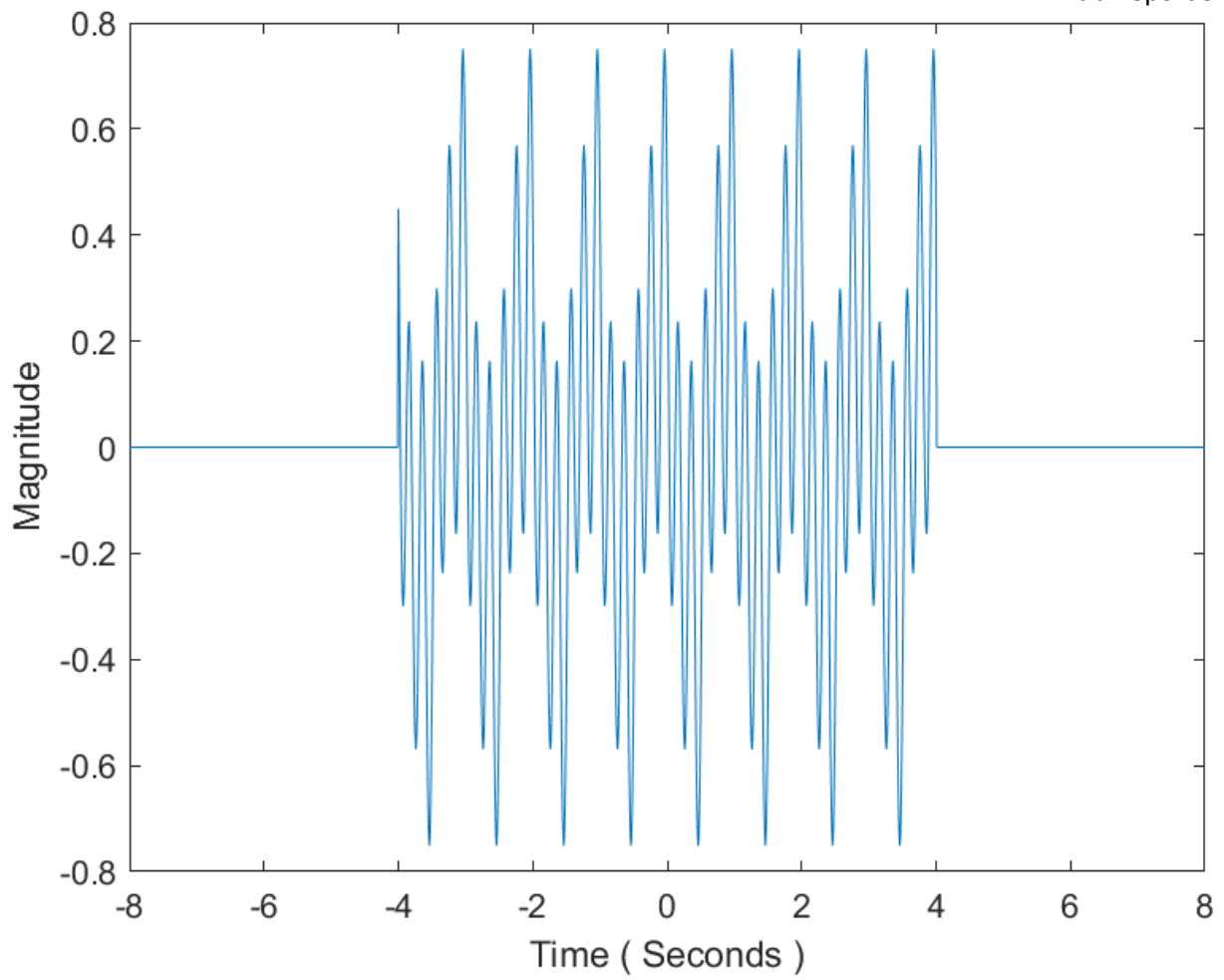


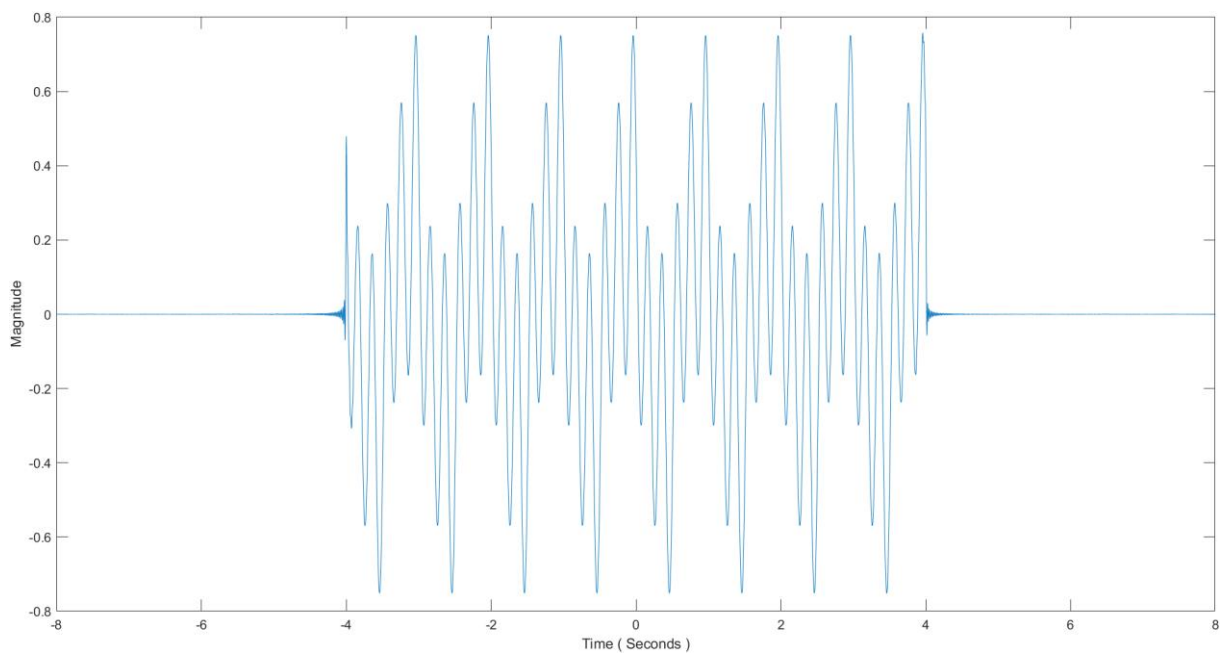
Figure 8: Plot of  $x(t)$  and  $x_{sampled}(t)$  in The Same Graph when  $T_s = 0.005(D_6 + 1)$



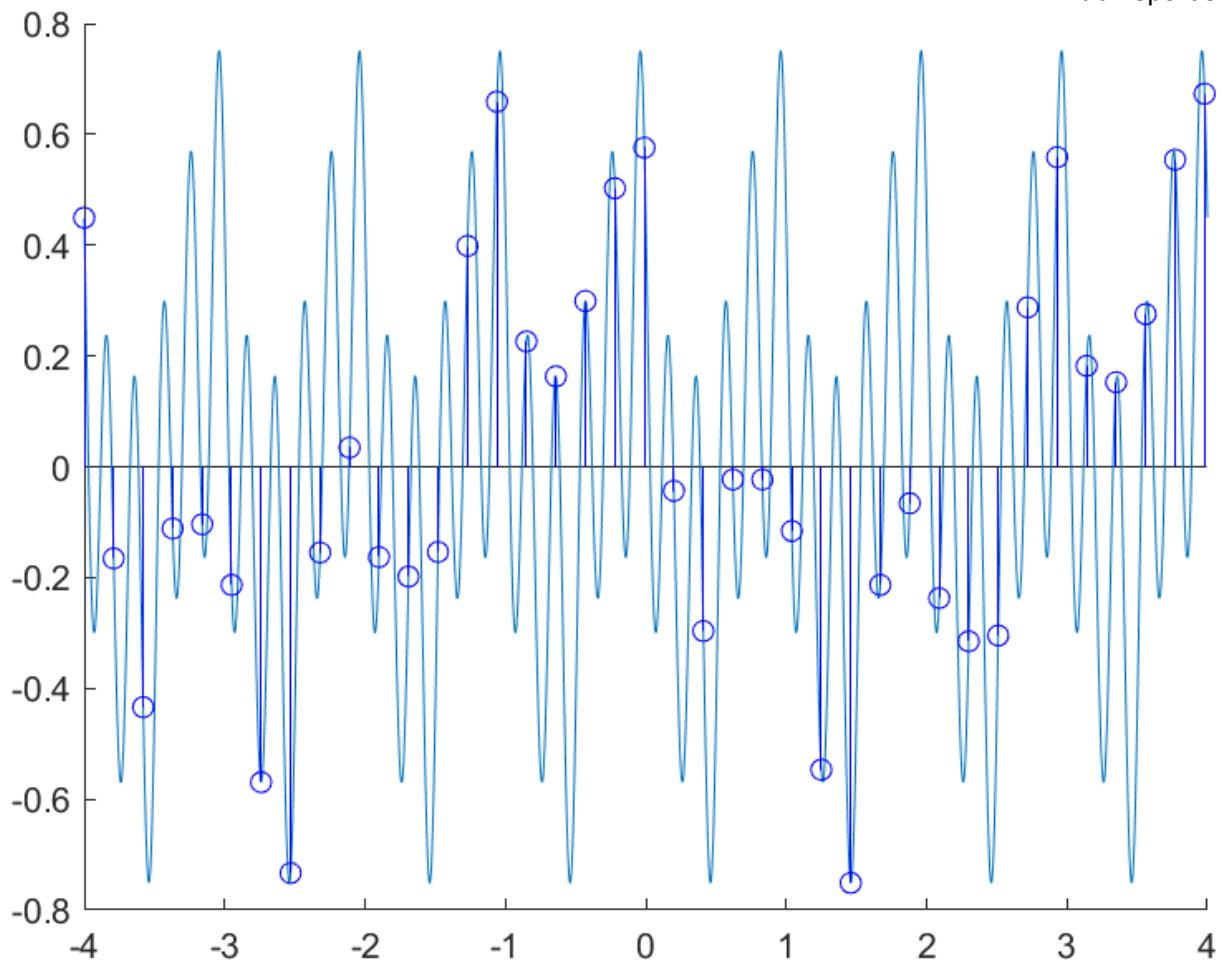
**Figure 9:** Plot of  $x_R(t)$  After Using Zero - Order Hold Interpolation when  $T_s = 0.005(D_6 + 1)$



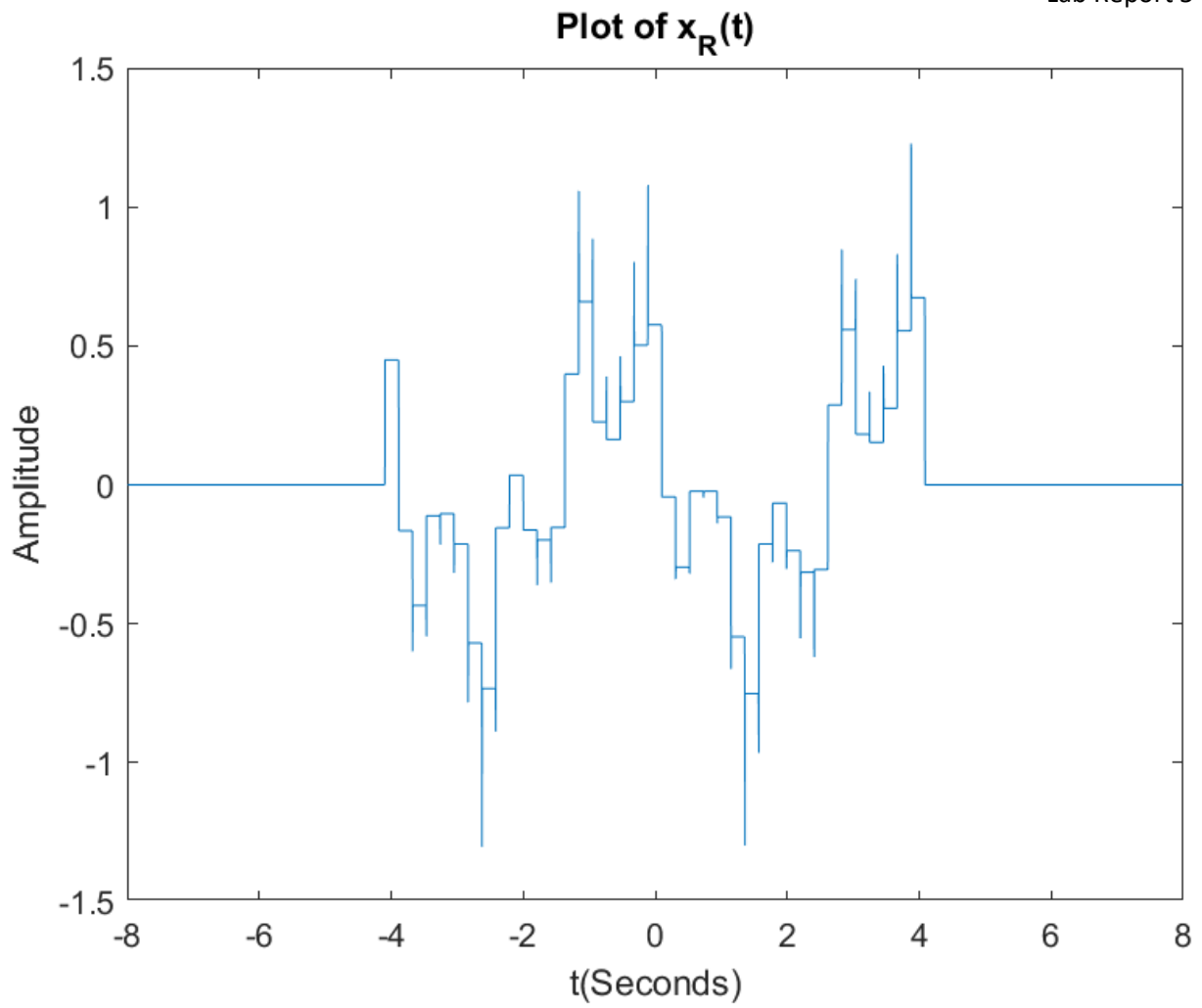
**Figure 10:** Plot of  $x_R(t)$  After Using Linear Interpolation when  $T_s = 0.005(D_6 + 1)$



**Figure 11:** Plot of  $x_R(t)$  After Using Ideal Band - Limited Interpolation when  $T_s = 0.005(D_6 + 1)$

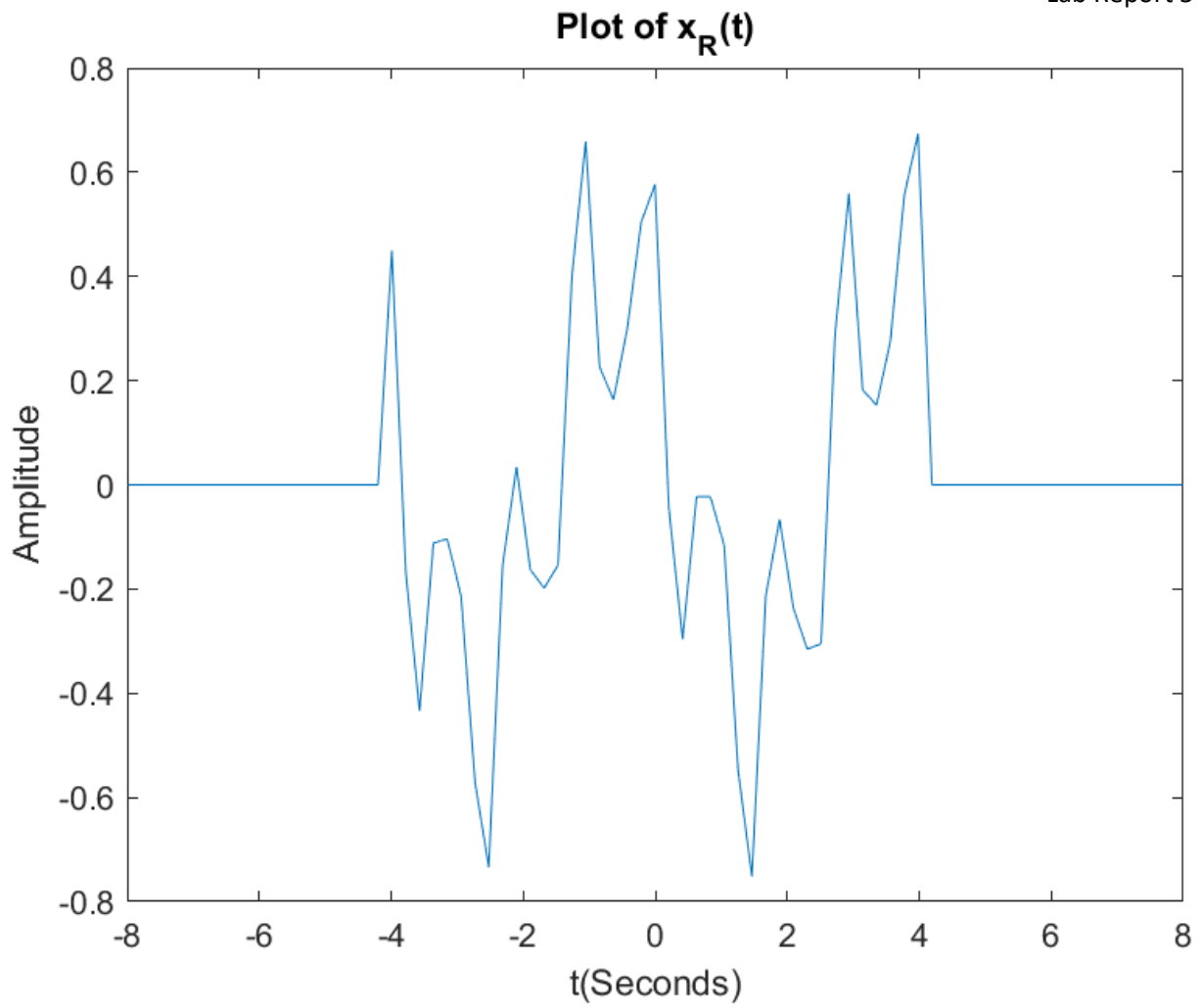


**Figure 12:** Plot of  $x(t)$  and  $x_{\text{sampled}}(t)$  in The Same Graph when  $T_s = 0.2 + 0.01 \cdot D6$ .

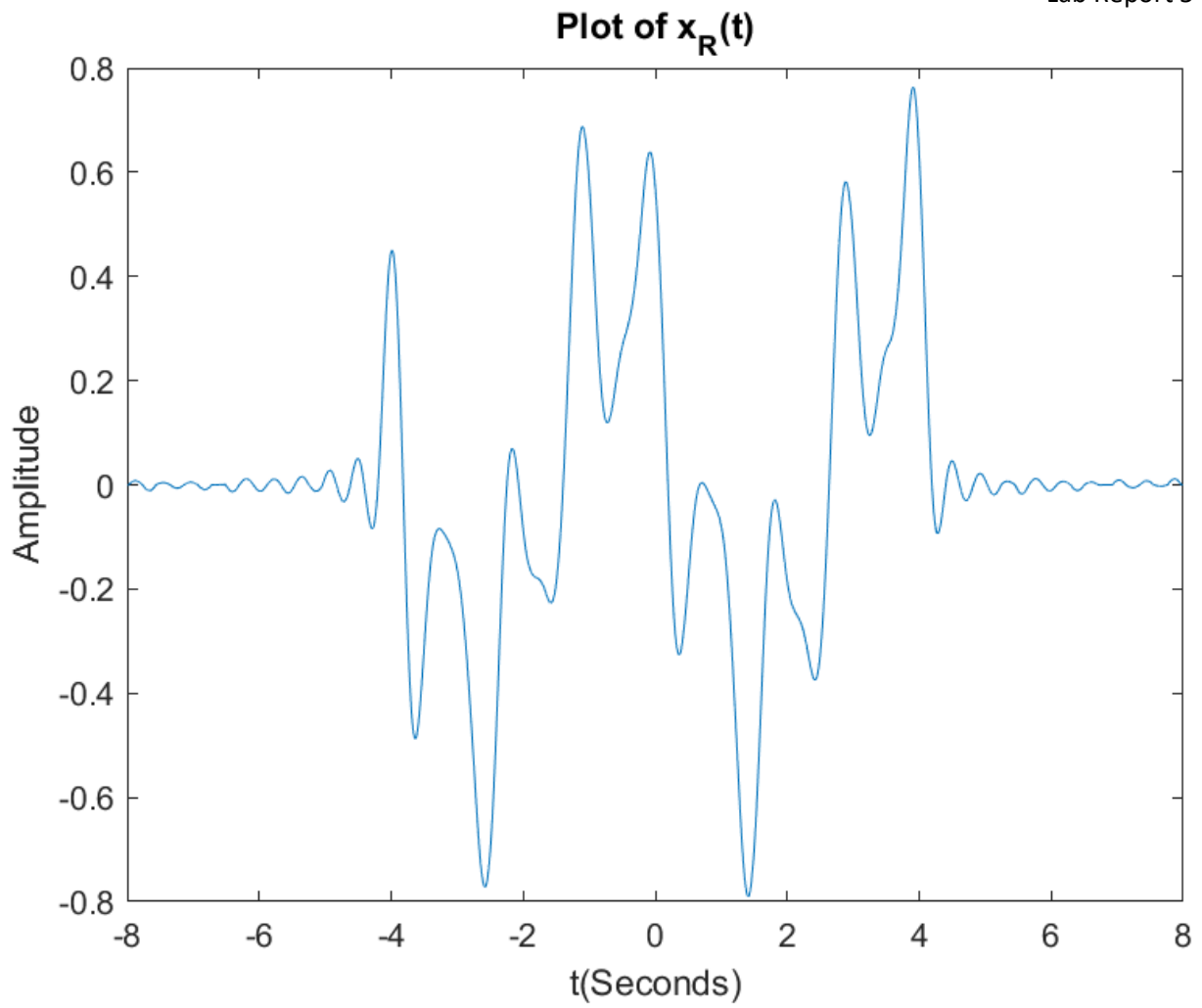


**Figure 13:** Plot of  $x_R(t)$  After Using Zero - Order Hold Interpolation when  $T_s = 0.2 + 0.01 \cdot D6$ .

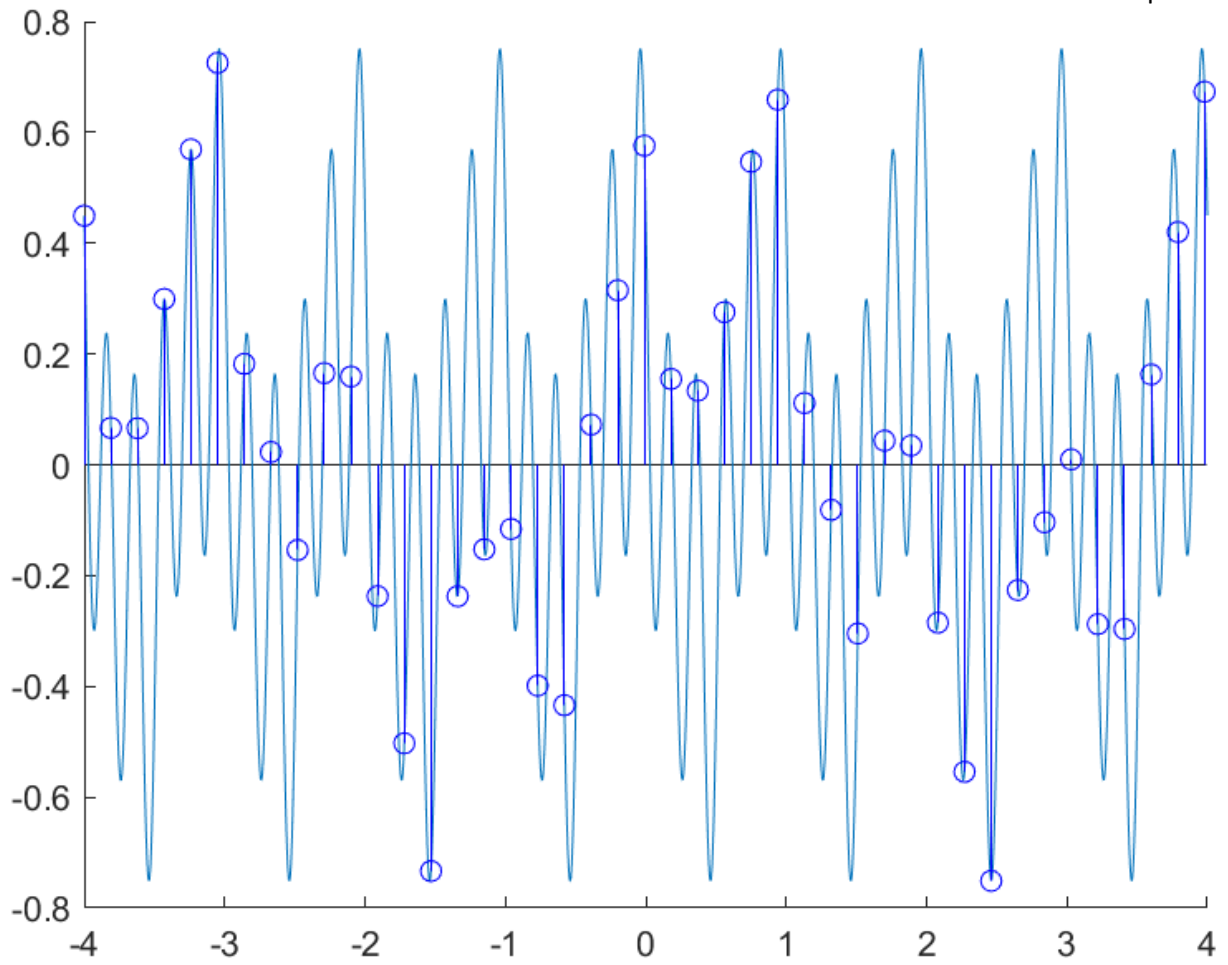




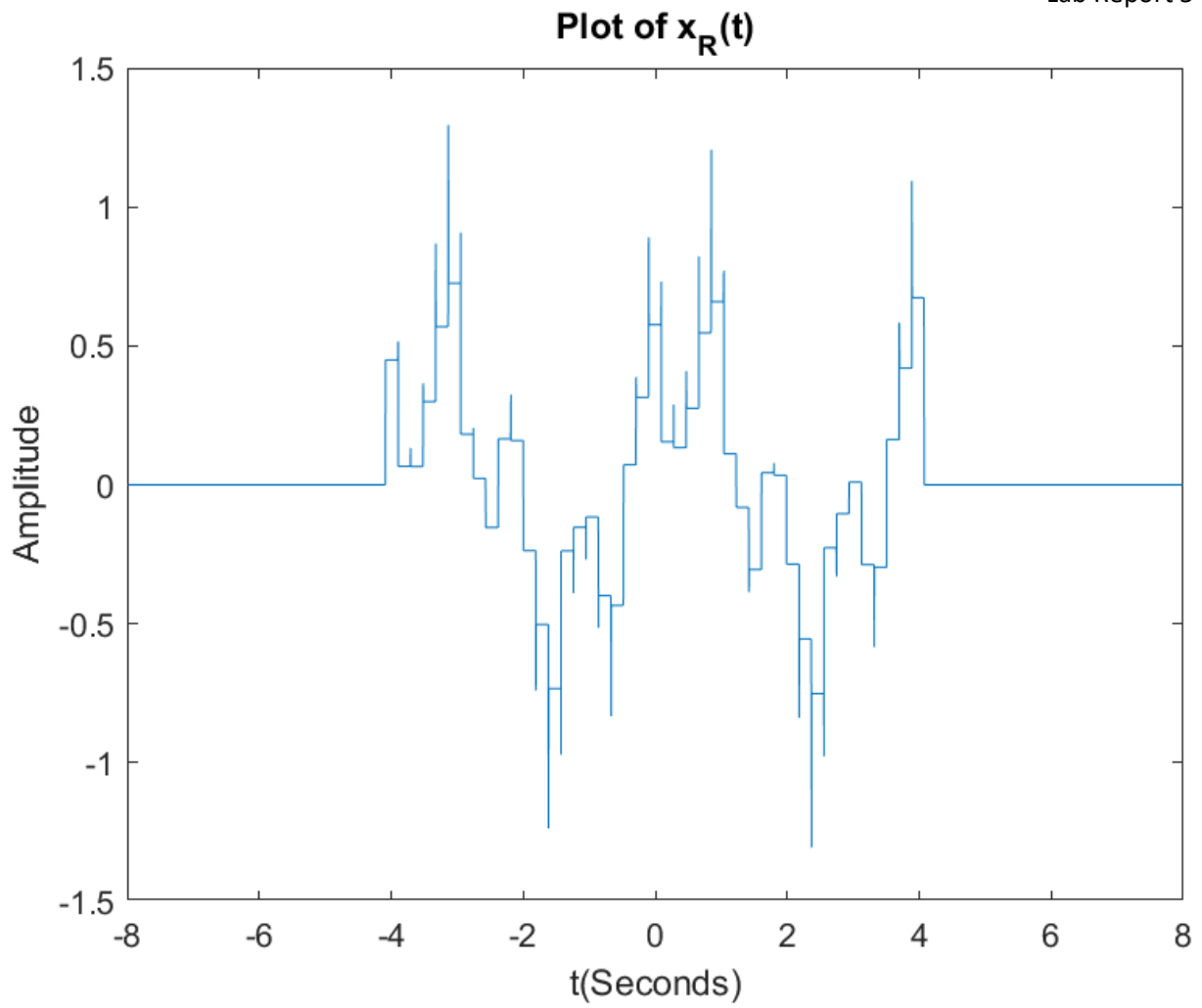
**Figure 14:** Plot of  $x_R(t)$  After Using Linear Interpolation when  $T_s = 0.2 + 0.01 \cdot D6$ .



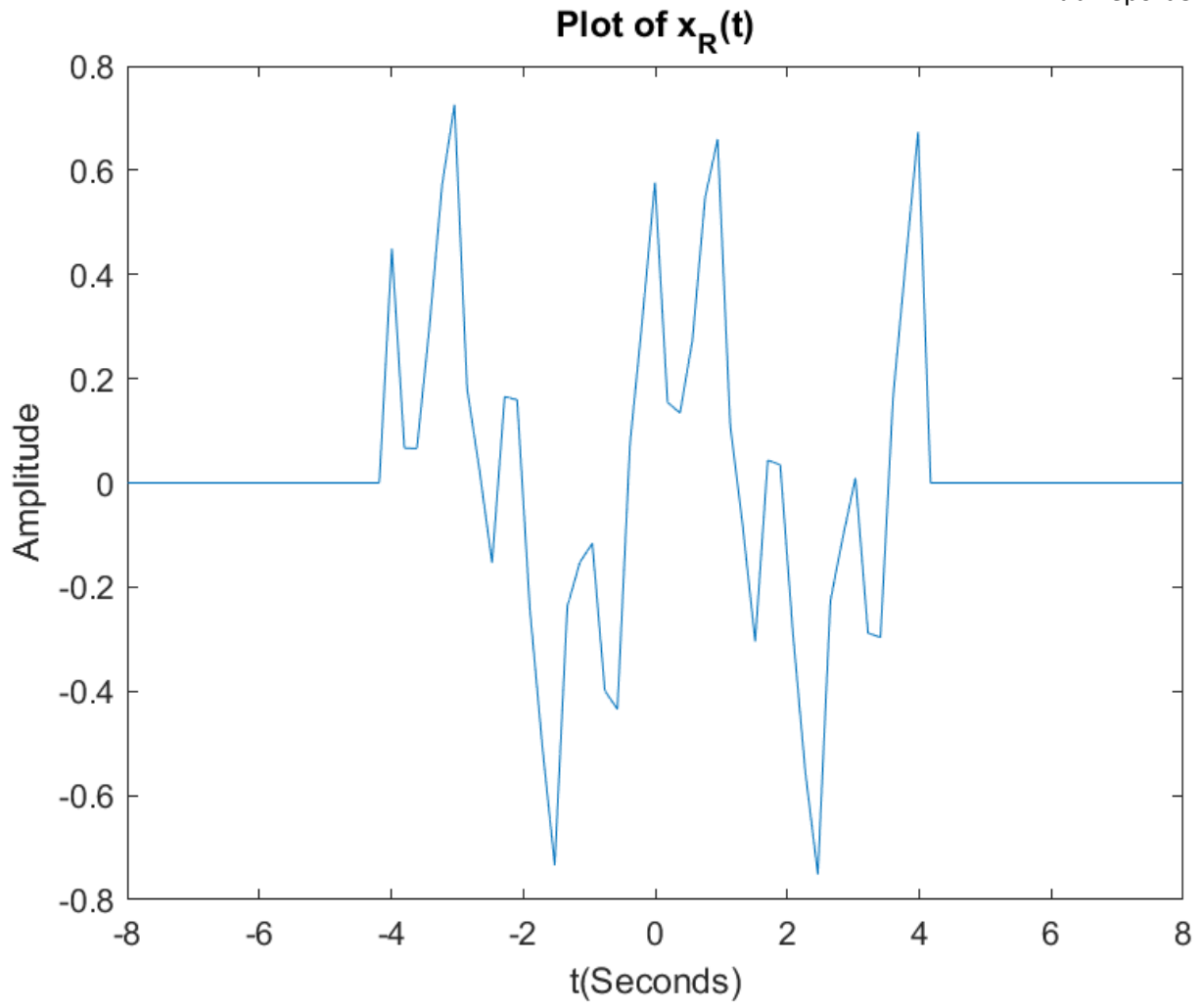
**Figure 15:** Plot of  $x_R(t)$  After Using Ideal Band when  $T_s = 0.2 + 0.01 \cdot D_6$ .



**Figure 16:** Plot of  $x(t)$  and  $x_{\text{sampled}}(t)$  in The Same Graph when  $T_s = 0.18 + 0.005 \cdot (D6 + 1)$ .

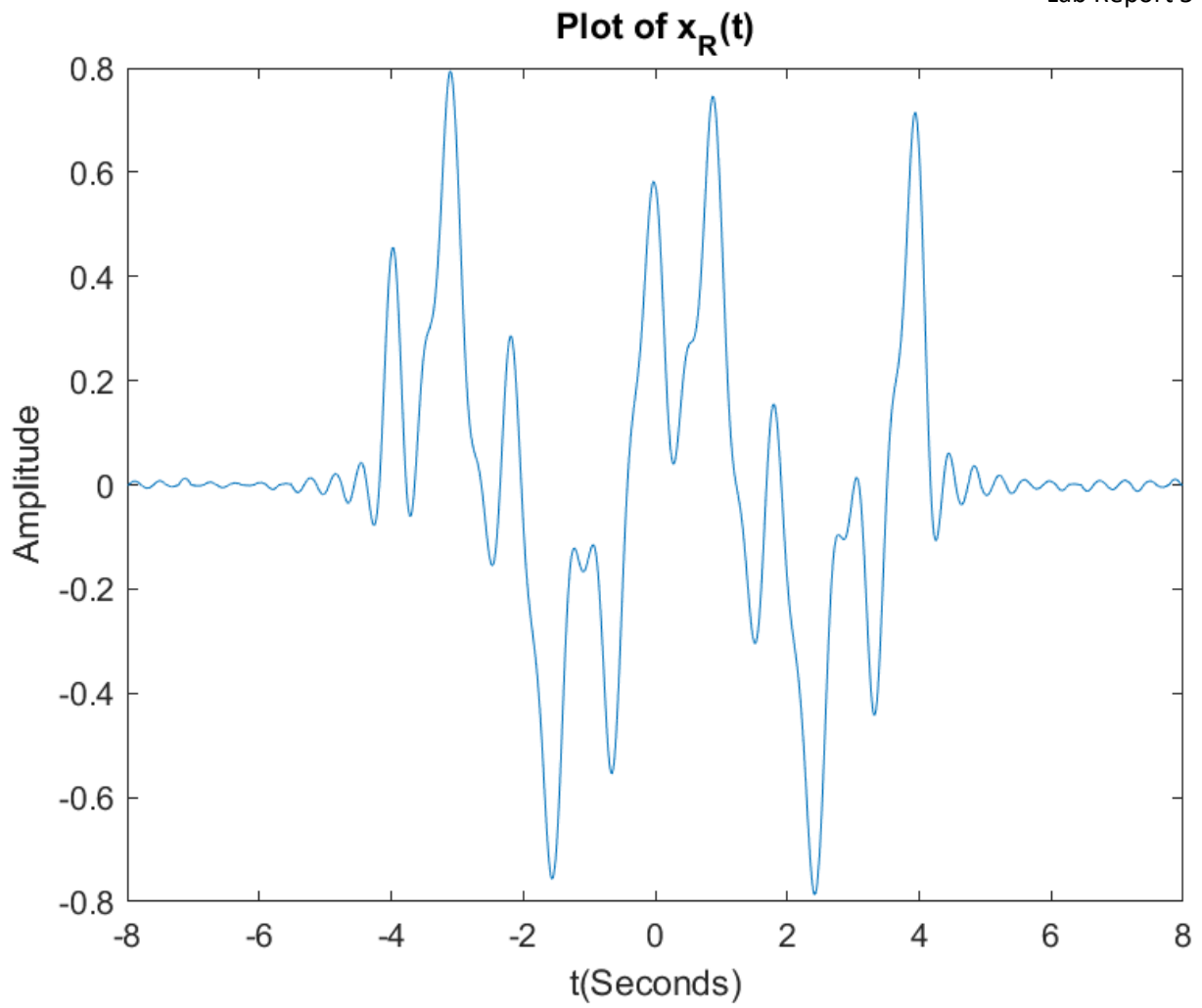


**Figure 17:** Plot of  $x_R(t)$  After Using Zero - Order Hold Interpolation when  $T_s = 0.18 + 0.005 \cdot (D6 + 1)$ .

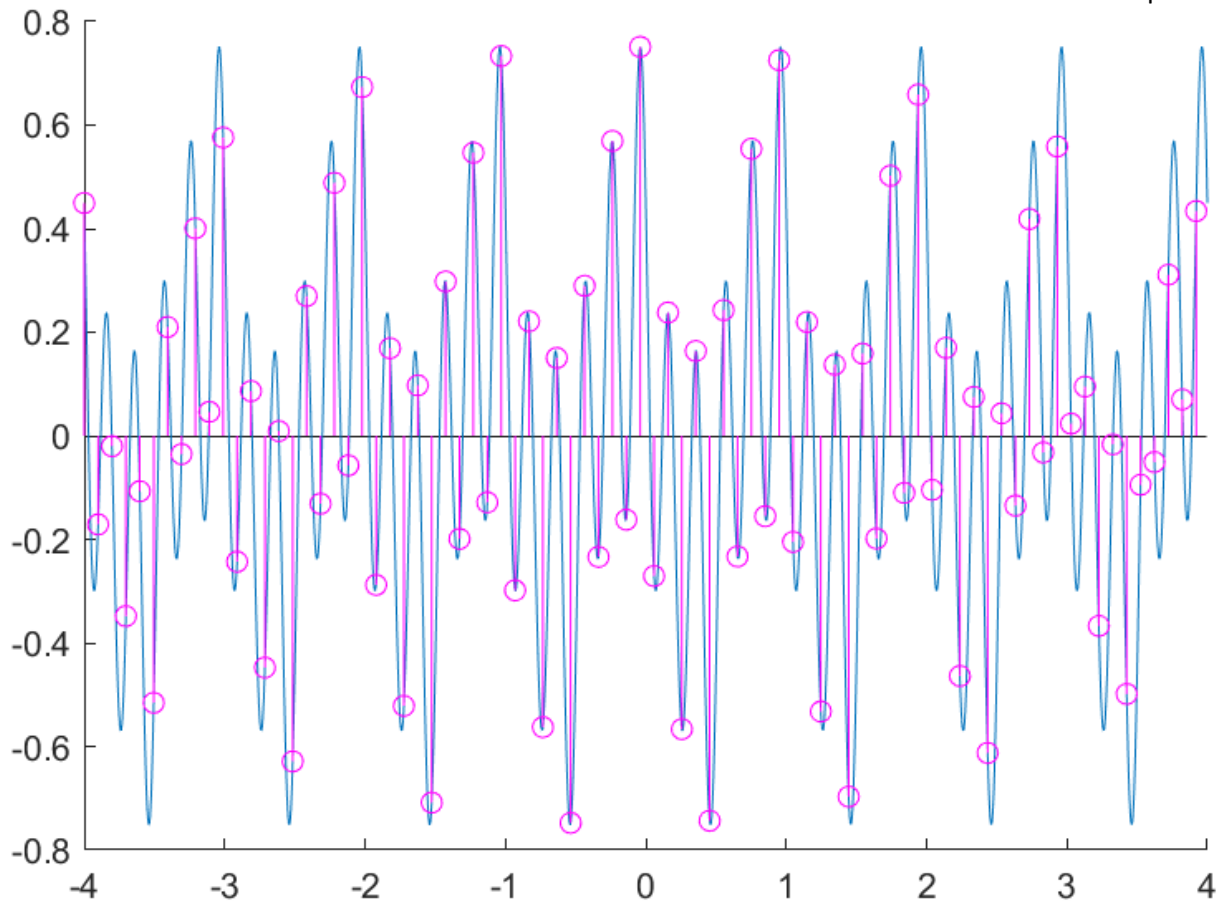


**Figure 18:** Plot of  $x_R(t)$  After Using Linear Interpolation when  $T_s = 0.18 + 0.005 \cdot (D6 + 1)$ .

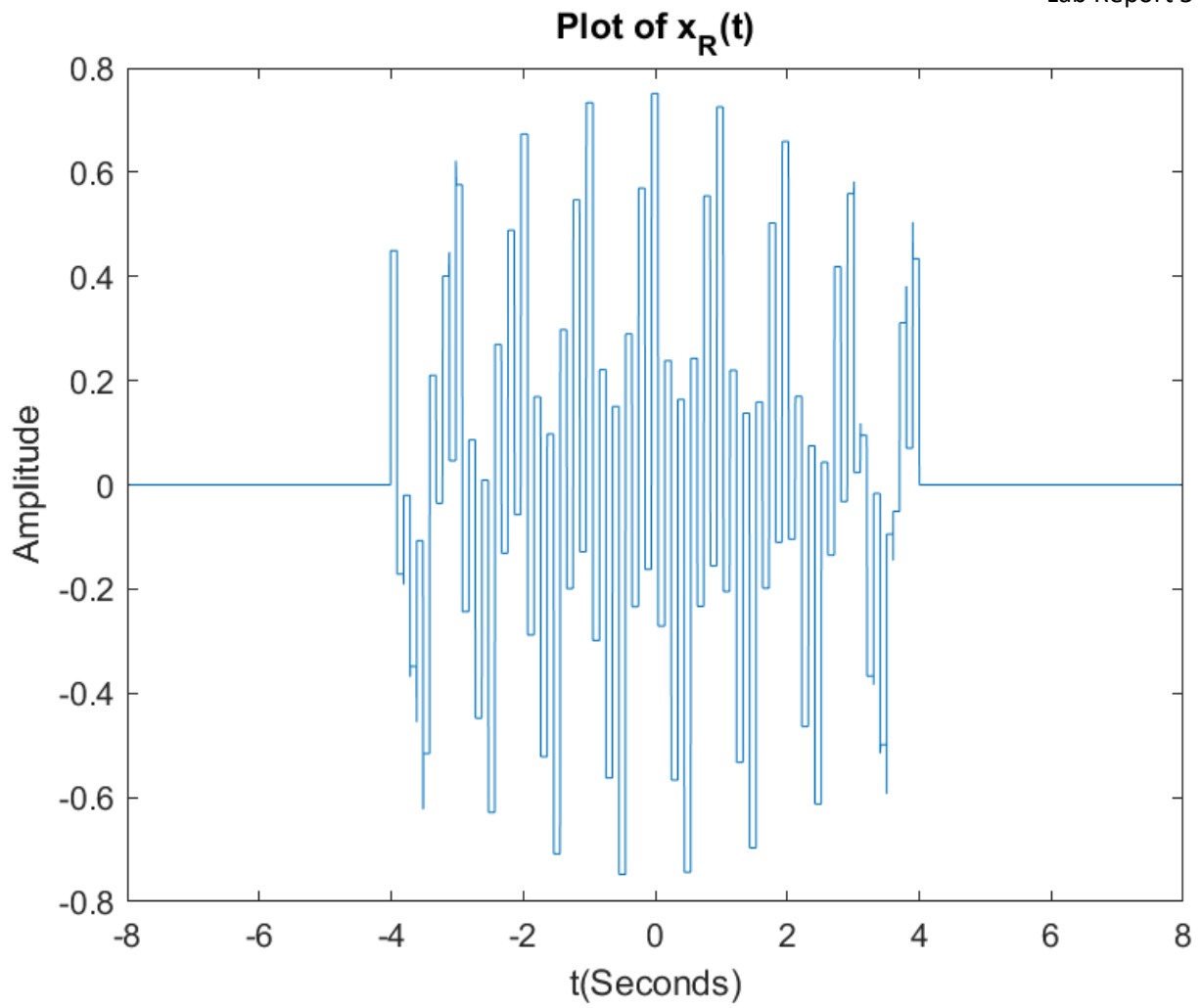




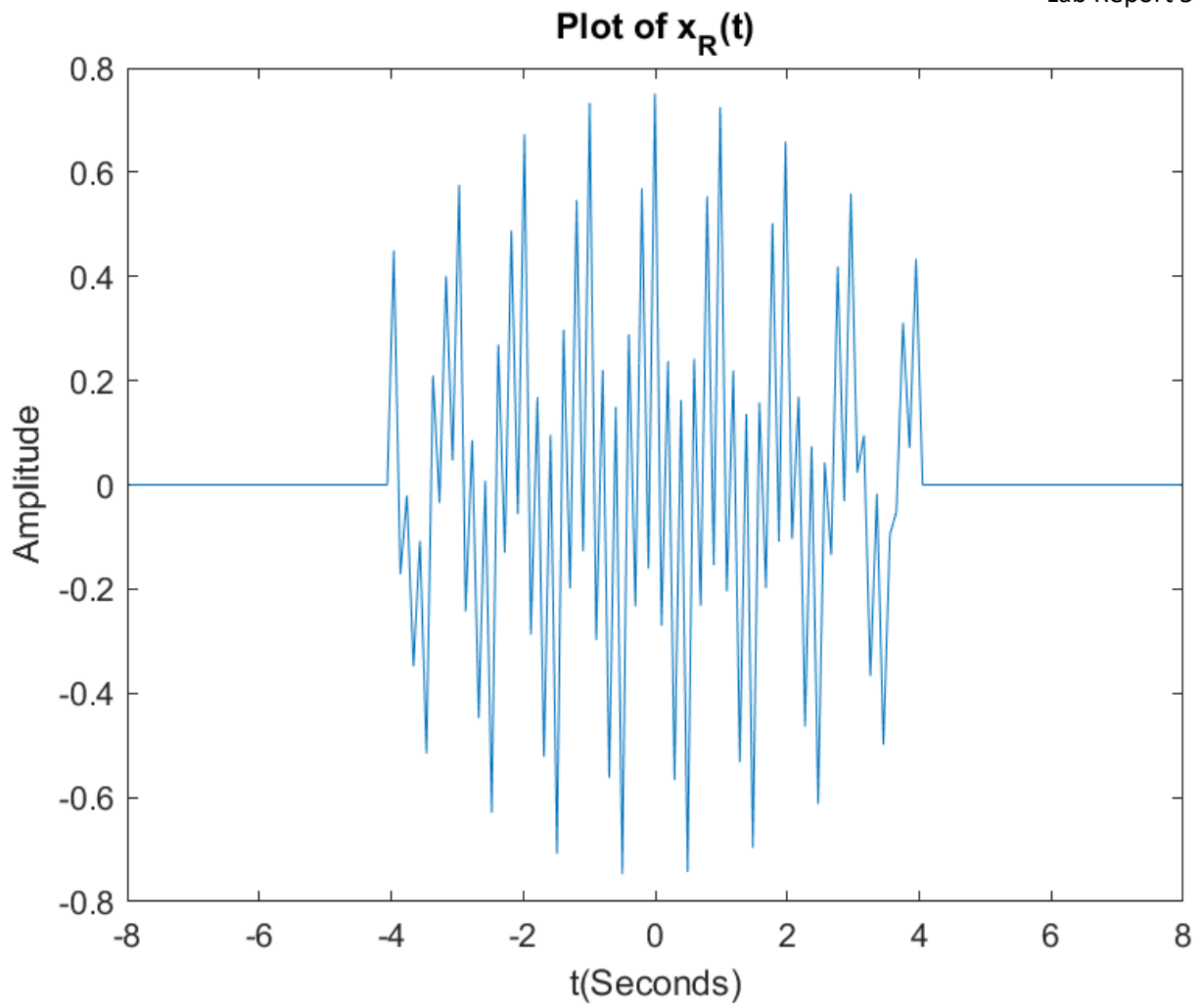
**Figure 19:** Plot of  $x_R(t)$  After Using Ideal Band - Limited Interpolation when  $T_s = 0.18 + 0.005 \cdot (D6 + 1)$ .



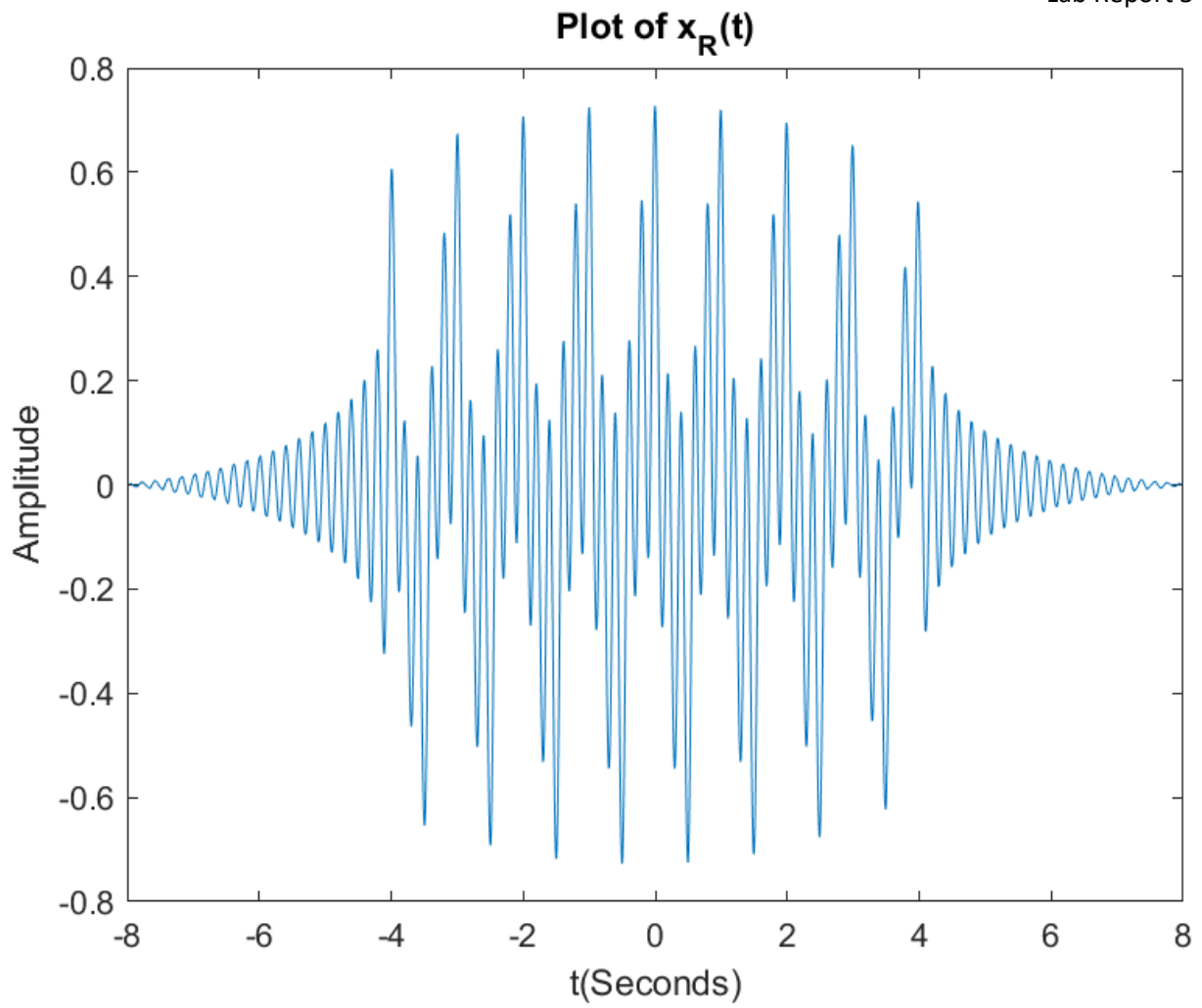
**Figure 20:** Plot of  $x(t)$  and  $x_{\text{sampled}}(t)$  in The Same Graph when  $T_s = 0.099$ .



**Figure 21:** Plot of  $x_R(t)$  After Using Zero - Order Hold Interpolation when  $T_s = 0.099$ .



**Figure 22:** Plot of  $x_R(t)$  After Using Linear Interpolation when  $T_s = 0.099$ .



**Figure 23:** Plot of  $x_R(t)$  After Using Ideal Band - Limited Interpolation when  $T_s = 0.099$ .



## Matlab Codes

```
%% Part 3 %%
dur = mod(21801985,9);
p_rect = generateInterp(0, dur/5, dur);
%figure; plot(t, p); xlabel('Time (Seconds)'); ylabel('Magnitude');

p_tri = generateInterp(1, dur/5, dur);
%figure; plot(t, p); xlabel('Time (Seconds)'); ylabel('Magnitude');

p_sinc = generateInterp(2, dur/5, dur);
%figure; plot(t, p); xlabel('Time (Seconds)'); ylabel('Magnitude');

%% Part 5 %%
Ts = 1 / (15 * (3 + (8 - 3) .* rand(1, 1)));

t_sampling = -4 : Ts : 4;

g = zeros(1, length(t_sampling));
g(find(t_sampling == -1) : find(t_sampling == 0) - 1) = 1;
g(find(t_sampling == 0) + 1 : find(t_sampling == 1)) = -2;
%stem(t_sampling, g);

g2 = zeros(1, length(t_sampling));
g2(t_sampling > -1 & t_sampling < 0) = -1;
g2(t_sampling > 0 & t_sampling < 1) = 1;
%stem(t_sampling, g2);

%gR_w_rect = DtoA(0, Ts, 8, g2); xlabel('Time (Seconds)'); ylabel('g_R(t)');
title('Zero - Order Hold Interpolation');
%gR_w_tri = DtoA(1, Ts, 8, g2); plot(linspace(-4, 4, length(gR_w_tri)), gR_w_tri);
xlabel('Time (Seconds)'); ylabel('g_R(t)'); title('Linear Interpolation');
%gR_w_sinc = DtoA(2, Ts, 8, g2); xlabel('Time (Seconds)'); ylabel('g_R(t)');
title('Ideal Band - Limited Interpolation');

%% Part 6 %%
D6 = rem(21801985,6);
% Ts = 0.005 * (D6 + 1);
%Ts = 0.2 + 0.01 * D6;
%Ts = 0.18 + 0.005 * (D6 + 1);
%Ts = 0.099;
t = -4 : Ts/1000 : 4; sam_t = -4 : Ts : 4;
x_t = (0.3) * cos(2 * pi * t + pi / 4) + (0.1) * cos(6 * pi * t + pi / 8) + (0.4)
* cos(10 * pi * t + 1.2);
x_sam = (0.3) * cos(2 * pi * sam_t + pi / 4) + (0.1) * cos(6 * pi * sam_t + pi / 8)
+ (0.4) * cos(10 * pi * sam_t + 1.2);
hold on; plot(t, x_t); stem(sam_t, x_sam, 'Blue'); hold off;
figure; DtoA(0, Ts, 8, x_sam); title('Plot of x_R(t)'); xlabel('t(Seconds)');
ylabel('Amplitude');
figure; DtoA(1, Ts, 8, x_sam); title('Plot of x_R(t)'); xlabel('t(Seconds)');
ylabel('Amplitude');
figure; DtoA(2, Ts, 8, x_sam); title('Plot of x_R(t)'); xlabel('t(Seconds)');
ylabel('Amplitude');
```

%% Functions %%

```
function xR = DtoA(type, Ts, dur, Xn)
    p = generateInterp(type, Ts, dur);
    len_p = length(p); len_x = length(Xn); len_r = floor(len_p * (1 + (len_x - 1) *
Ts/dur));
    tot = floor(len_r / (len_x - 1 + dur/Ts));
    xR = zeros(1, len_r);
    t = linspace(-(dur + (len_x - 1) * Ts) / 2, (dur + (len_x - 1) * Ts) /
2, len_r);
    for i = 0 : len_x - 1
        xR(tot * i + 1 : tot * i + len_p) = xR(tot * i + 1 : tot * i + len_p) + Xn(i + 1)
        * p;
    end
    plot(t, xR);
end
function p = generateInterp(type, Ts, dur)
    t = (-dur/2 : Ts/1000 : dur/2 - Ts/1000);

    if (type == 0)
        p = zeros(1, length(t));
        p(t >= -Ts/2 & t < Ts/2) = 1;
    elseif (type == 1)
        p = zeros(1, length(t));
        p(t > -Ts & t < Ts) = 1 - abs(t(t > -Ts & t < Ts))/Ts;
    elseif (type == 2)
        p = sin(pi*t/Ts)./(pi*t/Ts);
        p(t==0) = 1;
    end
end
```