

Utilizing Parallel Workers: LLVM’s Vectorization Plan

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Abstract

Modern SIMD processors provide various vector registers and ISAs for programmers to utilize. However, manually vectorizing code can be time-consuming, so compilers look to auto-vectorize code for better performance. LLVM, as a widely used compiler toolchain, could only auto-vectorize basic scalar code. Intel proposed a comprehensive refactoring of the underlying system to enable LLVM’s auto-vectorization to support more complex optimizations. The suggested Vectorization Plan (VPlan) architecture would be more modular and scalable. Since then, significant efforts have been made to implement this new system. Today, VPlan is already actively involved in vectorizing innermost loops. Other areas, such as outer loop vectorization, are also in development. In this paper, we introduce VPlan and summarize its latest development results.

1 Introduction

Modern CPUs are often equipped with multiple different vector registers. These registers are nowadays as wide as 512 bits, allowing for the processing of multiple data streams at once (SIMD). By batching multiple values together in one register, different ISAs like Intel AVX or ARM SVE allow the execution of the same instruction for all values in a vector register simultaneously. Utilizing this leads to significant performance improvements over the scalar equivalent most of the time.

However, manual code vectorization can quickly become time-consuming, especially when supporting different CPU architectures. Modern compilers aim to automatically transform scalar code to use vectorization when applicable.

As one of the most widely used compilation frameworks, LLVM [5] has implemented and refined its auto-vectorization over many years. It provides two different Vectorizers, one for innermost loops

(LoopVectorizer) and one for super-word parallelism (SLPVectorizer) [17].

This system, however, had quite a few limitations, as the loop vectorizer could only handle innermost loops and neither outer loops, complex control-flow, nor non-inlined functions. Additionally, while multiple different vectorizations for the same scalar code would be possible, the current vectorizers working directly on the LLVM IR could not model and compare the costs of such different vectorization approaches.

With these limitations in mind, Intel started an ongoing refactorization effort to migrate LLVM’s auto-vectorization pipeline to utilize a more abstract Vectorization Plan (VPlan) [15, 18]. The final goal would be to unite LLVM’s auto-vectorization in a single flexible system capable of optimizing SLPs, inner, and nested loops with complex control-flow.

The auto-vectorization pass would create multiple different VPlans based on initial legality checks. Each VPlan represents a different vectorization approach, by modeling the underlying scalar control flow with its own abstracted vectorized version. Different VPlan-to-VPlan transformations can then optimize these abstracted control-flows based on a cost model. After that, the best VPlan, and with it, the best vectorization approach is chosen by the cost model. This VPlan is then executed by going over its own vectorized control flow representation and materializing it back into the underlying LLVM IR.

LLVM’s VPlan is currently being integrated into the existing Loop Vectorizer and is already modeling most inner loop vectorizations and transformations [4]. Vectorization for outer loops is also in development and can be enabled by setting the `-enable-vplan-native-path` feature flag [1, 3]. In the future, the plan will be to merge both of these loop vectorization paths into one. Merging the existing SLP Vectorizer with VPlan is also planned.

```

1  for (int i = 0; i < N; i++) {
2      if (z[i]) {
3          x[i] += y[i];
4      }
5  }

```

Figure 1. A code snippet of a simple loop that would be vectorized over the variable i . The conditional branch would be flattened into a masked addition. The mask would be generated based on $z[i]$.

The rest of this paper is organized as follows. First, we explain different vectorization strategies and constraints in general and describe the original auto-vectorization approach in LLVM. Section 3 then introduces the new VPlan approach, focusing on its most important individual components, and gives an outlook on future developments. In Section 6, we highlight work related to LLVM’s auto-vectorization. Concluding, we summarize VPlan, its current state, and its potential future.

2 Background

2.1 Vectorization Strategies

In general, vectorization techniques can be separated into different categories:

Inner Loop Vectorization Innermost loops are loops whose body’s control flow does not contain any more loops. Vectorization of these loops is more straightforward as the only option to vectorize is over the loop’s induction variable.

There are various ways to transform the control flow of a loop to accommodate operating on widened vector registers. Figure 1 shows an example of an if-conversion. Some more examples can also be found in LLVM’s Auto-Vectorization Documentation [17].

Super-Word Parallelism (SLP) Vectorization SLP Vectorization vectorizes similar independent sequential instructions. This can often be seen after a loop has been partially or fully unrolled. The resulting similar scalar instructions might then be vectorized later by an SLP vectorizer.

Outer Loop Vectorization Outer loop vectorization focuses on control flow with nested loops. Such control flow often presents more challenges for auto-vectorization, as one could vectorize over the outer

```

1  for (int i = 0; i < N; i++) {
2      float sum = 0;
3
4      for (int j = 0; j < 6; j++) {
5          sum += y[j][i] * z[j];
6      }
7
8      x[i] = sum;
9  }

```

Figure 2. A code snippet of a nested loop where it would be beneficial to vectorize over the outer loop. The inner loop has a trip count (6) that is too low to vectorize. Additionally, the memory access pattern of y would be consecutive compared to scattered when vectorizing over i instead of j .

loop, inner loop, or a mix of both, representing a hybrid/multi-dimensional vectorization approach. Finding the best legal vectorization can therefore be more difficult.

Figure 2 shows a nested loop code snippet where vectorization over the outer loop would be beneficial.

Function Vectorization Function vectorization refers to the vectorization of entire functions. A loop might contain a non-inlined function call, passing data related to the iteration variable. During auto-vectorization, this call could be replaced with a call to a newly constructed function with the same semantic control-flow but operating on multiple values at once through vector registers.

2.2 Vectorization Legality

Not all loops can be vectorized. There are various factors that can ultimately hinder any vectorization attempts.

Some of the most common vectorization barriers are data dependencies. As the vectorized version of a code executes for Vectorization Factor (VF) N data streams simultaneously, it inherently changes the order of operations. To guarantee that the semantics of the code do not change, all operations on these N data streams must, generally, be independent. The simplest case where this is not provided is when the i -th loop iteration depends on any of the $(i - N)$ -th previous iterations.

While explicit data dependencies are easier to see, a simple loop, as in Figure 1, could carry an

implicit dependency in line 3 if the `x` and `y` point to overlapping memory regions (pointer aliasing).

Not all data dependencies directly hinder any vectorization [19]. An exception can, for example, sometimes be made for reduction idioms, as seen in the inner loop in Figure 2, where `sum` would be a reduction variable.

Uncountable loops, meaning loops where the total iteration count cannot be determined before the loop is executed, can often not be vectorized. This is because their exit condition usually depends on the loop's body itself, making it impossible to pre-determine how many vector lanes are needed for the next loop iteration when executing.

Finally, some instructions do generally not have a direct vectorized instruction equivalent. For example Integer division, commonly implemented using the *Newton-Raphson method*, is already a complex and iterative operation on modern CPUs. Applying this algorithm to multiple data elements in a single vector register would result in even more implementation complexity and is thus considered not worthwhile in most cases. Workarounds for some specialized cases do exist [10].

2.3 Vectorization Costs

While vectorizing a given control flow may not be legal, the vectorized code sometimes performs worse than its scalar equivalent.

Some control flow transformations that seem beneficial at compile time might reveal a performance bottleneck at runtime. Considering the code snippet from Figure 1, it might be that almost all `z[i]` evaluate to false at runtime. The branch predictor of a CPU would then be able to guess the correct branch in the scalar code. The vectorized version would always load the `y[i]` into memory only for the addition to be masked away. Different approaches to avoid such runtime penalties are branch-on-superword-condition code (BOSCC) [11, 16] or active-lane consolidation (ALC) [12, 13].

The actual performance of a vector instruction also heavily depends on the ISA and its hardware implementation. For example, gather, scatter, shuffle, and permutation instructions are typically slow. Control flow with many non-adjacent memory accesses or operations that combine different vector elements from the same register (horizontal reductions) can thus decrease vectorization performance.

Additionally, the vectorized code size will always be larger than the scalar equivalent. This is due to many factors: (1) The transformed control flow often includes more instructions. (2) As the loop trip count might not be a perfect multiple of the Vectorization Factor, a scalar epilogue/remainder of the loop might be used to handle the tail iterations. (3) Various runtime checks might be inserted throughout the vectorized control flow to handle, for example, pointers to overlapping memory regions, in which case the scalar version of the loop must be executed due to unclear data dependencies.

2.4 Auto-Vectorization in LLVM

LLVM implements two different vectorizers for auto-vectorization, LoopVectorize (LV) and SLPVectorize [2, 17]. Auto-Vectorization is part of LLVM's middle-end and runs after module simplification. These vectorizers take scalar LLVM IR and transform it into optimized vectorized LLVM IR.

SLPVectorize is a SLP vectorizer working on straight-line code (non-loops). It works by analyzing the code bottom-up, keeping track of dependencies and grouping similar independent scalar instructions together if possible. Based on a cost model SLPVectorize then decides to vectorize these groups.

LoopVectorize was designed to focus only on vectorization of innermost loops [14]. When starting with an initial scalable loop in IR, it would first run a legality phase to check whether and how it is legal to vectorize the loop. This phase would produce different artifacts, such as if and what runtime aliasing checks would be required. Then, the cost model ran next, creating more cost-based artifacts based on the underlying scalar IR and the legality artifacts. Lastly, the transformation phase would vectorize the IR in one go based on all the previously produced artifacts.

However, this rigid flow of LoopVectorize presented a challenge. Extending LV to include outer loop and nested loop vectorizations would have been difficult, as LV was designed to flatten a loop's control flow into a single basic block. Producing and considering more and more artifacts when trying to transform the scalar loop into a vectorized one all at once also did not scale well.

As a potential solution, Intel proposed a long-term effort to refactor LLVM's whole auto-vectorization using a more modular and flexible system called Vectorization Plan (VPlan) [15].

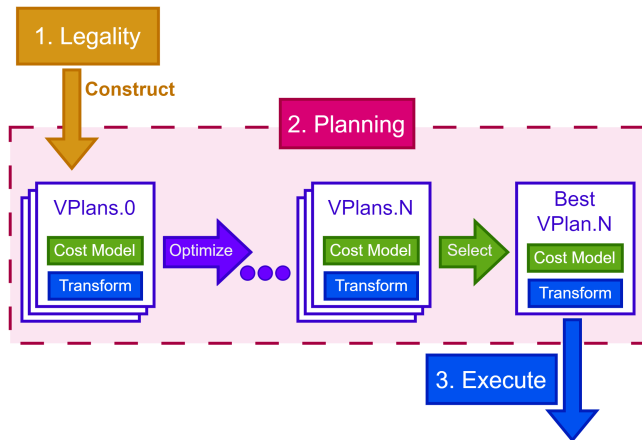


Figure 3. The planned future architecture for auto-vectorization in LLVM. The optimization step in phase 2 would iteratively apply VPlan-to-VPlan transformations.

3 LLVM’s Vectorization Plan

Intel’s initial VPlan proposal aimed to unite any auto-vectorization systems (SLP, Inner-/Outer-Loop, Whole-Function) into a single flexible system [14, 15, 21]. This system would use VPlans to represent different vectorization approaches, abstracting away from the underlying scalar loop IR using its own hierarchical control flow graph (H-CFG). This allows iteratively exploring different optimization decisions by performing transformations on this CFG without modifying any LLVM IR. Each VPlan could to calculate its cost and execute itself, materializing the vectorization approach back into LLVM IR.

This planned system is shown in Figure 3. At first, the Legality Phase would check if the scalar code would be legal to vectorize at all, and if so, initial VPlans would be constructed. In the following Planning Phase, these initial VPlans would be optimized using various VPlan-to-VPlan transformations [3]. The VPlan’s cost model would supervise those transformations. Finally, the best VPlan would be chosen and executed, modifying the underlying IR.

3.1 VPlan Structure

Before explaining how far this system has been implemented in LLVM, we will review the different elements of a VPlan in more detail.

The purpose of a single VPlan object is to model a candidate for vectorization. Such a single candidate can potentially represent multiple different vectorized loops. For example, one VPlan might

model a general vectorization approach for various Vectorization Factors (VFs) and Unroll Factors (UFs).

H-CFG This is achieved by introducing a new layer of abstraction from the underlying loop’s scalar IR. Each VPlan stores its own Hierarchical-CFG (H-CFG) modeling the vectorization candidate. This control-flow graph and its components are the main elements of a single VPlan. It is hierarchical in that a single node of this graph can be a complete subgraph, representing more complex nested behavior. Specifically, any node of this H-CFG is one of three types:

- **VPBasicBlock** stores a list of **VPRecipes** similar to the LLVM IR’s **BasicBlock** holding a list of IR Instructions.
- **VPRegionBlock** represents a subgraph with a single VP entry node and a single VP exit node. A **VPRegionBlock** can be marked to replicate its subgraph $\text{VF} * \text{UF}$ times when executing. This is useful for modeling scalarized or predicated instructions within the final vectorized loop body.
- **VPIRBasicBlock** is a special **VPBasicBlock** that wraps an underlying IR **BasicBlock**. These nodes help model the scalar parts around the final vectorized loops, such as the loop preheader and the epilogue loop.

Figure 4 shows the loop part of the scalar IR for the code example of Figure 1. Comparatively, Figure 5 shows the loop part of the H-CFG of a VPlan that models the vectorization approach described in Figure 1.

Recipes **VPRecipes** can be seen as instructions of an IR specialized for auto-vectorization. A single **VPRecipe** inside a VPlan is based on zero or more LLVM IR instructions of the underlying scalar IR and will materialize into one or more LLVM IR instructions when executed.

There are many different types of **VPRecipes**, most notably:

- **VPReplicateRecipe** will replicate one IR instruction either once (**CLONE**) or $\text{VF} * \text{UF}$ times (**REPLICATE**) into the vectorized IR when executed.
- **VPWidenRecipe** will **WIDEN** one IR instruction into a vector-equivalent when executed.

State of LLVM's Vectorization Plan

```

for.body:
  %indvars.iv = phi i64 [ 0, %for.body.preheader ],
                    [ %indvars.iv.next, %for.inc ]
  %arrayidx = getelementptr inbounds i8, ptr %z, i64 %indvars.iv
  %0 = load i8, ptr %arrayidx, align 1
  %tobool.not = icmp eq i8 %0, 0
  br i1 %tobool.not, label %for.inc, label %if.then

if.then:
  %arrayidx2 = getelementptr inbounds float, ptr %y, i64 %indvars.iv
  %1 = load float, ptr %arrayidx2, align 4
  %arrayidx4 = getelementptr inbounds float, ptr %x, i64 %indvars.iv
  %2 = load float, ptr %arrayidx4, align 4
  %add = fadd float %1, %2
  store float %add, ptr %arrayidx4, align 4
  br label %for.inc

for.inc:
  %indvars.iv.next = add nuw nsw i64 %indvars.iv, 1
  %exitcond.not = icmp eq i64 %indvars.iv.next, %wide.trip.count
  br i1 %exitcond.not, label %for.cond.cleanup, label %for.body

```

Figure 4. The scalar IR for the main loop section of the conditional loop depicted in Figure 1. Note that `getelementptr inbounds` was abbreviated to `getelmptptr inbs`.

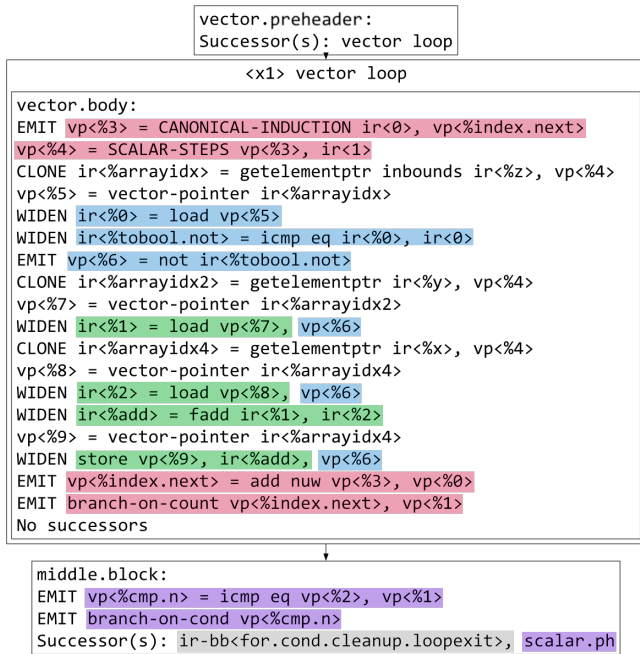


Figure 5. The vectorized loop section of the hierarchical CFG of a VPlan modeling the conditional loop depicted in Figure 1. Surrounding `VPIRBasicBlock`-nodes are omitted. Some predefined values are $vp\langle\%0\rangle = VF * UF$; $vp\langle\%1\rangle =$ vector-trip-count; $vp\langle\%2\rangle =$ original trip-count.

- `VPIRInstruction` has no underlying IR instruction it is based on and is used to model newly needed instructions for the vectorized IR. When executed it will `EMIT` one or more new IR instructions.

The `VPRecipes` in Figure 5 have a `PREFIX` in front of them indicating their type. Additionally instructions/recipes of the same color between Figure 4 and Figure 5 are related. The only recipes in our example VPlan CFG that do not semantically model any instructions found in the scalar IR are from the `middle.block` (purple). This block decides if the scalar epilogue loop will be executed following the vectorized loop.

Transformations Another main benefit of the modular VPlan system is that most vector-optimization cases can be directly implemented as standalone VPlan-to-VPlan transformations. A VPlan-to-VPlan transformation is a static method that either transforms a given VPlan or creates a new VPlan based on a given VPlan. The analysis for these transformations can also be done directly on the VPlan via its `VPRecipes`.

4 State of VPlan (LLVM 19.1.4)

In its current state, VPlan is already deeply integrated into LoopVectorize (LV) and is used to model, optimize, and execute vectorization of innermost loops [4, 14, 18]. While outer loop vectorization via VPlan has already seen some development, any outer loop vectorization features are still experimental and must be explicitly enabled by passing the `-enable-vplan-native-path` feature flag [1, 3].

To better understand how VPlan is already being used in LLVM, we will now follow along the LoopVectorize pass and summarize its key components.

4.1 Phase 1: Legality

The main part of this phase is checking whether it is even legal to optimize a given loop. In addition to the general vectorization legality concepts mentioned in Section 2.2, LV has a several extra conditions to check.

Some of the most important legality checks done are:

- The scalar loop's control flow must not contain indirect branches or multiple back-edges. An indirect branch is a branch that jumps to a value evaluated at runtime. A back-edge in a loop is an edge from the loop back to it.
- Loops with non-linear control flow must be if-convertible. This means any branch or switch

statement must not exit the loop. All instructions of such a block can be executed speculatively (e.g. via masking)

- Loop-carried dependencies must be vectorizable (see Section 2.2). In LV this means explicitly that such a value must *at least* either be an induction variable, a reduction variable, or a fixed-order recurrence.
- The loop must not contain function calls outside of standard math library calls.
- The number of runtime checks to guarantee no pointers used by recurrences overlap must not be too high.

One can find more details about these legality checks and their implementations by looking at the LLVM codebase under `LoopVectorizationLegality::canVectorize`.

4.2 Phase 2: Planning

After the Legality Phase has analyzed the scalar loop, initial VPlans are constructed. A VPlan is initialized by creating the H-CFG skeleton building blocks like preheaders, a region block for the vector loop, a middle block with the potential runtime check for the scalar epilogue loop, and a block for the scalar loop. After the H-CFG has been created, the scalar LLVM IR is iterated in topological order, and each scalar IR instruction is transformed into a `VRecipe`. After modeling each scalar IR instruction with a `VRecipe`, several VPlan transformations are executed, optimizing the initialized VPlan.

After the initial VPlans have been optimized, the best Vectorization Factor is computed. This is done by comparing all generated VPlans for all their possible VFs and choosing the most profitable one. If this step computes an optimal VF of 1, any vectorization is not profitable compared to the scalar version.

Cost Model Currently, LV and VPlan still mostly rely on the old cost model. This legacy cost model derives costs based on the scalar LLVM IR instructions or, if applicable, their vectorized equivalent. This is suboptimal for VPlan as VPlans work on `VRecipes` abstracted away from the underlying IR. These costs per instruction are then generally just lookup tables influenced by the underlying compile target.

4.3 Phase 3: Execution

After the best VPlan has been chosen, it is executed (`LoopVectorizationPlanner::executePlan`). For this VPlan, some final transformations are run depending on a specifically chosen VF and UF. First, a vectorized code skeleton is created in the IR, and then the VPlan is executed. Upon execution, the H-CFG of the VPlan is walked, and each node is executed, which in turn executes all of its `VRecipes` in order.

Figure 6 shows the general CFG of a vectorized loop in LLVM and, for branches, the general branch condition per block.

If the epilogue loop could be further vectorized, it would be in a second pass by creating VPlans, finding the best one, and executing it.

5 Future of VPlan

Many of the VPlan internals and surrounding systems are still in active development. To stay up-to-date with the latest developments regarding auto-vectorization in LLVM, one can follow the Community Forum¹ or attend the monthly online meetings².

5.1 VPlan and Integration with LV

Setting up and integrating the VPlan structure into LV has seen tremendous effort over the last few years. Florian Hahn presented future directions for VPlan [4], which mostly revolve around transforming more LV-based decisions into explicit VPlan-to-VPlan transformations. Additionally, the legacy LV cost model still influences many cost model-related decisions. However, the transition to a VPlan-based cost model has already started. This new model would derive costs based on `VRecipes` directly instead of the abstracted scalar IR instructions.

5.2 Outer Loop Vectorization

Development around outer loop vectorization has slowed as the focus shifted to VPlan internals and integration into LV. The inner and outer loop paths are still separated, and the experimental `-enable-vplan-native-path` flag must be set to activate any outer loop vectorization. Further development

¹<https://discourse.llvm.org/c/ir-optimizations/loop-optimizations/62>

²<https://discourse.llvm.org/t/monthly-vectorizer-online-sync-up/78978/3>

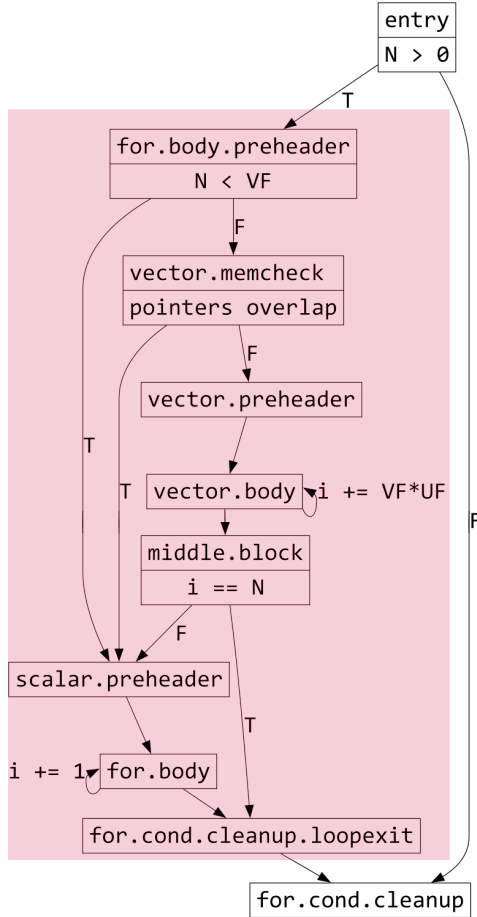


Figure 6. The generalized CFG for a vectorized loop with trip count N , iteration variable i , vectorization factor VF , and unroll factor UF in LLVM. A VPlan would so far explicitly model the red-highlighted region in its H-CFG. If a node branches, the condition is stated in the body, and the two possible path edges are marked with T (True) and F (False).

of the outer loop path and eventually merging it with the innermost loop path is planned.

5.3 Merging with SLP Vectorize

Merging the existing SLP Vectorizer with the current VPlan infrastructure is in the early planning phase.

5.4 Function Vectorization

There is currently no active development for whole-function vectorization in the llvm-project’s upstream.

6 Related Work

Next to the main llvm-projects upstream, many projects are using or extending the LLVM toolchain.

One such project that tries to enable auto-vectorization support for inner/outer loops and whole-functions is the region vectorizer (RV) from the University Saarland [20]. The idea is that all the different vectorization strategies shown in Section 2.1 can be generalized into a single vectorization approach.

For example, function vectorization can be transformed into loop vectorization by creating a loop around the function’s body and vectorizing it and vice versa. The same applies to SLP Vectorization and loop vectorization by unrolling a loop.

RV aims to have such a generalized auto-vectorization by vectorizing over *regions*. A region is defined as any control flow with a single entry and one or more non-divergent exits. Non-divergent exits mean that control flow must not diverge to different exits starting from the same entry. Such a region can then be, for example, an inner/outer loop, function, or SLP code [6, 7].

To achieve this, RV implements partial control flow linearization [8] and a divergence analysis that can handle unstructured CFGs. There has been an effort to partially implement this control flow linearization and divergence analysis into LLVM’s upstream [7, 9].

7 Summary and Future Work

In conclusion, VPlan has been in active development for several years now. When compiling with LLVM, VPlans are used to model different vectorization approaches. They do so by adding a new layer of abstraction over the underlying LLVM IR. This VPlan layer uses **VPRecipes** to model vectorization-specific instructions. This abstraction allows for efficiently exploring many optimization decisions simultaneously, keeping the underlying implementation flexible and modular. In the end, a cost model currently working based on LLVM IR instead of **VPRecipes** is used to compare different VPlans and choose the most optimal one. Finally, this chosen VPlan is executed, materializing its **VPRecipes** back into LLVM IR.

Outer loop vectorization support via VPlan is still experimental and separated from the inner loop LV integration. In the near future, development on

outer loop vectorization will continue, and merging it with LV's VPlan path is planned.

Active development of other approaches, such as SLP and whole-function vectorization based on the VPlan architecture, has yet to be started.

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