

The goal is to compute a decimal quotient using integer division. The following outlines the logic to do so:  
Let  $Q_{\text{float}}$  be the desired quotient we want, and let  $Q_{\text{int}}$  be the integer quotient. We can then write the formula:

$$Q_{\text{float}} = N/D = Q_{\text{int}} + R/D$$

In order to find the value of  $R/D$  in terms of decimal value, we can multiply  $R$  by 100, and then continue dividing by  $D$ . This should give us 2 more digits to place after the decimal point.

$$Q_{\text{float}} = Q_1Q_2.R_1R_2 \text{ where } Q_i = \text{digit of } Q_{\text{int}} \text{ and } R_i = \text{digit of remainder}$$

Furthermore, we can round the decimal value by using the remainder  $R^*$  of  $R/D$ . We'll define a rounding cut  $\rho$  such that:

$$R^* \leq \rho \implies \text{round down}$$

$$R^* > \rho \implies \text{round up}$$

In order to determine the value of  $\rho$ , let's remember that we round up when  $R^* \geq D/2$ . If  $D$  is even, then it is possible for that expression to hold true. If  $D$  is odd however, the expression can not hold true because  $R^*$  must be an integer. However, subtracting  $D - 1$  gives us the largest integer less than  $D$  that is divisible by 2. Dividing this new value should thus give us the maximum remainder of  $D$  that we can round down with.

$$\rho = \begin{cases} \frac{D-1}{2} & \text{if } D \text{ is odd.} \\ \frac{D}{2} - 1 & \text{if } D \text{ is even.} \end{cases}$$