1. Write the basic feasible solutions of the following LP:

For the following questions, assume we are given an LP in equational form: maximize  $c^Tx$  subject to Ax = b and  $x \ge 0$ . Assume that the LP is feasible and A is an  $m \times n$  matrix with m linearly independent rows.

- 2. Suppose x and y are feasible solutions. Let w = x y and  $K = \{i \mid w(i) \neq 0\}$ . Show that the set of columns of A indexed by K are linearly dependent.
- 3. Prove the following statement. Let x be a basic feasible solution. Let y be a feasible solution satisfying: y(i) = 0 iff x(i) = 0. Then x = y.
- 4. Show that the statement in the previous question does hold when x is not a basic feasible solution.