

Find the binary for the following decimal in 32-bit single precision IEEE754 format:

22.34

Step 1: Convert the given decimal into binary form

Exponent: Divide 22 by 2

Quotient	Remainder
11	0
5	1
2	1
1	0

Mantissa: Multiply 0.34 by 2

0.34*2 =	0
0.68*2 =	1
0.36*2 =	0
0.72*2 =	1
0.44*2 =	0
0.88*2 =	1
0.76*2 =	1
0.52*2 =	1
0.04*2 =	0
0.08*2 =	0
0.16*2 =	0
0.32*2 =	0
0.64*2 =	1
0.28*2 =	0
0.56*2 =	1
0.12*2 =	0
0.24*2 =	0
0.48*2 =	0
0.96*2 =	1
0.92*2 =	1

Decimal:	22	.	34
Binary:	10110	.	01010111000010100011...

Step 2: Represent the obtained binary in scientific notation

In scientific notation, a float binary is written in a form so that it begins with "1."  
Hence, we must move the point 4 places to the *left* in the obtained binary.

We have,	10110	.	01010111000010100011...
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After bit-shifting,

1	.	01110	01010111000010100011... *2^4
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Step 3: Convert the scientific notation into 32-bit single precision IEEE754 format

We need to represent the power of 2, 4 in our case, in bits. As per the IEEE rules, we must add a *bias* to the power, and then represent the resultant in bits. In 32-bit format,

Bias: 127

=> Exponent = 127 + 4 = 131

Binary of 131:	Quotient	Remainder
	65	1
	32	1
	16	0
	8	0
	4	0
	2	0
	1	0

Now we can represent the exponent in 8 bits as per the 32-bit IEEE format.

1	0	0	0	0	0	0	1	1
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So in single precision, 22.34 is represented as:

Sign	Exponent	Mantissa
0	1000011	01100101011100001010001
		01100101011100001010010

Rounded!

Sign	0			
	1			
Exponent	0			
	0			
	0			
	0			
	0			
	1			
	1			
	0	2 <sup>-1</sup>	0	
Mantissa	1	2 <sup>-2</sup>	0.25	
	1	2 <sup>-3</sup>	0.125	
	0	2 <sup>-4</sup>	0	
	0	2 <sup>-5</sup>	0	
	1	2 <sup>-6</sup>	0.015625	
	0	2 <sup>-7</sup>	0	
	1	2 <sup>-8</sup>	0.00390625	
	0	2 <sup>-9</sup>	0	
	1	2 <sup>-10</sup>	0.0009765625	
	1	2 <sup>-11</sup>	0.00048828125	
	1	2 <sup>-12</sup>	0.000244140625	
	0	2 <sup>-13</sup>	0	
	0	2 <sup>-14</sup>	0	
	0	2 <sup>-15</sup>	0	
	0	2 <sup>-16</sup>	0	
	1	2 <sup>-17</sup>	0.00000762939453125	
	0	2 <sup>-18</sup>	0	
	1	2 <sup>-19</sup>	0.0000019073486328125	
	0	2 <sup>-20</sup>	0	
	0	2 <sup>-21</sup>	0	
	1	2 <sup>-22</sup>	0.0000002384185791015625	
	0	2 <sup>-23</sup>	0	
			<hr/>	
			0.3962500095367431640625	Sum

#### Cross-verification:

The above sum is in IEEE format, so it must be converted to decimal. The standard formula for the same:

$$(-1)^{\text{sign}} * (1 + \text{mantissa}) * 2^{\text{exponent}}$$

$$\begin{aligned}
 \Rightarrow & (-1)^0 * (1 + 0.3962500095367431640625) * 2^4 \\
 = & 1.3962500095367431640625 * 16 \\
 = & \mathbf{22.340000152587890625}
 \end{aligned}$$