## 2021

## ECONOMICS — HONOURS

**Seventh Paper** 

(Group - A)

Full Marks: 50

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

Section - A

(Marks: 20)

- 1. Answer any five questions:
  - (a) Define Type-I and Type-II error. Can you reduce both the errors simultaneously?
  - (b) Are the following linear regression models? Give reasons.

(i) 
$$Y_i = \alpha + \sqrt{\beta}X_i + u_i$$

(ii) 
$$Y_i = \alpha X_i^{\beta} e^{u_i}$$

- (c) Show that if a regression line is fitted through origin, the sum of the residuals may not equal to zero.
- (d) A random sample  $x_1, x_2, \dots, x_n$  is drawn from an infinite population with variance  $\sigma^2$  and  $\bar{x}$  is the sample mean. Derive an unbiased estimator of  $\sigma^2$ .
- (e) A sample of size 25 drawn from a normal population with variance 81, produced a mean of 81.2. Find a 0.95 level of confidence interval for the population mean.

(Given that 
$$\frac{1}{\sqrt{2\pi}} \int_{1.96}^{\infty} e^{-z^2/2} dz = 0.025$$
).

- (f) Show that the square of Student's t-statistic with n degrees of freedom has an F-distribution with (1, n) degrees of freedom.
- (g) Discuss the method of least squares for computing trend in time series analysis.
- (h)  $Y_i = \hat{\alpha} + \hat{\beta}X_i + u_i$  where n = 10,

$$\sum X_i = 70$$
,  $\sum Y_i = 80$ ,  $\sum X_i^2 = 600$ ,  $\sum Y_i^2 = 734$ ,  $\sum X_i Y_i = 480$ 

Obtain the estimated value of  $\alpha$  and  $\beta$ .

2+2

4

4

Please Turn Over

## Section - B

(Marks: 30)

Answer any five questions.

2. Let x and y be two continuous random variables having joint probability density function:

$$f(x,y) = \begin{cases} 1 - \frac{x}{3} - \frac{y}{3}, & 0 \le x < 2, 0 \le y \le 1 \\ 0, & \text{otherwise.} \end{cases}$$

Obtain the marginal densities of x and y.

3+3

3+3

- 3. (a) What do you mean by a Minimum Variance Unbiased Estimator (MVUE)?
  - (b) Let  $T_1$  and  $T_2$  be statistics with expectations  $E(T_1) = 2\theta_1 + 3\theta_2$  and  $E(T_2) = \theta_1 + \theta_2$ . Find unbiased estimators of  $\theta_1$  and  $\theta_2$ .
- 4. Find the standard error of sample proportion in both SRSWR and SRSWOR.
- **5.** (a) A simple random sample of size 5 is drawn without replacement from a finite population consisting of 41 units. If the population standard deviation is 6.25, what is the standard error of sample mean?
  - (b) If  $X_1, X_2, \dots, X_n$ , be 'n' normally distributed variables having identical variances  $\sigma^2$  with mean 0, what form will the distribution of  $X_1^2 + X_2^2 + \dots + X_n^2 / \sigma^2$  take? Justify your answer.
- 6. Show that the least squares estimator of  $\beta$  in the model  $Y_i = \alpha + \beta X_i + u_i$  is linear and unbiased. Derive the variance of the estimator of  $\beta$ .
- 7. Find the maximum likelihood estimator of the mean of a Poisson population from a random sample of size n and show that it is unbiased. 4+2
- **8.** What assumptions are made regarding the error term in a Classical Linear Regression Model? What happens to the OLS estimators if homoscedasticity assumption is violated?

  3+3
- 9. Fit a straight line trend to the following data and obtain the trend value for 2004: 4+2

Year	1995	1996	1997	1998	1999	2000	2001	2002	2003
Average Monthly Profit (Million ₹)	6.3	7.4	9.3	7.4	8.3	10.6	9.0	8.7	7.9