

**2021**  
**MATHEMATICS HONOURS**  
**SEMESTER-1**  
**INTERNAL ASSESSMENT**  
**Full Marks of each Course:10**

*The figures in the margin indicate full marks.*  
*Symbols and notations used here carry their usual meaning.*  
*Candidates are required to give their answers in their own words as far as practical.*

**Course: CC1**  
**(Calculus, Geometry & Vector Calculus)**

Answer all the questions with proper justification:

5x2=10

1. If  $a, b, c$  are non-zero coplanar vectors then
  - (i) *the volume of the parallelopiped formed by them is 0*
  - (ii)  $a \times b = 0$  or  $b \times c = 0$  or  $c \times a = 0$
  - (iii)  $a.b = 0$  or  $b.c = 0$  or  $c.a = 0$
  - (iv) none of these
  - (v)
2. Equations of the planes parallel to z-axis are
  - (i)  $ax + cz + d = 0$
  - (ii)  $ax + by + d = 0$
  - (iii)  $by + cz + d = 0$
  - (iv)  $ax + by + cz = 0$ .
3. If a straight line makes angles  $\alpha, \beta, \gamma$  with the axes of co-ordinates, then  $\cos 2\alpha + \cos 2\beta + \cos 2\gamma$  is equal to
  - (i) -1, (ii) 1, (iii) 0, (iv) 2
4. Find  $\lim_{x \rightarrow 0} \left(1 + \frac{1}{x}\right)^x$ 
  - (i) 1 (ii) e (iii)  $1/e$  (iv)  $e^2$
5. The conic  $11x^2 + 4xy + 14y^2 - 26x - 32y + 23 = 0$  represents a/an
  - (i) Ellipse
  - (ii) Circle
  - (iii) Hyperbola
  - (iv) Parabola

**Course: CC2**  
**(Algebra)**

Answer all the questions with proper justification:

5x2=10

1. Let  $A$  and  $B$  be two finite sets of  $n$  elements and a mapping  $f: A \rightarrow B$  is injective. Then
  - (i)  $f$  bijective (ii)  $f$  is not onto (iii)  $f$  may not be onto (iv) none of these .

2. A relation  $\rho$  defined on, the set of all integers, by “ $a\rho b$  iff  $ab > 0$ ” for  $a, b \in \mathbb{Z}$ . Then  
 (i)  $\rho$  is equivalence relation (ii)  $\rho$  is reflexive but not symmetric (iii)  $\rho$  is not reflexive and transitive (iv)  $\rho$  is not reflexive but is symmetric and transitive
3. Consider the equation  $x^{100} - 100x + 99 = 0$ . Then the multiplicity of the root  $x = 1$  is  
 (i) 50, (ii) 3, (iii) 4, (iv) 2
4. The number of real roots of the equation  $x^6 + 3x^2 - 2x - 3 = 0$  is  
 (i) 6, (ii) 4, (iii) 2, (iv) 0
5. Let  $A$  be an  $m \times n$  matrix then which one is true ?  
 (i) Rank of  $A = m$  (ii) Rank of  $A = n$   
 (iii) Rank of  $A \leq \max \{m, n\}$  (iv) Rank of  $A \leq \min \{m, n\}$