

**2020**  
**MATHEMATICS - GENERAL**  
**SEMESTER-1**  
**Course: CC1/GE1**  
**INTERNAL ASSESSMENT**  
**Full Marks: 10**

*The figures in the margin indicate full marks .*

*Symbols and notations used here carry their usual meaning.*

*Candidates are required to give their answers in their own words as far as practical.*

Answer all the questions with proper justification:

5x2=10

- 1) The equation  $(x - a)^2 + (x - b)^2 + (x - c)^2 + (x - d)^2 = 0$ , where a, b, c, d are all real and not all equal has

- i) No real roots                      ii) three real roots  
 iii) only one real root      iv) two real roots

- 2) The rank of the matrix  $\begin{bmatrix} 1 & 1 & 2 \\ 3 & 4 & 5 \\ 4 & 8 & 0 \end{bmatrix}$  is

- i) 1                      ii) 2  
 iii) 3                      iv) 0

- 3) The order and degree of the differential equation  $\frac{d^2y}{dx^2} = \sqrt[3]{1 - \left(\frac{dy}{dx}\right)^4}$  are respectively

- i) 1, 2                      ii) 2, 3  
 iii) 3, 2                      iv) 2, 4

- 4) If the equation  $\alpha xy - 8x + 9y - 12 = 0$  represents a pair of straight line, values of  $\alpha$  are

- i) 1, 6                      ii) 2, 6  
 iii) 3, 5                      iv) 0, 6

- 5) Let  $f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right), & x \neq 0 \\ 0, & x = 0 \end{cases}$ , then which of the following is wrong

- i)  $f$  is continuous at  $x = 0$   
 ii)  $f$  is derivable at  $x = 0$   
 iii)  $f'$  is continuous at  $x = 0$   
 iv)  $f'$  is not continuous at  $x = 0$