

$O(n)$  ---> initialization

$O(n)$  ---creating priority queue

$u = \text{Extract-min}()$  ---->  $O(\log n)$  ----->  $O(n \log n)$

(in worst case)

For each  $u$ , inner for-loop will be executed  $d$  number of times where  $d$  is the degree of  $u$

In total, inner loop will be executed

$\sum_i d_i = O(m)$  where  $m$  = number of edges

$\text{decrease-key}()$  --- $O(\log n)$  ---->  $O(m \log n)$

Total running time =  $O(n \log n) + O(m \log n) = O((m+n) \log n)$

For loosely connected graph

$$m \cong n$$

Total running time =  $O((n+n) \log n) = O(n \log n)$