

```
int power(int x, unsigned int y)

{
    if (y == 0)
        return 1;
    else return(x* power(x,y-1));
}    ==>O(n)
```

$z = x^y = x^{y/2} * x^{y/2}$, if y is even

```
int power(int x, unsigned int y)
{
    if (y == 0)
        return 1;
    else if (y % 2 == 0)
        return power(x, y / 2) * power(x, y / 2);
    else
        return x * power(x, y / 2) * power(x, y / 2);
}
```

$T(n) = 2T(n/2) + O(1)$master theorem says--- $O(n)$

Better version:

logarithmic Paradigm: Divide and conquer.

Above function can be optimized to $O(\log n)$ by calculating $\text{power}(x, y/2)$ only once and storing it.

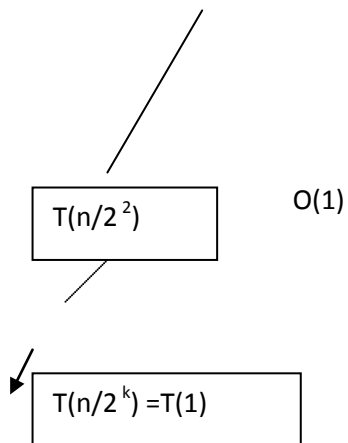
/* Function to calculate x raised to the power y in $O(\log n)$ */

```
int power(int x, unsigned int y)
{
    int temp;
    if( y == 0)
        return 1;
    temp = power(x, y / 2);
    if (y % 2 == 0)
        return temp * temp;
    else
        return x * temp * temp;
}
```

$T(n) = T(n/2) + O(1)$ ---- $O(\log n)$ (master theorem)

$T(n/2)$

$O(1)$



$$n/2^k = 1 \implies k = \log n$$

$$T(n) = O(1) + O(1) + \dots \text{upto } k \text{ terms} = O(k) = O(\log n)$$