

Dijkstra's Algorithm: single source **shortest path** finding algorithm

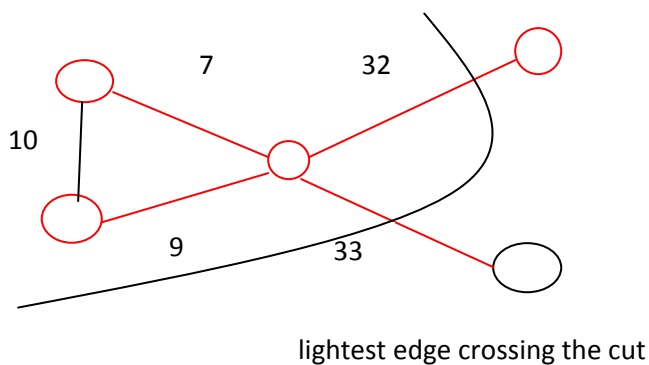
## Now Prim's Algorithm

Greedy Algorithm

Graph is undirected

For finding **minimum spanning tree** (MST).

Applications: **Data clustering**



**Prim** (  $G, w, s$  )

{ for (each  $u \in V$ )

{  $d[u] = \text{inf}$ ;  $\text{color}[u] = \text{white}$ ;

$d[s] = 0$ ;  $\text{pred}[s] = \text{NIL}$ ;  $X = \{s\}$ ;  $\text{pred}[s] = \text{NIL}$ ; /\*  $X$  is maintaining the visited nodes\*/

$Q = \{\text{queue with all vertices}\}$

while (non-empty( $Q$ ))

{

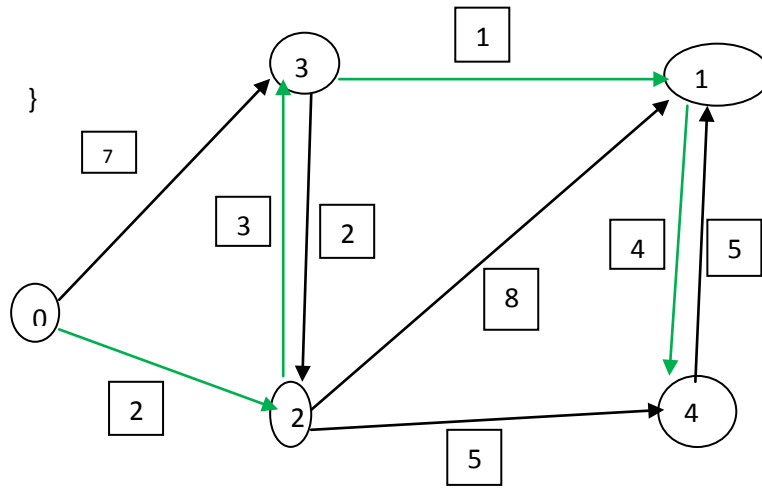
$u = \text{extract-min}(Q)$ ;

for (each  $v \in \text{adj}[u]$  &&  $v \in V - X$ ) /\*  $V - X$ : vertices not visited so far\*/

{ if ( $w(u,v) < d[v]$ )  $d[v] = w(u,v)$ ; insert ( $Q, v, d[v]$ );  $\text{pred}[v] = u$ ;

$\text{color}[u] = \text{black}$ ;  $X = X \cup u$ ;

}



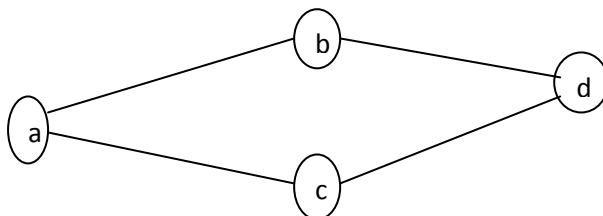
$v=\{a,b\}$

$$w[u,v] < d[a]$$

current:  $u = \text{vertex } a$

Q:  $b(3), c(8), d(5)$

v	c	d
D[v]	1	5



Adjacency matrix representation of a graph

	a	b	c	d
a	0	1	1	0
b	1	0	0	1
c				
d				

Adjacency list

$a \rightarrow \{(b,1), (c,1)\}$

$b \rightarrow \{a, d\}$

$c \rightarrow \{a, d\}$

$d \rightarrow \{b, c\}$