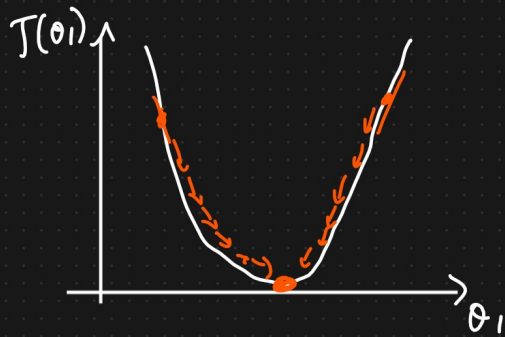
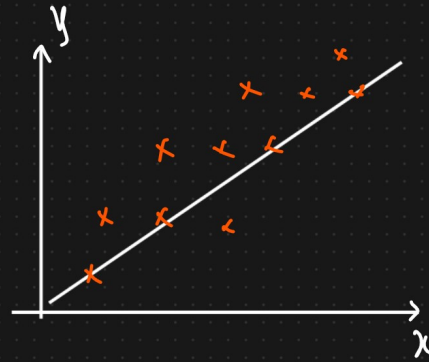


# MSE, MAE, RMSE [Cost functions]

- ① Mean Squared Error (MSE)
- ② Mean Absolute Error (MAE)
- ③ Root Mean Squared Error (RMSE)



$$J(\theta_0, \theta_1) = \frac{1}{n} \sum_{i=1}^n (y_i - h_{\theta}(x))^2$$

↓  
Mean Squared Error

$$\frac{\text{Ink}}{\text{Price}} = \frac{(I_{ink})^2}{(y - \hat{y})^2}$$

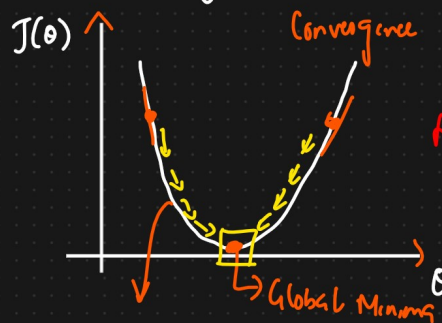
## ① Mean Squared Error (MSE) [cost fn]

$$MSE = \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n} \rightarrow \text{Quadratic Equation}$$

$$ax + by + c = 0$$

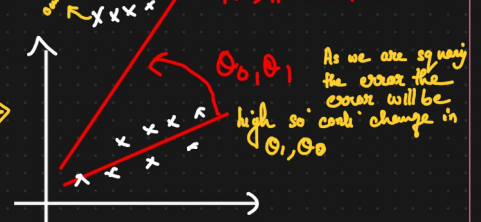
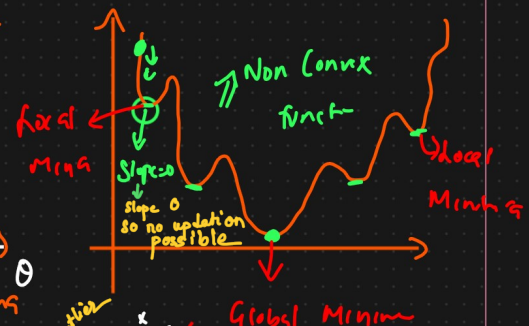
$$(a-b)^2 = a^2 - 2ab + b^2$$

## Non Quadratic Cost



Convex function.

$$(\text{Error})^2 \rightarrow$$



## Advantages

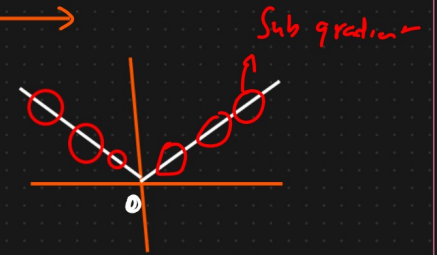
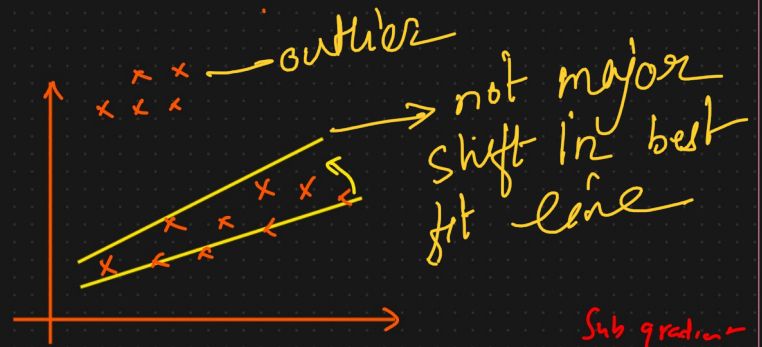
- ① It is differentiable
- ② It has one local and one global minimum

## Disadvantages

- ① MSE is Not Robust to outliers
- ② It is not in the same unit

## ② Mean Absolute Error

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$



### Advantage

- ① Robust to outliers
- ② It will be in the same unit

### Disadvantage

- ① Convergence usually takes time. Optimization is complex
- ② Time consuming

## ③ RMSE (Root Mean Squared Error)

$$RMSE = \sqrt{MSE}$$

$$= \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

### Advantage

- ① Same Unit
- ② Differentiable

### Disadvantage

- ① Not Robust to outliers

Note : Linear Regression

Performance check  $\rightarrow R^2$  and Adjusted  $R^2$

Cost function  $\rightarrow MSE, MAE, RMSE$