

Probability Density Function And Probability Mass Function

Cumulative Distribution Function (cdf)

① PMF :

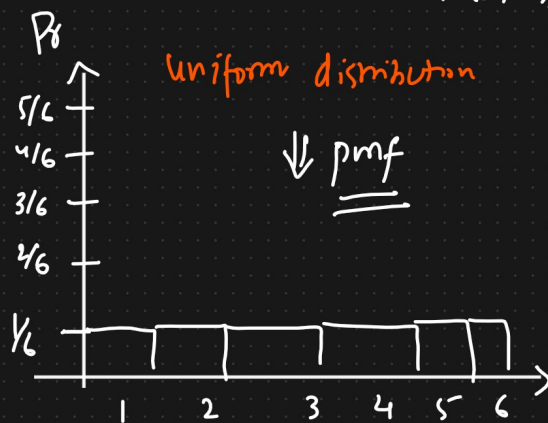
① Discrete Random Variable

PMF

Eg: Rolling a dice

$\{1, 2, 3, 4, 5, 6\}$ $\Pr(1) = 1/6$

$\Pr(2) = 1/6$



$$\Pr(X=1) = \frac{1}{6}$$

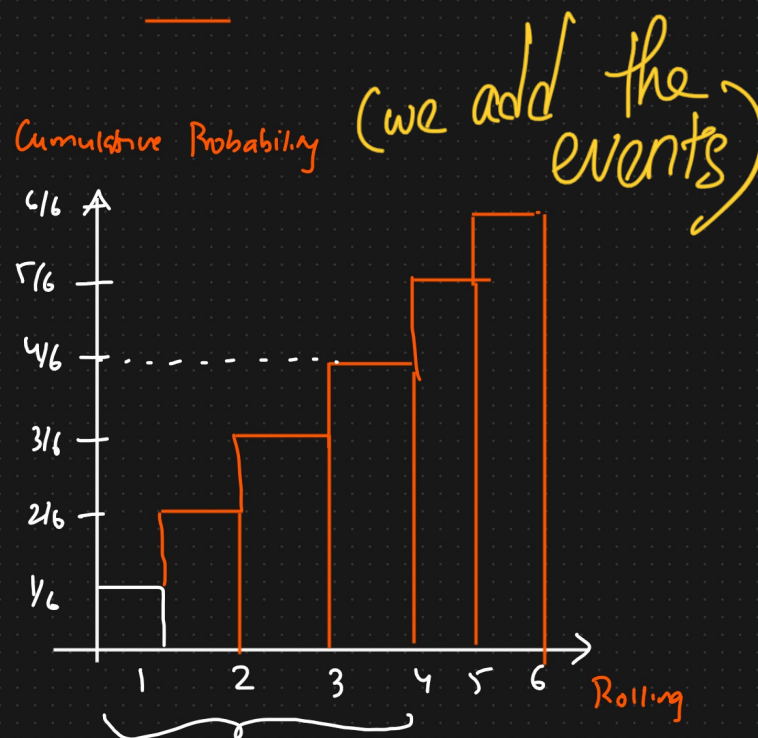
$$\Pr(X=2) = \frac{1}{6}$$

$$\Pr(X \leq 4) = \Pr(X=1) + \Pr(X=2)$$

$$+ \Pr(X=3) + \Pr(X=4)$$

$$= \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{4}{6} = \frac{2}{3}$$

CDF

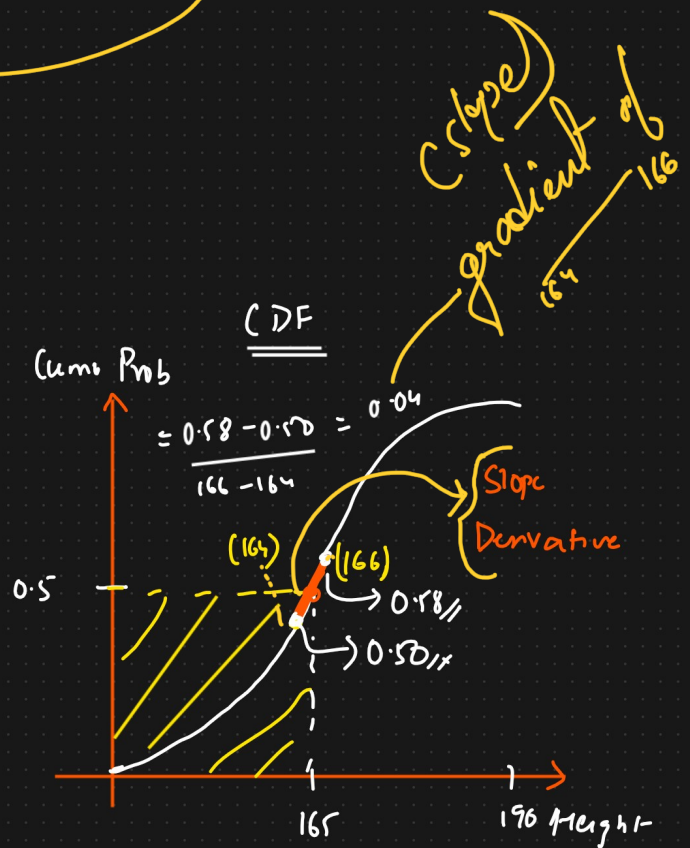
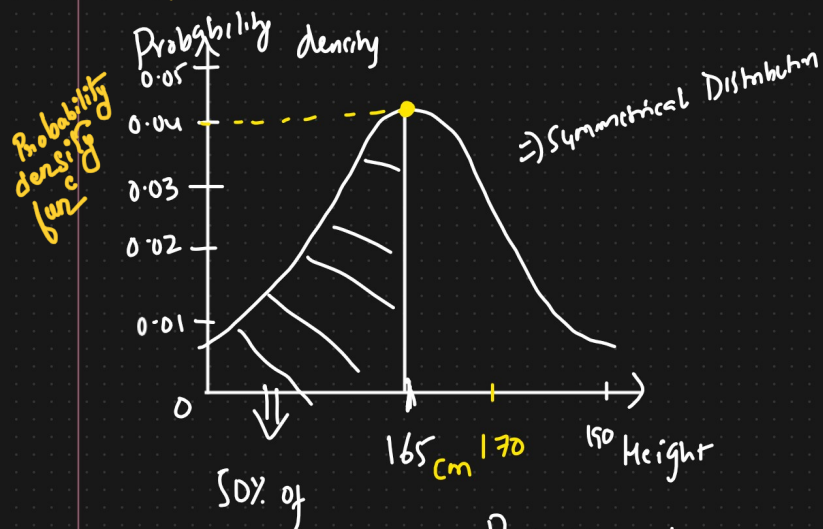


Cumulative

$$\begin{aligned} \Pr(X \leq 6) &= \Pr(X=1) + \Pr(X=2) + \Pr(X=3) \\ &\quad + \Pr(X=4) + \Pr(X=5) + \Pr(X=6) \\ &= 1 \end{aligned}$$

② Probability Density Function (PDF)

Continuous Random Variable



Probability density
 ↳ Gradient descent of
 CDF