# **Summary of OLS Results - Model Variables**

Variable	Coefficient [a]	StdError	t-Statistic	Probability [b]	Robust_SE	Robust_t	Robust_Pr [b]	VIF [c]
Intercept	-3332.791479	407.626521	-8.176091	0.000000*	279.008038	-11.945145	0.000000*	
SUM_SHAPE_LE	0.311387	0.038190	8.153693	0.000000*	0.038293	8.131691	0.000000*	2.948502
SUM_SHAPE_AR	0.013119	0.001248	10.510569	0.000000*	0.001388	9.451260	0.000000*	2.948502

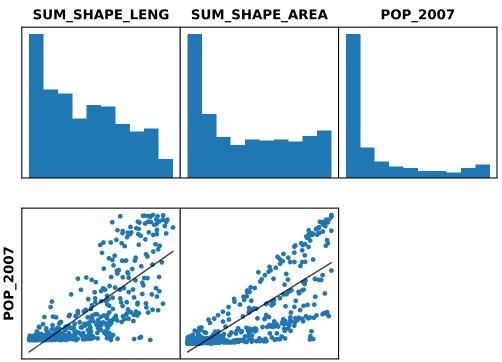
#### **OLS Diagnostics**

Input Features:	grid	Dependent Variable:	POP_2007
Number of Observations:	474	Akaike's Information Criterion (AICc) [d]:	9454.986320
Multiple R-Squared [d]:	0.664430	Adjusted R-Squared [d]:	0.663005
Joint F-Statistic [e]:	466.290457	Prob(>F), (2,471) degrees of freedom:	0.000000*
Joint Wald Statistic [e]:	622.829490	Prob(>chi-squared), (2) degrees of freedom:	0.000000*
Koenker (BP) Statistic [f]:	240.977030	Prob(>chi-squared), (2) degrees of freedom:	0.000000*
Jarque-Bera Statistic [g]:	1.166495	Prob(>chi-squared), (2) degrees of freedom:	0.558083

#### **Notes on Interpretation**

- \* An asterisk next to a number indicates a statistically significant p-value (p < 0.01).
- [a] Coefficient: Represents the strength and type of relationship between each explanatory variable and the dependent variable.
- [b] Probability and Robust Probability (Robust\_Pr): Asterisk (\*) indicates a coefficient is statistically significant (p < 0.01); if the Koenker
- (BP) Statistic [f] is statistically significant, use the Robust Probability column (Robust\_Pr) to determine coefficient significance.
- [c] Variance Inflation Factor (VIF): Large Variance Inflation Factor (VIF) values (> 7.5) indicate redundancy among explanatory variables.
- [d] R-Squared and Akaike's Information Criterion (AICc): Measures of model fit/performance.
- [e] Joint F and Wald Statistics: Asterisk (\*) indicates overall model significance (p < 0.01); if the Koenker (BP) Statistic [f] is statistically significant, use the Wald Statistic to determine overall model significance.
- [f] Koenker (BP) Statistic: When this test is statistically significant (p < 0.01), the relationships modeled are not consistent (either due to non-stationarity or heteroskedasticity). You should rely on the Robust Probabilities (Robust\_Pr) to determine coefficient significance and on the Wald Statistic to determine overall model significance.
- [g] Jarque-Bera Statistic: When this test is statistically significant (p < 0.01) model predictions are biased (the residuals are not normally distributed).

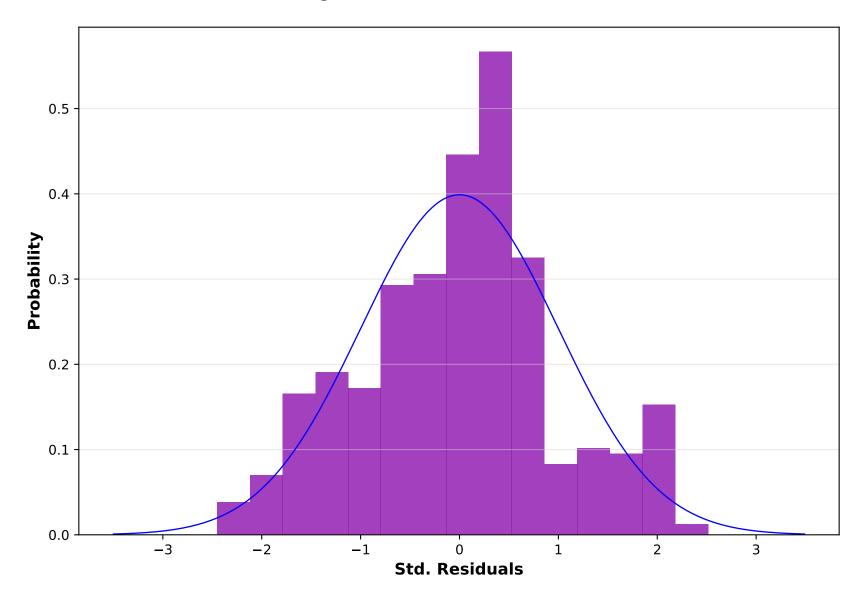
### **Variable Distributions and Relationships**



The above graphs are Histograms and Scatterplots for each explanatory variable and the dependent variable. The histograms show how each variable is distributed. OLS does not require variables to be normally distributed. However, if you are having trouble finding a properly-specified model, you can try transforming strongly skewed variables to see if you get a better result.

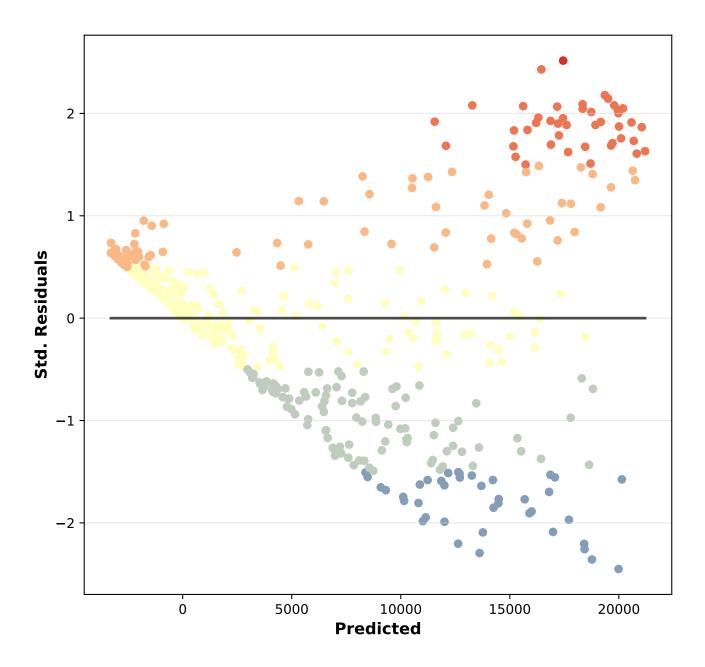
Each scatterplot depicts the relationship between an explanatory variable and the dependent variable. Strong relationships appear as diagonals and the direction of the slant indicates if the relationship is positive or negative. Try transforming your variables if you detect any non-linear relationships. For more information see the Regression Analysis Basics documentation.

### **Histogram of Standardized Residuals**

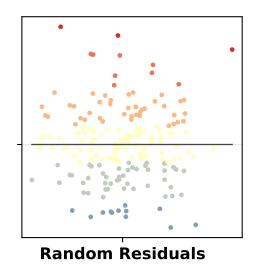


Ideally the histogram of your residuals would match the normal curve, indicated above in blue. If the histogram looks very different from the normal curve, you may have a biased model. If this bias is significant it will also be represented by a statistically significant Jarque-Bera p-value (\*).

#### **Residual vs. Predicted Plot**



This is a graph of residuals (model over and under predictions) in relation to predicted dependent variable values. For a properly specified model, this scatterplot will have little structure, and look random (see graph on the right). If there is a structure to this plot, the type of structure may be a valuable clue to help you figure out what's going on.



## **Ordinary Least Squares Parameters**

Parameter Name	Input Value	
Input Features	grid	
Unique ID Field	UniqueID	
Output Feature Class		
Dependent Variable	POP_2007	
Explanatory Variables	SUM_SHAPE_LENGTH	
	SUM_SHAPE_AREA	
Selection Set	False	