

# Eigenvectors of Symmetric Matrices

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```
S <- RM_symm(8,0.5,10)
prop <- prop_real_rows(evec_frame(S))
prop
```

```
## # A tibble: 8 x 3
##   row_i prop_reals is_real
##   <dbl>      <dbl> <lgl>
## 1     1         1 TRUE
## 2     2         1 TRUE
## 3     3         1 TRUE
## 4     4         1 TRUE
## 5     5         1 TRUE
## 6     6         1 TRUE
## 7     7         1 TRUE
## 8     8         1 TRUE
```

```
avgprop_real_components(evec_frame(S))
```

```
## [1] 1
```

## Simulation

```
simulate_by_f <- function(M_max,f,ep,draws){
  M_vec <- sample(1:M_max, draws, replace = F)
  table <- data.frame(M = M_vec)

  prop_vec <- rep(NA, length(table$M))

  for(i in 1:length(table$M)){
    S_curr <- RM_symm(table$M[i],f,ep)
    prop <- avgprop_real_components(evec_frame(S_curr))
    #print(prop)
    prop_vec[i] <- prop
  }
  cbind(table,prop_vec)
}

plot_f_table <- function(table, f){
  ggplot() +
    geom_point(data = table, aes(x=M, y=prop_vec, color = prop_vec)) +
    labs(color = "EV Real", title = paste("f = ",f,sep="")) +
    scale_color_gradient(high="blue", low="red")
}
```

```

}

M <- 200
ep <- 100
d <- ep

f <- 0.5
table <- simulate_by_f(f = f, M_max = M, ep = ep, draws = d)
head(table)

##      M prop_vec
## 1  97         1
## 2  17         1
## 3 113         1
## 4  71         1
## 5  77         1
## 6 102         1

model <- glm(formula = prop_vec ~ I(1/M), data = table)
summary(model)

##
## Call:
## glm(formula = prop_vec ~ I(1/M), data = table)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## 1.776e-15  2.109e-15  2.109e-15  2.109e-15  2.109e-15
##
## Coefficients:
##              Estimate Std. Error  t value Pr(>|t|)
## (Intercept) 1.000e+00  2.215e-16  4.514e+15  <2e-16 ***
## I(1/M)       3.508e-16  2.020e-15  1.740e-01    0.862
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for gaussian family taken to be 4.517964e-30)
##
##      Null deviance: 0.0000e+00  on 99  degrees of freedom
## Residual deviance: 4.4276e-28  on 98  degrees of freedom
## AIC: -6469.2
##
## Number of Fisher Scoring iterations: 1

pred <- function(M){
  b0 <- model$coefficients[1]
  b1 <- model$coefficients[2]
  b0 + b1/M
}

ggplot() +
  geom_point(data = table, aes(x=M, y=prop_vec, color = prop_vec)) +
  labs(color = "EV Real", title = paste("f = ", f, sep="")) +
  scale_color_gradient(high="blue", low="red") +
  stat_function(mapping = aes(x = M), fun = pred)

```

