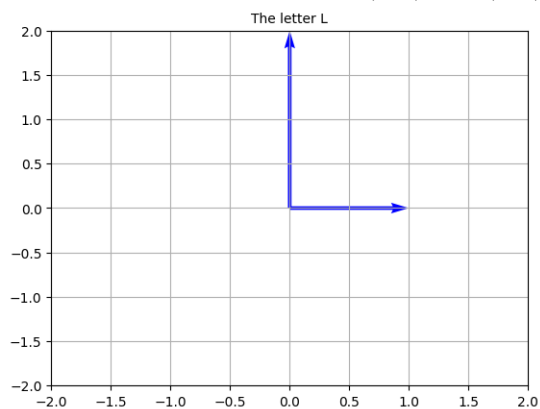


Chapter 2 Section 2

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The letter L can be represented by the vectors $(0, 2)$ and $(1, 0)$.



The following problems ask for a linear transformation of the letter L. In the following problems, give the matrix of the transformation and plot the result.

Problem 1. Scale L by a factor of $\frac{1}{2}$

Solution. The matrix of the transformation is

$$\begin{bmatrix} 0.5 & 0.0 \\ 0.0 & 0.5 \end{bmatrix}$$

After the scaling, the L looks like this



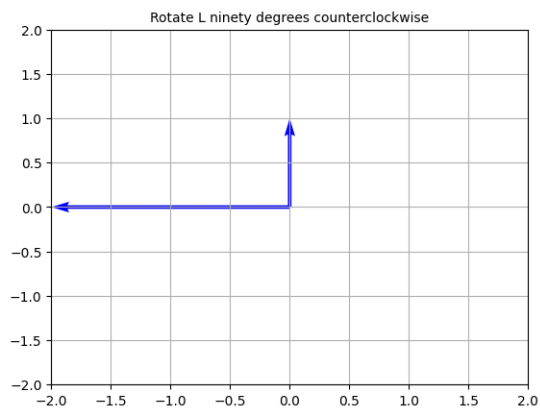
Note that in creating this shape, we scaled both vectors that make up the L.

Problem 2. *Rotate L ninety degrees counterclockwise*

Solution. *The matrix of the transformation is*

$$\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$$

After the rotation, the L looks like this

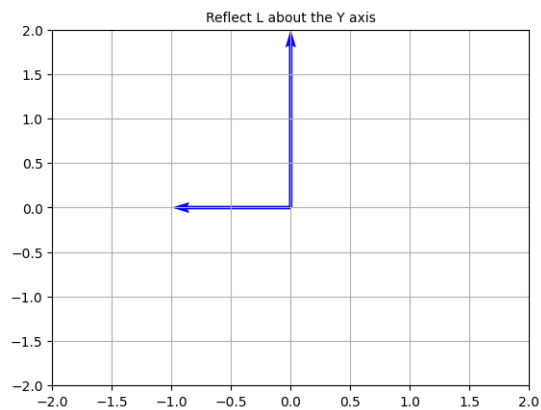


Problem 3. *Reflect L about the Y axis*

Solution. *The matrix of the transformation is*

$$\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

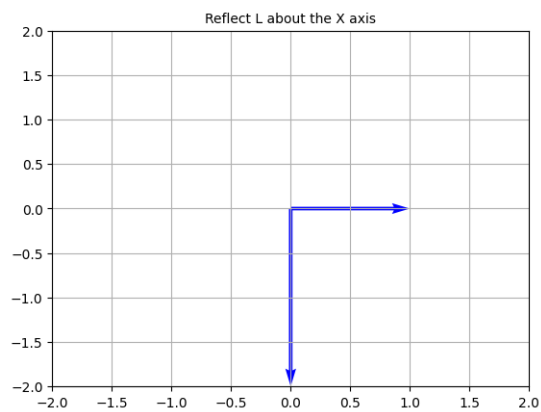
The plot looks like this



Problem 4. *Reflect L about the X axis*

Solution. *The matrix of the transformation is*

$$\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$$



Problem 5. *Rotate L forty five degrees counterclockwise*

Solution. *The matrix of the transformation is*

$$\begin{bmatrix} \cos(\frac{\pi}{4}) & -1 * \sin(\frac{\pi}{4}) \\ \sin(\frac{\pi}{4}) & \cos(\frac{\pi}{4}) \end{bmatrix}$$

