

Problem 11: Find $\lim_{x \rightarrow \infty} \frac{x}{x}$

(Source: AoPS Calculus)

Let $\epsilon > 0$. We want to find an N such that

$$x > N \quad \implies \quad \left| \frac{x}{x} - 1 \right| < \epsilon$$

Let $N = 0$. Then

$$x > N \quad \implies \quad \frac{x}{x} = 1 \quad \implies \quad \left| \frac{x}{x} - 1 \right| = 0$$

Thus

$$\lim_{x \rightarrow \infty} \frac{x}{x} = 1 \quad \square$$