

Problem 12: Find $\lim_{x \rightarrow 0^+} \frac{1}{x}$

Proof. Let N be a real number. We want to find a $\delta > 0$ such that

$$0 < x < \delta \implies f(x) > N$$

Let $\delta = \left| \frac{1}{N} \right|$. Then

$$0 < x < \delta \implies \frac{1}{x} > N$$

Thus

$$\lim_{x \rightarrow 0^+} \frac{1}{x} = \infty$$

□