

Problem 8: Let $f(x) = \frac{x^6 + x^4}{x + 1}$. What is $f(i - 1)$?

First let's plug in $(i - 1)$ for x .

$$f(i - 1) = \frac{(i - 1)^6 + (i - 1)^4}{(i - 1) + 1}$$

Now let's calculate $(i - 1)^2$, $(i - 1)^4$, and $(i - 1)^6$.

$$(i - 1)^2 = i^2 - 2i + 1 = -1 - 2i + 1 = -2i$$

$$(i - 1)^4 = (-2i)^2 = 4i^2 = -4$$

$$(i - 1)^6 = (i - 1)^2(i - 1)^4 = (-2i)(-4) = 8i$$

So

$$\begin{aligned} f(i - 1) &= \frac{(i - 1)^6 + (i - 1)^4}{(i - 1) + 1} \\ &= \frac{8i + -4}{i} \\ &= \frac{8i + -4}{i} \cdot \frac{i}{i} \\ &= \frac{8i^2 - 4i}{i^2} \\ &= \frac{-8 - 4i}{-1} \\ &= \boxed{8 + 4i} \end{aligned}$$