

Problem 7: Find the sum of the n^{th} roots of unity. (Source: AoPS Precalculus)

We can sum the n^{th} roots of unity using the sigma operator.

$$\begin{aligned}\sum_{k=0}^{n-1} e^{2\pi i k/n} &= \sum_{k=0}^{n-1} (e^{2\pi i/n})^k \\ &= \frac{(e^{2\pi i/n})^n - 1}{e^{2\pi i/n} - 1} \\ &= \frac{e^{2\pi i} - 1}{e^{2\pi i/n} - 1} \\ &= \frac{1 - 1}{e^{2\pi i/n} - 1} \\ &= \boxed{0}\end{aligned}$$

notice that this is a geometric series

we apply the formula for the sum of a geometric series

So the sum of the n^{th} roots of unity is $\boxed{0}$.