Application of Integrals

- Elementary area: The area is called elementary area which is located at any arbitary position within the region which is specified by some value of x between a and b.
- The area of the region bounded by the curve y = f(x), x-axis and the lines x = a and x = b (b > a) is given by the formula: $Area = \int_a^b y dx = \int_a^b f(x) dx$.
- The area of the region bounded by the curve $x = \theta(y)$, y-axis and the lines y = c, y = d is given by the formula: $Area = \int_{c}^{b} xdy = \int_{c}^{d} \theta(y)dy$
- The area of the region enclosed between two curves y = f(x), y = g(x) and the lines x = a, x = b is given by the formula, Area $= \int_a^b [f(x) g(x)] dx$, where $f(x) \ge g(x)$ in [a, b].
- If $f(x) \geq g(x)$ in [a, c] and $f(x) \leq g(x)$ in [c, b], a < c < b, then we write the areas as : Area = $\int\limits_a^b \left[f(x) g(x) \right] dx + \int\limits_c^b \left[g(x) f(x) \right] dx$.