

## SETS

---

1. Sets and their Representations
2. The Empty Set, Finite and Infinite Sets, Equal Sets
3. Subsets, Power Set, Universal Set
4. Venn Diagrams, Operations on Sets
5. Complement of a Set
6. Union and Intersection of Two Sets

- **Set:** A set is a well-defined collection of objects.
- **Representaiton of sets:** (i) Roster or Tabular form, (ii) Rule method or set builder form.

### Types of sets:

- **Empty set:** A set which does not contain any element is called empty set or null set or void set. It is denoted by  $\phi$  or  $\{\}$ .
- **Singleton set:** A set, consisting of a single element, is called a singleton set.
- **Finite set:** A set which consists of a definite number of elements is called finite set.
- **Infinite set:** A set, which is not finite, is called infinite set.
- **Equivalent sets:** Two finite sets A and B are equivalent, if their cardinal numbers are same, .i.e,  $n(A) = n(B)$ .
- **Equal sets:** Two sets A and B are said to be equal if they have exactly the same elements.
- **Subset:** A set A is said to be subset of a set B, if every element of A is also an element of B. Intervals are subsets of R.
- **Proper set:** If  $A \subseteq B$  and  $A \neq B$ , then A is called a proper set of B, written as  $A \subset B$ .

- **Universal set:** If all the sets under consideration are subsets of a large set  $U$ , then  $U$  is known as a universal set. And it is denoted by rectangle in Venn-Diagram.
- **Power set:** A power set of a set  $A$  is collection of all subsets of  $A$ . It is denoted by  $P(A)$ .
- **Venn-Diagram:** A geometrical figure illustrating universal set, subsets and their operations is known as Venn-Diagram.
- **Union of sets:** The union of two sets  $A$  and  $B$  is the set of all those elements which are either in  $A$  or in  $B$ .
- **Intersection of sets:** The intersection of two sets  $A$  and  $B$  is the set of all elements which are common. The difference of two sets  $A$  and  $B$  in this order is the set of elements which belong to  $A$  but not to  $B$ .
- **Disjoint sets:** Two sets  $A$  and  $B$  are said to be disjoint, if  $A \cap B = \phi$ .
- **Difference of sets:** Difference of two sets i.e., set  $(A - B)$  is the set of those elements of  $A$  which do not belong to  $B$ .
- **Complement of a set:** The complement of a subset  $A$  of universal set  $U$  is the set of all elements of  $U$  which are not the elements of  $A$ .  $A' = U - A$ .
- For any two sets  $A$  and  $B$ ,  $(A \cup B)' = A' \cap B'$  and  $(A \cap B)' = A' \cup B'$
- If  $A$  and  $B$  are finite sets such that  $A \cap B = \phi$ , then
 
$$n(A \cup B) = n(A) + n(B).$$
- If  $A \cap B \neq \phi$ , then
 
$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$