

Armando Tejada

Homework Week 10

11/2/22

Question 14.1

The breast cancer data set breast-cancer-wisconsin.data.txt from

<http://archive.ics.uci.edu/ml/machine-learning-databases/breast-cancer-wisconsin/> (description at <http://archive.ics.uci.edu/ml/datasets/Breast+Cancer+Wisconsin+%28Original%29>) has missing values.

1. Use the mean/mode imputation method to impute values for the missing data.
2. Use regression to impute values for the missing data.
3. Use regression with perturbation to impute values for the missing data.
4. (Optional) Compare the results and quality of classification models (e.g., SVM, KNN) build using (1) the data sets from questions 1,2,3; (2) the data that remains after data points with missing values are removed; and (3) the data set when a binary variable is introduced to indicate missing values.

Solution:

```
In [ ]: # Load packages I may need
```

```
library(tidyverse)
library(caret)
library(modelr)
library(ggthemes)
library(corrplot)
```

```
library(mice)
library(VIM)
```

```
In [ ]: set.seed(1)
```

```
# read in the cancer data
```

```
cancer_df = read_delim('C:/Users/ateje/OneDrive/Desktop/VS Code Projects/GTx_MM_in_Analytics/breast-cancer-wisconsin.data.txt',
                        col_names = F, na = c('?')) %>%
  as.data.frame() %>%
  mutate(X11 = ifelse(X11 == 2, 'Benign', 'Malignant'))
```

```
# using mice to see missing data - including complete cases
```

```
md.pattern(cancer_df[, -11])
```

```
# plot the missing data
```

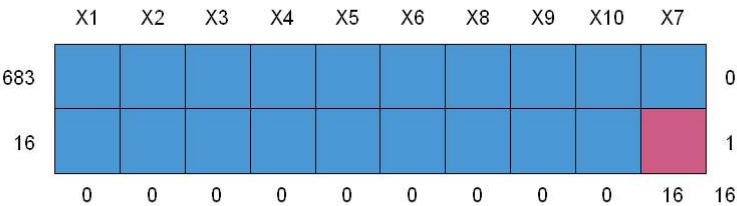
```
plot_missing <- aggr(cancer_df, col = c('navyblue', 'red'), numbers = T, sortVars = T)
```

```
Rows: 699 Columns: 11
Column specification
Delimiter: ","
dbl (11): X1, X2, X3, X4, X5, X6, X7, X8, X9, X10, X11

i Use `spec()` to retrieve the full column specification for this data.
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

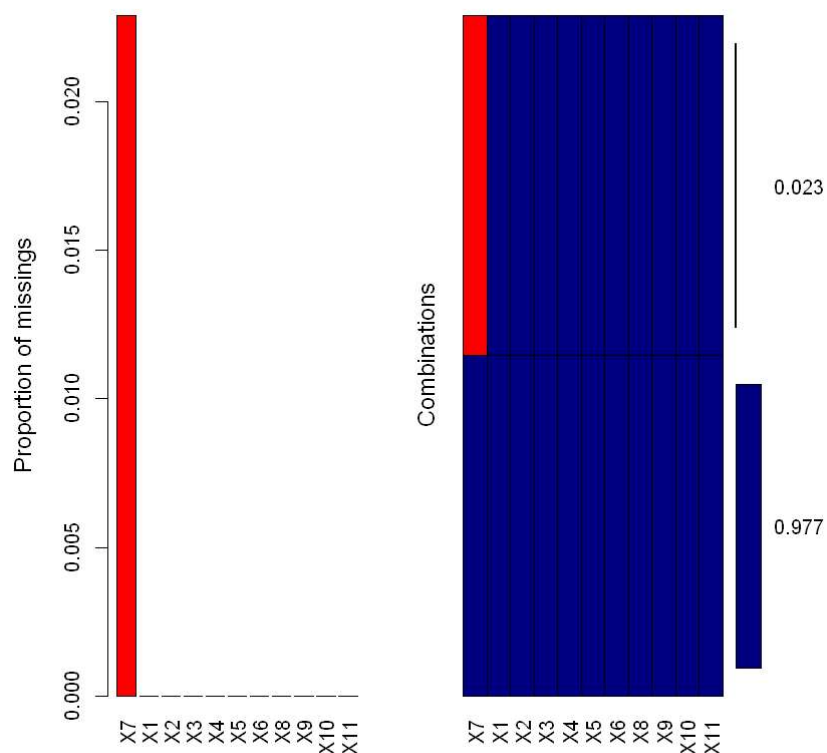
A matrix: 3 × 11 of type dbl

| | X1 | X2 | X3 | X4 | X5 | X6 | X8 | X9 | X10 | X7 |
|-----|----|----|----|----|----|----|----|----|-----|----|
| 683 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
| 16 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
| | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 16 |



Variables sorted by number of missings:

| Variable | Count |
|----------|------------|
| X7 | 0.02288984 |
| X1 | 0.00000000 |
| X2 | 0.00000000 |
| X3 | 0.00000000 |
| X4 | 0.00000000 |
| X5 | 0.00000000 |
| X6 | 0.00000000 |
| X8 | 0.00000000 |
| X9 | 0.00000000 |
| X10 | 0.00000000 |
| X11 | 0.00000000 |



```
In [ ]: # imputation using the mice package - mean imputation
mean_impute <- mice(cancer_df, m = 5, meth = 'mean' )

# Look at the values
mean_impute$imp
```

```
iter imp variable
1 1 X7
1 2 X7
1 3 X7
1 4 X7
1 5 X7
2 1 X7
2 2 X7
2 3 X7
2 4 X7
2 5 X7
3 1 X7
3 2 X7
3 3 X7
3 4 X7
3 5 X7
4 1 X7
4 2 X7
4 3 X7
4 4 X7
4 5 X7
5 1 X7
5 2 X7
5 3 X7
5 4 X7
5 5 X7
```

Warning message:
"Number of logged events: 1"

\$X1

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X2

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X3

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X4

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X5

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X6

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X7

| A data.frame: 16 × 5 | | | | | |
|----------------------|----------|----------|----------|----------|----------|
| | 1 | 2 | 3 | 4 | 5 |
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 24 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 41 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 140 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 146 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 159 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 165 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 236 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 250 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 276 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 293 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 295 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 298 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 316 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |

| | 1 | 2 | 3 | 4 | 5 |
|-----|----------|----------|----------|----------|----------|
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 322 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 412 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |
| 618 | 3.544656 | 3.544656 | 3.544656 | 3.544656 | 3.544656 |

\$X8

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X9

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X10

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X11

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

```
iter imp variable
1 1 X7
1 2 X7
1 3 X7
1 4 X7
1 5 X7
2 1 X7
2 2 X7
2 3 X7
2 4 X7
2 5 X7
3 1 X7
3 2 X7
3 3 X7
3 4 X7
3 5 X7
4 1 X7
4 2 X7
4 3 X7
4 4 X7
4 5 X7
5 1 X7
5 2 X7
5 3 X7
5 4 X7
5 5 X7
```

Warning message:
"Number of logged events: 1"

\$X1

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X2

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X3

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X4

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X5

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X6

| A data.frame: 0 × 5 | | | | |
|---------------------|-------|-------|-------|-------|
| 1 | 2 | 3 | 4 | 5 |
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X7

| A data.frame: 16 × 5 | | | | | |
|----------------------|-----------|-----------|-----------|-----------|-----------|
| | 1 | 2 | 3 | 4 | 5 |
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 24 | 5.3669508 | 5.3669508 | 5.3669508 | 5.3669508 | 5.3669508 |
| 41 | 8.1907122 | 8.1907122 | 8.1907122 | 8.1907122 | 8.1907122 |
| 140 | 0.8738591 | 0.8738591 | 0.8738591 | 0.8738591 | 0.8738591 |
| 146 | 1.6463893 | 1.6463893 | 1.6463893 | 1.6463893 | 1.6463893 |
| 159 | 1.0731978 | 1.0731978 | 1.0731978 | 1.0731978 | 1.0731978 |
| 165 | 2.1870186 | 2.1870186 | 2.1870186 | 2.1870186 | 2.1870186 |
| 236 | 2.7459168 | 2.7459168 | 2.7459168 | 2.7459168 | 2.7459168 |
| 250 | 2.0127161 | 2.0127161 | 2.0127161 | 2.0127161 | 2.0127161 |
| 276 | 2.3072038 | 2.3072038 | 2.3072038 | 2.3072038 | 2.3072038 |
| 293 | 5.9989744 | 5.9989744 | 5.9989744 | 5.9989744 | 5.9989744 |
| 295 | 1.1204527 | 1.1204527 | 1.1204527 | 1.1204527 | 1.1204527 |
| 298 | 2.6839366 | 2.6839366 | 2.6839366 | 2.6839366 | 2.6839366 |
| 316 | 5.6353059 | 5.6353059 | 5.6353059 | 5.6353059 | 5.6353059 |

| | 1 | 2 | 3 | 4 | 5 |
|------------|-----------|-----------|-----------|-----------|-----------|
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 322 | 1.8585015 | 1.8585015 | 1.8585015 | 1.8585015 | 1.8585015 |
| 412 | 0.8587684 | 0.8587684 | 0.8587684 | 0.8587684 | 0.8587684 |
| 618 | 0.5907393 | 0.5907393 | 0.5907393 | 0.5907393 | 0.5907393 |

\$X8

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X9

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X10

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X11

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

```
In [ ]: # imputation using the mice package - regression ignoring model error
regression_impute <- mice(cancer_df, m = 5, meth = 'norm.predict')

# Look at the values
regression_impute$imp
```

```
In [ ]: # imputation using the mice package - perturbation impute
pert_impute <- mice(cancer_df, m = 5, meth = 'norm.nob')

# Look at the values
pert_impute$imp
```


| iter | imp | variable |
|------|-----|----------|
|------|-----|----------|

| | | |
|---|---|----|
| 1 | 1 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 2 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 3 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 4 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 5 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 2 | 1 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 2 | 2 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 2 | 3 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 2 | 4 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 2 | 5 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 3 | 1 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 3 | 2 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 3 | 3 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 3 | 4 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 3 | 5 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 4 | 1 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 4 | 2 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 4 | 3 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 4 | 4 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 4 | 5 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 5 | 1 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 5 | 2 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 5 | 3 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 5 | 4 | X7 |
|---|---|----|

| | | |
|---|---|----|
| 5 | 5 | X7 |
|---|---|----|

Warning message:

"Number of logged events: 1"

\$X1

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X2

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X3

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X4

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X5

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X6

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X7

A data.frame: 16 × 5

| | 1 | 2 | 3 | 4 | 5 |
|------------|------------|-----------|-----------|--------------|------------|
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 24 | 3.74019613 | 2.112548 | 5.754193 | 6.542245038 | 8.3991056 |
| 41 | 6.47785909 | 13.327107 | 11.031538 | 5.279079278 | 7.3691419 |
| 140 | 1.02816124 | -1.205451 | 2.338500 | -0.401999456 | 0.3160545 |
| 146 | 1.48513771 | -2.179527 | 3.562301 | 0.008079856 | -0.1830189 |
| 159 | 2.33526892 | -1.725926 | -1.833393 | -0.559918789 | 0.8977351 |
| 165 | 1.73465992 | -1.528415 | 1.617340 | -0.988170624 | 1.5126888 |
| 236 | 3.11101934 | 1.408588 | -2.822924 | 6.147719083 | 5.4472161 |
| 250 | 0.09159326 | 2.701089 | 3.150801 | -1.743670278 | 3.4485212 |
| 276 | 2.38663866 | -1.583771 | 3.171041 | 2.070783192 | 2.4976321 |
| 293 | 6.07586930 | 5.927439 | 3.048709 | 6.976790384 | 6.6228084 |
| 295 | 1.98902076 | 1.424256 | 3.886388 | 3.508502749 | 3.8107415 |
| 298 | 2.63590012 | 2.728575 | 4.621931 | 4.930007558 | -1.4773002 |
| 316 | 5.16059793 | 4.842153 | 6.895866 | 4.993188229 | 3.4155540 |

| | 1 | 2 | 3 | 4 | 5 |
|-----|-------------|-----------|-----------|--------------|------------|
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 322 | 1.09375193 | 2.803795 | 2.331938 | 4.507931165 | -1.8924155 |
| 412 | -0.38016150 | 3.449344 | -2.296806 | 1.278841938 | 0.2325643 |
| 618 | 0.88052310 | -3.112713 | 1.746031 | -0.125077946 | -0.8736359 |

\$X8

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X9

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X10

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

\$X11

A data.frame: 0 × 5

| 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|
| <lgl> | <lgl> | <lgl> | <lgl> | <lgl> |

```
In [ ]: # Data with mean impute
cancer_mean_df <- complete(mean_impute)
cancer_mean_df
```

A data.frame: 699 × 11

| X1 | X2 | X3 | X4 | X5 | X6 | X7 | X8 | X9 | X10 | X11 |
|---------|-------|-------|-------|-------|-------|-----------|-------|-------|-------|-----------|
| <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <chr> |
| 1000025 | 5 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1002945 | 5 | 4 | 4 | 5 | 7 | 10.000000 | 3 | 2 | 1 | Benign |
| 1015425 | 3 | 1 | 1 | 1 | 2 | 2.000000 | 3 | 1 | 1 | Benign |
| 1016277 | 6 | 8 | 8 | 1 | 3 | 4.000000 | 3 | 7 | 1 | Benign |
| 1017023 | 4 | 1 | 1 | 3 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1017122 | 8 | 10 | 10 | 8 | 7 | 10.000000 | 9 | 7 | 1 | Malignant |
| 1018099 | 1 | 1 | 1 | 1 | 2 | 10.000000 | 3 | 1 | 1 | Benign |
| 1018561 | 2 | 1 | 2 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1033078 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 1 | 1 | 5 | Benign |
| 1033078 | 4 | 2 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1035283 | 1 | 1 | 1 | 1 | 1 | 1.000000 | 3 | 1 | 1 | Benign |
| 1036172 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1041801 | 5 | 3 | 3 | 3 | 2 | 3.000000 | 4 | 4 | 1 | Malignant |
| 1043999 | 1 | 1 | 1 | 1 | 2 | 3.000000 | 3 | 1 | 1 | Benign |
| 1044572 | 8 | 7 | 5 | 10 | 7 | 9.000000 | 5 | 5 | 4 | Malignant |
| 1047630 | 7 | 4 | 6 | 4 | 6 | 1.000000 | 4 | 3 | 1 | Malignant |
| 1048672 | 4 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1049815 | 4 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1050670 | 10 | 7 | 7 | 6 | 4 | 10.000000 | 4 | 1 | 2 | Malignant |
| 1050718 | 6 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1054590 | 7 | 3 | 2 | 10 | 5 | 10.000000 | 5 | 4 | 4 | Malignant |
| 1054593 | 10 | 5 | 5 | 3 | 6 | 7.000000 | 7 | 10 | 1 | Malignant |
| 1056784 | 3 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1057013 | 8 | 4 | 5 | 1 | 2 | 3.544656 | 7 | 3 | 1 | Malignant |
| 1059552 | 1 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1065726 | 5 | 2 | 3 | 4 | 2 | 7.000000 | 3 | 6 | 1 | Malignant |
| 1066373 | 3 | 2 | 1 | 1 | 1 | 1.000000 | 2 | 1 | 1 | Benign |
| 1066979 | 5 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1067444 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1070935 | 1 | 1 | 3 | 1 | 2 | 1.000000 | 1 | 1 | 1 | Benign |
| ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ |
| 1350423 | 5 | 10 | 10 | 8 | 5 | 5 | 7 | 10 | 1 | Malignant |

| | X1 | X2 | X3 | X4 | X5 | X6 | X7 | X8 | X9 | X10 | X11 |
|---------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----------|
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <chr> |
| 1352848 | | 3 | 10 | 7 | 8 | 5 | 8 | 7 | 4 | 1 | Malignant |
| 1353092 | | 3 | 2 | 1 | 2 | 2 | 1 | 3 | 1 | 1 | Benign |
| 1354840 | | 2 | 1 | 1 | 1 | 2 | 1 | 3 | 1 | 1 | Benign |
| 1354840 | | 5 | 3 | 2 | 1 | 3 | 1 | 1 | 1 | 1 | Benign |
| 1355260 | | 1 | 1 | 1 | 1 | 2 | 1 | 2 | 1 | 1 | Benign |
| 1365075 | | 4 | 1 | 4 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1365328 | | 1 | 1 | 2 | 1 | 2 | 1 | 2 | 1 | 1 | Benign |
| 1368267 | | 5 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1368273 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1368882 | | 2 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1369821 | | 10 | 10 | 10 | 10 | 5 | 10 | 10 | 10 | 7 | Malignant |
| 1371026 | | 5 | 10 | 10 | 10 | 4 | 10 | 5 | 6 | 3 | Malignant |
| 1371920 | | 5 | 1 | 1 | 1 | 2 | 1 | 3 | 2 | 1 | Benign |
| 466906 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 466906 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 534555 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 536708 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 566346 | | 3 | 1 | 1 | 1 | 2 | 1 | 2 | 3 | 1 | Benign |
| 603148 | | 4 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 654546 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 8 | Benign |
| 654546 | | 1 | 1 | 1 | 3 | 2 | 1 | 1 | 1 | 1 | Benign |
| 695091 | | 5 | 10 | 10 | 5 | 4 | 5 | 4 | 4 | 1 | Malignant |
| 714039 | | 3 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 763235 | | 3 | 1 | 1 | 1 | 2 | 1 | 2 | 1 | 2 | Benign |
| 776715 | | 3 | 1 | 1 | 1 | 3 | 2 | 1 | 1 | 1 | Benign |
| 841769 | | 2 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 888820 | | 5 | 10 | 10 | 3 | 7 | 3 | 8 | 10 | 2 | Malignant |
| 897471 | | 4 | 8 | 6 | 4 | 3 | 4 | 10 | 6 | 1 | Malignant |
| 897471 | | 4 | 8 | 8 | 5 | 4 | 5 | 10 | 4 | 1 | Malignant |

A data.frame: 699 × 11

| X1 | X2 | X3 | X4 | X5 | X6 | X7 | X8 | X9 | X10 | X11 |
|---------|-------|-------|-------|-------|-------|-----------|-------|-------|-------|-----------|
| <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <chr> |
| 1000025 | 5 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1002945 | 5 | 4 | 4 | 5 | 7 | 10.000000 | 3 | 2 | 1 | Benign |
| 1015425 | 3 | 1 | 1 | 1 | 2 | 2.000000 | 3 | 1 | 1 | Benign |
| 1016277 | 6 | 8 | 8 | 1 | 3 | 4.000000 | 3 | 7 | 1 | Benign |
| 1017023 | 4 | 1 | 1 | 3 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1017122 | 8 | 10 | 10 | 8 | 7 | 10.000000 | 9 | 7 | 1 | Malignant |
| 1018099 | 1 | 1 | 1 | 1 | 2 | 10.000000 | 3 | 1 | 1 | Benign |
| 1018561 | 2 | 1 | 2 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1033078 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 1 | 1 | 5 | Benign |
| 1033078 | 4 | 2 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1035283 | 1 | 1 | 1 | 1 | 1 | 1.000000 | 3 | 1 | 1 | Benign |
| 1036172 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1041801 | 5 | 3 | 3 | 3 | 2 | 3.000000 | 4 | 4 | 1 | Malignant |
| 1043999 | 1 | 1 | 1 | 1 | 2 | 3.000000 | 3 | 1 | 1 | Benign |
| 1044572 | 8 | 7 | 5 | 10 | 7 | 9.000000 | 5 | 5 | 4 | Malignant |
| 1047630 | 7 | 4 | 6 | 4 | 6 | 1.000000 | 4 | 3 | 1 | Malignant |
| 1048672 | 4 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1049815 | 4 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1050670 | 10 | 7 | 7 | 6 | 4 | 10.000000 | 4 | 1 | 2 | Malignant |
| 1050718 | 6 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1054590 | 7 | 3 | 2 | 10 | 5 | 10.000000 | 5 | 4 | 4 | Malignant |
| 1054593 | 10 | 5 | 5 | 3 | 6 | 7.000000 | 7 | 10 | 1 | Malignant |
| 1056784 | 3 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1057013 | 8 | 4 | 5 | 1 | 2 | 5.366951 | 7 | 3 | 1 | Malignant |
| 1059552 | 1 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1065726 | 5 | 2 | 3 | 4 | 2 | 7.000000 | 3 | 6 | 1 | Malignant |
| 1066373 | 3 | 2 | 1 | 1 | 1 | 1.000000 | 2 | 1 | 1 | Benign |
| 1066979 | 5 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1067444 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1070935 | 1 | 1 | 3 | 1 | 2 | 1.000000 | 1 | 1 | 1 | Benign |
| ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ |
| 1350423 | 5 | 10 | 10 | 8 | 5 | 5 | 7 | 10 | 1 | Malignant |

| | X1 | X2 | X3 | X4 | X5 | X6 | X7 | X8 | X9 | X10 | X11 |
|---------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----------|
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <chr> |
| 1352848 | | 3 | 10 | 7 | 8 | 5 | 8 | 7 | 4 | 1 | Malignant |
| 1353092 | | 3 | 2 | 1 | 2 | 2 | 1 | 3 | 1 | 1 | Benign |
| 1354840 | | 2 | 1 | 1 | 1 | 2 | 1 | 3 | 1 | 1 | Benign |
| 1354840 | | 5 | 3 | 2 | 1 | 3 | 1 | 1 | 1 | 1 | Benign |
| 1355260 | | 1 | 1 | 1 | 1 | 2 | 1 | 2 | 1 | 1 | Benign |
| 1365075 | | 4 | 1 | 4 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1365328 | | 1 | 1 | 2 | 1 | 2 | 1 | 2 | 1 | 1 | Benign |
| 1368267 | | 5 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1368273 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1368882 | | 2 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1369821 | | 10 | 10 | 10 | 10 | 5 | 10 | 10 | 10 | 7 | Malignant |
| 1371026 | | 5 | 10 | 10 | 10 | 4 | 10 | 5 | 6 | 3 | Malignant |
| 1371920 | | 5 | 1 | 1 | 1 | 2 | 1 | 3 | 2 | 1 | Benign |
| 466906 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 466906 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 534555 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 536708 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 566346 | | 3 | 1 | 1 | 1 | 2 | 1 | 2 | 3 | 1 | Benign |
| 603148 | | 4 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 654546 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 8 | Benign |
| 654546 | | 1 | 1 | 1 | 3 | 2 | 1 | 1 | 1 | 1 | Benign |
| 695091 | | 5 | 10 | 10 | 5 | 4 | 5 | 4 | 4 | 1 | Malignant |
| 714039 | | 3 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 763235 | | 3 | 1 | 1 | 1 | 2 | 1 | 2 | 1 | 2 | Benign |
| 776715 | | 3 | 1 | 1 | 1 | 3 | 2 | 1 | 1 | 1 | Benign |
| 841769 | | 2 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 888820 | | 5 | 10 | 10 | 3 | 7 | 3 | 8 | 10 | 2 | Malignant |
| 897471 | | 4 | 8 | 6 | 4 | 3 | 4 | 10 | 6 | 1 | Malignant |
| 897471 | | 4 | 8 | 8 | 5 | 4 | 5 | 10 | 4 | 1 | Malignant |

A data.frame: 699 × 11

| X1 | X2 | X3 | X4 | X5 | X6 | X7 | X8 | X9 | X10 | X11 |
|---------|-------|-------|-------|-------|-------|-----------|-------|-------|-------|-----------|
| <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <chr> |
| 1000025 | 5 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1002945 | 5 | 4 | 4 | 5 | 7 | 10.000000 | 3 | 2 | 1 | Benign |
| 1015425 | 3 | 1 | 1 | 1 | 2 | 2.000000 | 3 | 1 | 1 | Benign |
| 1016277 | 6 | 8 | 8 | 1 | 3 | 4.000000 | 3 | 7 | 1 | Benign |
| 1017023 | 4 | 1 | 1 | 3 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1017122 | 8 | 10 | 10 | 8 | 7 | 10.000000 | 9 | 7 | 1 | Malignant |
| 1018099 | 1 | 1 | 1 | 1 | 2 | 10.000000 | 3 | 1 | 1 | Benign |
| 1018561 | 2 | 1 | 2 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1033078 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 1 | 1 | 5 | Benign |
| 1033078 | 4 | 2 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1035283 | 1 | 1 | 1 | 1 | 1 | 1.000000 | 3 | 1 | 1 | Benign |
| 1036172 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1041801 | 5 | 3 | 3 | 3 | 2 | 3.000000 | 4 | 4 | 1 | Malignant |
| 1043999 | 1 | 1 | 1 | 1 | 2 | 3.000000 | 3 | 1 | 1 | Benign |
| 1044572 | 8 | 7 | 5 | 10 | 7 | 9.000000 | 5 | 5 | 4 | Malignant |
| 1047630 | 7 | 4 | 6 | 4 | 6 | 1.000000 | 4 | 3 | 1 | Malignant |
| 1048672 | 4 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1049815 | 4 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1050670 | 10 | 7 | 7 | 6 | 4 | 10.000000 | 4 | 1 | 2 | Malignant |
| 1050718 | 6 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1054590 | 7 | 3 | 2 | 10 | 5 | 10.000000 | 5 | 4 | 4 | Malignant |
| 1054593 | 10 | 5 | 5 | 3 | 6 | 7.000000 | 7 | 10 | 1 | Malignant |
| 1056784 | 3 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1057013 | 8 | 4 | 5 | 1 | 2 | 3.740196 | 7 | 3 | 1 | Malignant |
| 1059552 | 1 | 1 | 1 | 1 | 2 | 1.000000 | 3 | 1 | 1 | Benign |
| 1065726 | 5 | 2 | 3 | 4 | 2 | 7.000000 | 3 | 6 | 1 | Malignant |
| 1066373 | 3 | 2 | 1 | 1 | 1 | 1.000000 | 2 | 1 | 1 | Benign |
| 1066979 | 5 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1067444 | 2 | 1 | 1 | 1 | 2 | 1.000000 | 2 | 1 | 1 | Benign |
| 1070935 | 1 | 1 | 3 | 1 | 2 | 1.000000 | 1 | 1 | 1 | Benign |
| ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ |
| 1350423 | 5 | 10 | 10 | 8 | 5 | 5 | 7 | 10 | 1 | Malignant |

| | X1 | X2 | X3 | X4 | X5 | X6 | X7 | X8 | X9 | X10 | X11 |
|---------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----------|
| | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <chr> |
| 1352848 | | 3 | 10 | 7 | 8 | 5 | 8 | 7 | 4 | 1 | Malignant |
| 1353092 | | 3 | 2 | 1 | 2 | 2 | 1 | 3 | 1 | 1 | Benign |
| 1354840 | | 2 | 1 | 1 | 1 | 2 | 1 | 3 | 1 | 1 | Benign |
| 1354840 | | 5 | 3 | 2 | 1 | 3 | 1 | 1 | 1 | 1 | Benign |
| 1355260 | | 1 | 1 | 1 | 1 | 2 | 1 | 2 | 1 | 1 | Benign |
| 1365075 | | 4 | 1 | 4 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1365328 | | 1 | 1 | 2 | 1 | 2 | 1 | 2 | 1 | 1 | Benign |
| 1368267 | | 5 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1368273 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1368882 | | 2 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 1369821 | | 10 | 10 | 10 | 10 | 5 | 10 | 10 | 10 | 7 | Malignant |
| 1371026 | | 5 | 10 | 10 | 10 | 4 | 10 | 5 | 6 | 3 | Malignant |
| 1371920 | | 5 | 1 | 1 | 1 | 2 | 1 | 3 | 2 | 1 | Benign |
| 466906 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 466906 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 534555 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 536708 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 566346 | | 3 | 1 | 1 | 1 | 2 | 1 | 2 | 3 | 1 | Benign |
| 603148 | | 4 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 654546 | | 1 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 8 | Benign |
| 654546 | | 1 | 1 | 1 | 3 | 2 | 1 | 1 | 1 | 1 | Benign |
| 695091 | | 5 | 10 | 10 | 5 | 4 | 5 | 4 | 4 | 1 | Malignant |
| 714039 | | 3 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 763235 | | 3 | 1 | 1 | 1 | 2 | 1 | 2 | 1 | 2 | Benign |
| 776715 | | 3 | 1 | 1 | 1 | 3 | 2 | 1 | 1 | 1 | Benign |
| 841769 | | 2 | 1 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | Benign |
| 888820 | | 5 | 10 | 10 | 3 | 7 | 3 | 8 | 10 | 2 | Malignant |
| 897471 | | 4 | 8 | 6 | 4 | 3 | 4 | 10 | 6 | 1 | Malignant |
| 897471 | | 4 | 8 | 8 | 5 | 4 | 5 | 10 | 4 | 1 | Malignant |

```
In [ ]: # Data with regression prediction impute
cancer_regression_df <- complete(regression_impute)
cancer_regression_df
```

```
In [ ]: # Data with perturbation impute
```

```
cancer_pert_df <- complete(pert_impute)  
cancer_pert_df
```

Question 15.1

Describe a situation or problem from your job, everyday life, current events, etc., for which optimization would be appropriate. What data would you need?

Solution:

Optimization can be used for airline to decide the number of first-class tickets, advantage tickets, and coach tickets they should sell to maximize their profits for their flights. The company might need to consider certain constraints like number of first class and coach seats available and the size of the staff to serve first class, etc.