two_layer_net

February 11, 2020

1 Implementing a Neural Network

In this exercise we will develop a neural network with fully-connected layers to perform classification, and test it out on the CIFAR-10 dataset.

The neural network parameters will be stored in a dictionary (model below), where the keys are the parameter names and the values are numpy arrays. Below, we initialize toy data and a toy model that we will use to verify your implementations.

```
[2]: # Create some toy data to check your implementations
input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5

def init_toy_model():
   model = {}
```

2 Forward pass: compute scores

Open the file cs231n/classifiers/neural_net.py and look at the function two_layer_net. This function is very similar to the loss functions you have written for the Softmax exercise in HW0: It takes the data and weights and computes the class scores, the loss, and the gradients on the parameters.

Implement the first part of the forward pass which uses the weights and biases to compute the scores for all inputs.

```
[3]: from cs231n.classifiers.neural_net import two_layer_net

scores = two_layer_net(X, model)
print(scores)
correct_scores = [[-0.5328368, 0.20031504, 0.93346689],
        [-0.59412164, 0.15498488, 0.9040914],
        [-0.67658362, 0.08978957, 0.85616275],
        [-0.77092643, 0.01339997, 0.79772637],
        [-0.89110401, -0.08754544, 0.71601312]]

# the difference should be very small. We get 3e-8
print('Difference between your scores and correct scores:')
print(np.sum(np.abs(scores - correct_scores)))
```

```
Difference between your scores and correct scores: 3.848682303062012e-08
```

3 Forward pass: compute loss

In the same function, implement the second part that computes the data and regularization loss.

```
[4]: reg = 0.1
loss, _ = two_layer_net(X, model, y, reg)
correct_loss = 1.38191946092

# should be very small, we get 5e-12
print('Difference between your loss and correct loss:')
print(np.sum(np.abs(loss - correct_loss)))
```

Difference between your loss and correct loss: 4.6769255135359344e-12

4 Backward pass

Implement the rest of the function. This will compute the gradient of the loss with respect to the variables W1, b1, W2, and b2. Now that you (hopefully!) have a correctly implemented forward pass, you can debug your backward pass using a numeric gradient check:

```
W2 max relative error: 9.913910e-10
b2 max relative error: 8.190173e-11
W1 max relative error: 4.426512e-09
b1 max relative error: 5.435433e-08
```

5 Train the network

To train the network we will use SGD with Momentum. Last assignment you implemented vanilla SGD. You will now implement the momentum update and the RMSProp update. Open the file classifier_trainer.py and familiarize yourself with the ClassifierTrainer class. It performs optimization given an arbitrary cost function data, and model. By default it uses vanilla SGD, which we have already implemented for you. First, run the optimization below using Vanilla SGD:

```
starting iteration 0
starting iteration 10
starting iteration 20
starting iteration 30
starting iteration 40
starting iteration 50
starting iteration 60
starting iteration 70
starting iteration 80
starting iteration 90
Final loss with vanilla SGD: 0.940686
```

Now fill in the **momentum update** in the first missing code block inside the **train** function, and run the same optimization as above but with the momentum update. You should see a much better result in the final obtained loss:

```
reg=0.001,
learning_rate=1e-1, momentum=0.9,
⇒learning_rate_decay=1,

update='momentum', sample_batches=False,
num_epochs=100,
verbose=False)

correct_loss = 0.494394
print('Final loss with momentum SGD: %f. We get: %f' % (loss_history[-1],
⇒correct_loss))
```

```
starting iteration 0
starting iteration 10
starting iteration 20
starting iteration 30
starting iteration 40
starting iteration 50
starting iteration 60
starting iteration 70
starting iteration 80
starting iteration 90
Final loss with momentum SGD: 0.494394. We get: 0.494394
The RMSProp update step is given as follows:
cache = decay_rate * cache + (1 - decay_rate) * dx**2
```

x += - learning_rate * dx / np.sqrt(cache + 1e-8)

Here, decay_rate is a hyperparameter and typical values are [0.9, 0.99, 0.999].

Implement the RMSProp update rule inside the train function and rerun the optimization:

```
[23]: model = init_toy_model()
     trainer = ClassifierTrainer()
      # call the trainer to optimize the loss
      # Notice that we're using sample_batches=False, so we're performing Gradientu
      → Descent (no sampled batches of data)
     best_model, loss_history, _, _ = trainer.train(X, y, X, y,
                                                  model, two_layer_net,
                                                  reg=0.001,
                                                  learning_rate=1e-1, momentum=0.9,
      →learning_rate_decay=1,
                                              update='rmsprop', sample_batches=False,
                                                  num_epochs=100,
                                                  verbose=False)
     correct_loss = 0.439368
     print('Final loss with RMSProp: %f. We get: %f' % (loss_history[-1],_
```

starting iteration 0

```
starting iteration 10
starting iteration 20
starting iteration 30
starting iteration 40
starting iteration 50
starting iteration 60
starting iteration 70
starting iteration 80
starting iteration 90
Final loss with RMSProp: 0.439368. We get: 0.439368
```

6 Load the data

Now that you have implemented a two-layer network that passes gradient checks, it's time to load up our favorite CIFAR-10 data so we can use it to train a classifier.

```
[9]: from cs231n.data_utils import load_CIFAR10
     def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000):
         Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
         it for the two-layer neural net classifier.
         # Load the raw CIFAR-10 data
         cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
         X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
         # Subsample the data
         mask = range(num_training, num_training + num_validation)
         X val = X train[mask]
         y_val = y_train[mask]
         mask = range(num_training)
         X_train = X_train[mask]
         y_train = y_train[mask]
         mask = range(num_test)
         X_test = X_test[mask]
         y_test = y_test[mask]
         # Normalize the data: subtract the mean image
         mean_image = np.mean(X_train, axis=0)
         X_train -= mean_image
         X_val -= mean_image
         X_test -= mean_image
         # Reshape data to rows
         X_train = X_train.reshape(num_training, -1)
```

```
X_val = X_val.reshape(num_validation, -1)
X_test = X_test.reshape(num_test, -1)

return X_train, y_train, X_val, y_val, X_test, y_test

# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)

7 Train a network

To train our network we will use SGD with momentum. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
starting iteration 0
Finished epoch 0 / 5: cost 2.302593, train: 0.087000, val 0.103000, lr 1.000000e-05
starting iteration 10
starting iteration 20
starting iteration 30
```

```
starting iteration
                   40
starting iteration
starting iteration
                   60
starting iteration
                   70
starting iteration 80
starting iteration
                   90
starting iteration 100
starting iteration 110
starting iteration 120
starting iteration 130
starting iteration
                   140
starting iteration
                   150
starting iteration
                   160
starting iteration
                   170
starting iteration
                   180
                   190
starting iteration
starting iteration
                   200
starting iteration
                   210
starting iteration 220
starting iteration
                   230
starting iteration
                   240
starting iteration
                   250
starting iteration 260
starting iteration 270
starting iteration
                   280
starting iteration
                   290
starting iteration
                   300
starting iteration
                   310
starting iteration
                   320
starting iteration
                   330
starting iteration
                   340
starting iteration
                   350
starting iteration
                   360
starting iteration
                   370
starting iteration
                   380
starting iteration
                   390
starting iteration 400
starting iteration 410
starting iteration
starting iteration 430
starting iteration 440
starting iteration
                   450
starting iteration
                   460
starting iteration
                   470
starting iteration 480
Finished epoch 1 / 5: cost 2.289076, train: 0.153000, val 0.180000, lr
9.500000e-06
starting iteration 490
```

```
starting iteration
                    500
starting iteration
                    510
starting iteration
                    520
starting iteration
                    530
starting iteration
                    540
starting iteration
                    550
starting iteration
                    560
starting iteration
                    570
starting iteration
                    580
starting iteration
                    590
starting iteration
                    600
starting iteration
                    610
starting iteration
                    620
starting iteration
                    630
starting iteration
                    640
                    650
starting iteration
starting iteration
                    660
starting iteration
                    670
starting iteration
                    680
starting iteration
                    690
starting iteration
                    700
starting iteration
                    710
starting iteration
                    730
starting iteration
starting iteration
                    740
starting iteration
                    750
starting iteration
                    760
starting iteration
                    770
                    780
starting iteration
starting iteration
                    790
                    800
starting iteration
starting iteration
                    810
starting iteration
                    820
starting iteration
                    830
starting iteration
                    840
starting iteration
                    850
starting iteration
                    860
starting iteration
                    870
starting iteration
starting iteration
                    890
                    900
starting iteration
starting iteration
                    910
starting iteration
                    920
starting iteration
                    930
starting iteration
                    940
starting iteration
                    950
starting iteration
                    960
starting iteration
                    970
```

```
Finished epoch 2 / 5: cost 2.071362, train: 0.237000, val 0.241000, lr
9.025000e-06
starting iteration 980
starting iteration
starting iteration 1000
starting iteration 1010
starting iteration 1020
starting iteration 1030
starting iteration 1040
starting iteration 1050
starting iteration 1060
starting iteration 1070
starting iteration 1080
starting iteration 1090
starting iteration 1100
starting iteration 1110
starting iteration 1120
starting iteration 1130
starting iteration 1140
starting iteration 1150
starting iteration 1160
starting iteration 1170
starting iteration 1180
starting iteration 1190
starting iteration 1200
starting iteration 1210
starting iteration 1220
starting iteration 1230
starting iteration 1240
starting iteration 1250
starting iteration 1260
starting iteration 1270
starting iteration 1280
starting iteration 1290
starting iteration 1300
starting iteration 1310
starting iteration 1320
starting iteration 1330
starting iteration 1340
starting iteration 1350
starting iteration 1360
starting iteration 1370
starting iteration 1380
starting iteration 1390
starting iteration 1400
starting iteration 1410
starting iteration 1420
starting iteration 1430
```

```
starting iteration 1440
starting iteration 1450
starting iteration 1460
Finished epoch 3 / 5: cost 1.901091, train: 0.302000, val 0.298000, lr
8.573750e-06
starting iteration 1470
starting iteration 1480
starting iteration 1490
starting iteration 1500
starting iteration 1510
starting iteration 1520
starting iteration 1530
starting iteration 1540
starting iteration 1550
starting iteration 1560
starting iteration 1570
starting iteration 1580
starting iteration 1590
starting iteration 1600
starting iteration 1610
starting iteration 1620
starting iteration 1630
starting iteration 1640
starting iteration 1650
starting iteration 1660
starting iteration 1670
starting iteration 1680
starting iteration 1690
starting iteration 1700
starting iteration 1710
starting iteration 1720
starting iteration 1730
starting iteration 1740
starting iteration 1750
starting iteration 1760
starting iteration 1770
starting iteration 1780
starting iteration 1790
starting iteration 1800
starting iteration 1810
starting iteration 1820
starting iteration 1830
starting iteration 1840
starting iteration 1850
starting iteration 1860
starting iteration 1870
starting iteration 1880
starting iteration 1890
```

```
starting iteration 1900
starting iteration 1910
starting iteration 1920
starting iteration 1930
starting iteration 1940
starting iteration 1950
Finished epoch 4 / 5: cost 1.844763, train: 0.335000, val 0.343000, lr
8.145063e-06
starting iteration 1960
starting iteration 1970
starting iteration 1980
starting iteration 1990
starting iteration 2000
starting iteration 2010
starting iteration 2020
starting iteration 2030
starting iteration 2040
starting iteration 2050
starting iteration 2060
starting iteration 2070
starting iteration 2080
starting iteration 2090
starting iteration 2100
starting iteration 2110
starting iteration 2120
starting iteration 2130
starting iteration 2140
starting iteration 2150
starting iteration 2160
starting iteration 2170
starting iteration 2180
starting iteration 2190
starting iteration 2200
starting iteration 2210
starting iteration 2220
starting iteration 2230
starting iteration 2240
starting iteration 2250
starting iteration 2260
starting iteration 2270
starting iteration 2280
starting iteration 2290
starting iteration 2300
starting iteration 2310
starting iteration 2320
starting iteration 2330
starting iteration 2340
starting iteration 2350
```

```
starting iteration 2360
starting iteration 2380
starting iteration 2390
starting iteration 2400
starting iteration 2410
starting iteration 2420
starting iteration 2430
starting iteration 2430
starting iteration 2440
Finished epoch 5 / 5: cost 1.851382, train: 0.390000, val 0.369000, lr 7.737809e-06
finished optimization. best validation accuracy: 0.369000
```

8 Debug the training

With the default parameters we provided above, you should get a validation accuracy of about 0.37 on the validation set. This isn't very good.

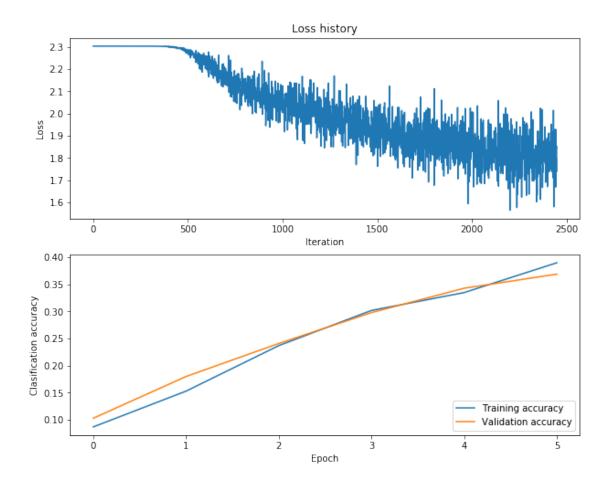
One strategy for getting insight into what's wrong is to plot the loss function and the accuracies on the training and validation sets during optimization.

Another strategy is to visualize the weights that were learned in the first layer of the network. In most neural networks trained on visual data, the first layer weights typically show some visible structure when visualized.

```
[26]: # Plot the loss function and train / validation accuracies
plt.subplot(2, 1, 1)
plt.plot(loss_history)
plt.title('Loss history')
plt.xlabel('Iteration')
plt.ylabel('Loss')

plt.subplot(2, 1, 2)
plt.plot(train_acc)
plt.plot(val_acc)
plt.legend(['Training accuracy', 'Validation accuracy'], loc='lower right')
plt.xlabel('Epoch')
plt.ylabel('Clasification accuracy')
```

[26]: Text(0, 0.5, 'Clasification accuracy')

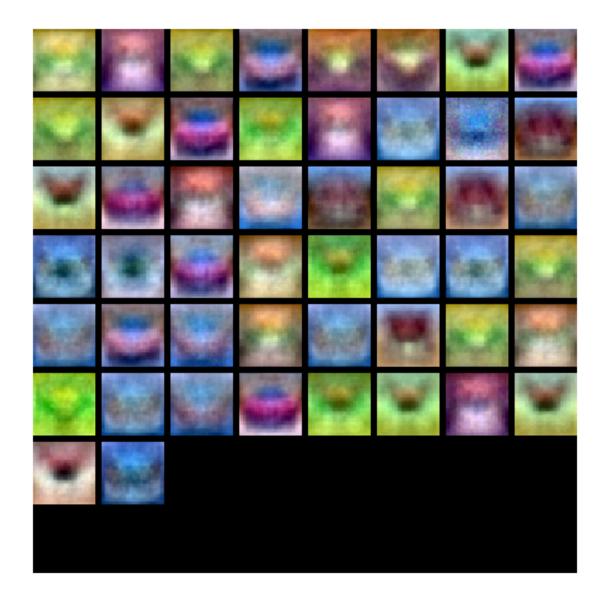


```
[27]: from cs231n.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(model):
    plt.imshow(visualize_grid(model['W1'].T.reshape(-1, 32, 32, 3), padding=3).
    astype('uint8'))
    plt.gca().axis('off')
    plt.show()

show_net_weights(model)
```



9 Tune your hyperparameters

What's wrong?. Looking at the visualizations above, we see that the loss is decreasing more or less linearly, which seems to suggest that the learning rate may be too low. Moreover, there is no gap between the training and validation accuracy, suggesting that the model we used has low capacity, and that we should increase its size. On the other hand, with a very large model we would expect to see more overfitting, which would manifest itself as a very large gap between the training and validation accuracy.

Tuning. Tuning the hyperparameters and developing intuition for how they affect the final performance is a large part of using Neural Networks, so we want you to get a lot of practice. Below, you should experiment with different values of the various hyperparameters, including hidden layer

size, learning rate, numer of training epochs, and regularization strength. You might also consider tuning the momentum and learning rate decay parameters, but you should be able to get good performance using the default values.

Approximate results. You should be aim to achieve a classification accuracy of greater than 50% on the validation set. Our best network gets over 56% on the validation set.

Experiment: You goal in this exercise is to get as good of a result on CIFAR-10 as you can, with a fully-connected Neural Network. For every 1% above 56% on the Test set we will award you with one extra bonus point. Feel free implement your own techniques (e.g. PCA to reduce dimensionality, or adding dropout, or adding features to the solver, etc.).

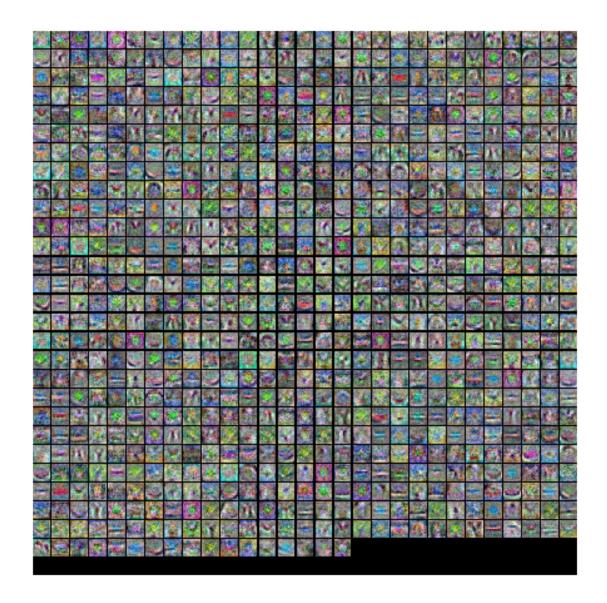
```
[50]: best_model = None # store the best model into this
     # TODO: Tune hyperparameters using the validation set. Store your best trained
     # model in best model.
                                                                                 #
                                                                                 #
     # To help debug your network, it may help to use visualizations similar to the
     # ones we used above; these visualizations will have significant qualitative
     # differences from the ones we saw above for the poorly tuned network.
                                                                                 #
     # Tweaking hyperparameters by hand can be fun, but you might find it useful to
     # write code to sweep through possible combinations of hyperparameters
     # automatically like we did on the previous assignment.
                                                                                 #
     # input size, hidden size, number of classes
      '''hsizes = [200,400,600,800,1000]
     lrs = [1e-5, 5e-5, 1e-4, 5e-4, 1e-3]
     momentums = [0.8, 0.85, 0.9, 0.95]
     lrds = [0.85, 0.9, 0.95]
     best = -1
     for idx hsizes, hsize in enumerate(hsizes):
         for idx_lrs, lr in enumerate(lrs):
             for idx momentums, momentum in enumerate(momentums):
                 for idx lrds, lrd in enumerate(lrds):
                     model = init two layer model(32*32*3, hsize, 10)
                     trainer = ClassifierTrainer()
                     current_model, loss_history, train_acc, val_acc = trainer.
      \hookrightarrow train(X_train, y_train,
                                                                           X val_{11}
      \hookrightarrow y\_val,
                                                                           model, u
      \hookrightarrow two\_layer\_net,
                                                                              Ш
      \rightarrow num_epochs=1, reg=1.0,
```

```
→momentum=momentum,
\rightarrow learning_rate_decay=lrd,
→ learning_rate=lr, verbose=False)
            #print(val_acc,best)
            if val acc[-1]>best:
               best = val \ acc[-1]
               best model = current model
               idx_hsize = idx_hsizes
               idx lr = idx lrs
               idx_m = idx_momentums
               idx lrd = idx lrds
print ('Learning rate is: %f.', lrs[idx_lr])
print ('Hidden layer size is: %d.',hsizes[idx hsize])
print ('Momentum is %f.',momentums[idx_m])
print ('Learning rate decay is:%f.',lrds[idx_lrd])'''
END OF YOUR CODE
~~~~~
```

```
[50]: "hsizes = [200,400,600,800,1000]\nlrs = [1e-5,5e-5,1e-4,5e-4,1e-3]\nmomentums =
      [0.8,0.85,0.9,0.95]\nlrds = [0.85,0.9,0.95]\nbest = -1\nfor idx_hsizes,hsize in
      enumerate(hsizes):\n
                              for idx_lrs,lr in enumerate(lrs):\n
                                                                          for
      idx momentums,momentum in enumerate(momentums):\n
                                                                   for idx lrds, lrd in
      enumerate(lrds):\n
                                        model = init_two_layer_model(32*32*3, hsize,
                           trainer = ClassifierTrainer()\n
      10)\n
      current_model, loss_history, train_acc, val_acc = trainer.train(X_train,
      y_train,\n
      X val, y val,\n
     model, two_layer_net,\n
     num_epochs=1, reg=1.0,\n
     momentum=momentum, \n
      learning_rate_decay=lrd,\n
      learning_rate=lr, verbose=False)\n
                                                        #print(val_acc,best)\n
      if val_acc[-1]>best:\n
                                                best = val_acc[-1]\n
      best_model = current_model\n
                                                      idx_hsize = idx_hsizes\n
      idx_lr = idx_lrs\n
                                            idx m = idx momentums\n
      idx lrd = idx lrds\nprint ('Learning rate is: %f.',lrs[idx lr])\nprint ('Hidden
      layer size is: %d.',hsizes[idx hsize])\nprint ('Momentum is
      %f.',momentums[idx_m]) \nprint ('Learning rate decay is:%f.',lrds[idx_lrd])"
```

9.1 The cell above and below was used to select the hyperparameters and was commented out for too many lines of log outputing

```
[16]: #hsizes = [200,400,600,800,1000]
      from cs231n.classifiers.neural net import init two layer model
      from cs231n.classifier_trainer import ClassifierTrainer
      hsizes = [800]
      best = -1
      for idx, hsize in enumerate(hsizes):
          model = init_two_layer_model(32*32*3, hsize, 10)
          trainer = ClassifierTrainer()
          \hookrightarrow y_train,
                                                                                   X_val,
       \hookrightarrow y \ val,
                                                                                   model,
       \hookrightarrow two\_layer\_net,
                                                                                     Ш
       \hookrightarrow num epochs=10, req=1.0,
                                                                                     ш
       \rightarrow momentum=0.8,
       \hookrightarrow learning_rate_decay=0.9,
                                                                                      ш
       → learning_rate=5e-4, verbose=False)
          if val_acc[-1]>best:
                           best = val\_acc[-1]
                           best model = current model
                           idx hsize = idx
      print(hsizes[idx hsize])
      111
      # visualize the weights
```



10 Run on the test set

When you are done experimenting, you should evaluate your final trained network on the test set.

```
[14]: scores_test = two_layer_net(X_test, best_model)
    print('Test accuracy: ', np.mean(np.argmax(scores_test, axis=1) == y_test))

Test accuracy: 0.51
[]:
```