Week 7 Homework

July 1, 2020

0.1 Question 15.2

In the videos, we saw the "diet problem". (The diet problem is one of the first large-scale optimization problems to be studied in practice. Back in the 1930's and 40's, the Army wanted to meet the nutritional requirements of its soldiers while minimizing the cost.) In this homework you get to solve a diet problem with real data. The data is given in the file diet.xls.

Importing packages

```
[132]: from pulp import *
import pandas as pd
import numpy as np
```

Read in Data

Binary Variable that specifies poultry

```
[13]: # Creating a binary variable that specifies poultry or not

poultry = np.zeros(64)
poultry[[8, 27, 28, 29, 30, 31, 32, 41, 43, 44, 49, 50, 51, 56, 57, 58, 59, 61, 463]] = 1
diet['Poultry'] = pd.Series(poultry)
```

[123]: diet.head()

```
[123]:
                         Foods Price/ Serving
                                                     Serving Size
                                                                    Calories \
       0
              Frozen Broccoli
                                           0.16
                                                        10 Oz Pkg
                                                                        73.8
       1
                  Carrots, Raw
                                           0.07 1/2 Cup Shredded
                                                                        23.7
       2
                  Celery, Raw
                                           0.04
                                                          1 Stalk
                                                                         6.4
       3
                  Frozen Corn
                                           0.18
                                                          1/2 Cup
                                                                        72.2
         Lettuce, Iceberg, Raw
                                           0.02
                                                           1 Leaf
                                                                         2.6
```

```
Cholesterol mg Total Fat g Sodium mg Carbohydrates g Dietary Fiber g \
0
              0.0
                            0.8
                                      68.2
                                                        13.6
                                                                           8.5
              0.0
                            0.1
                                      19.2
1
                                                         5.6
                                                                           1.6
2
              0.0
                            0.1
                                      34.8
                                                         1.5
                                                                           0.7
                            0.6
3
              0.0
                                       2.5
                                                        17.1
                                                                           2.0
4
              0.0
                            0.0
                                       1.8
                                                         0.4
                                                                           0.3
   Protein g Vit A IU Vit C IU Calcium mg Iron mg Poultry
         8.0
                5867.4
                            160.2
                                        159.0
                                                    2.3
0
                                                    0.3
                                                             0.0
         0.6
               15471.0
                              5.1
                                         14.9
1
2
         0.3
                  53.6
                              2.8
                                         16.0
                                                    0.2
                                                             0.0
3
         2.5
                 106.6
                              5.2
                                           3.3
                                                    0.3
                                                             0.0
4
         0.2
                  66.0
                              0.8
                                           3.8
                                                    0.1
                                                             0.0
```

Preparing Data for PuLP package

```
[129]: diet_data = diet[0:64]
       diet_data = diet_data.values.tolist()
       foods = [x[0] for x in diet_data]
       cost = {x[0]: float(x[1]) for x in diet_data}
       cals = {x[0]: float(x[3]) for x in diet_data}
       cholestrol = \{x[0]: float(x[4]) \text{ for } x \text{ in diet data}\}
       fat = {x[0]: float(x[5]) for x in diet_data}
       sodium = \{x[0]: float(x[6]) \text{ for } x \text{ in diet data}\}
       carbs = {x[0]: float(x[7]) for x in diet_data}
       fiber = \{x[0]: float(x[8]) \text{ for } x \text{ in diet data}\}
       protein = {x[0]: float(x[9]) for x in diet_data}
       Vit_A = {x[0]: float(x[10]) for x in diet_data}
       Vit_C = {x[0]: float(x[11]) for x in diet_data}
       Calcium = {x[0]: float(x[12]) for x in diet_data}
       Iron = {x[0]: float(x[13]) for x in diet_data}
       Poultry = {x[0]: float(x[14]) for x in diet_data}
       # Script for preparing the data so it can be looped over. Unfortunately, looped
        →script generated an error.
       # l = \Gamma 7
       \# names = [7]
       # nutrient_restrictions = []
       # for i in range(3, diet.shape[1]):
              names.append(diet.columns.values[i])
              l.append(\{x[0]: float(x[i]) for x in diet_data\})
              nutrient_restrictions.append([diet.iloc[65, i], diet.iloc[66, i]])
       # 1[0]
```

0.1.1 Question 1

Formulate an optimization model (a linear program) to find the cheapest diet that satisfies the maximum and minimum daily nutrition constraints, and solve it using PuLP. Turn in your code and the solution. (The optimal solution should be a diet of air-popped popcorn, poached eggs, oranges, raw iceberg lettuce, raw celery, and frozen broccoli. UGH!)()

Writing out Optimization Problem

```
[130]: problem = LpProblem('Diet Problem', LpMinimize)
       selectVars = LpVariable.dicts('Picked', foods, 0, 1, cat = 'Integer')
       amountVars = LpVariable.dicts('Amounts', foods, 0)
       problem += lpSum([cost[i] * amountVars[i] for i in foods]), 'total cost'
       # Script for looping over the nutrients which for some reason generated any
        \hookrightarrow error.
       # for a in range(len(l)):
             problem += lpSum([l[a][i] * amountVars[i] for i in foods]) >=_{\sqcup}
        \rightarrownutrient_restrictions[a][1], 'max ' + names[a]
             problem += lpSum([l[a][i] * amountVars[i] for i in foods]) <=__</pre>
        →nutrient_restrictions[a][0], 'min ' + names[a]
       problem += lpSum([cals[i] * amountVars[i] for i in foods]) >= diet.iloc[65, 3],
        →'min cals'
       problem += lpSum([cals[i] * amountVars[i] for i in foods]) <= diet.iloc[66, 3],
        →'max cals'
       problem += lpSum([cholestrol[i] * amountVars[i] for i in foods]) >= diet.
        →iloc[65, 4], 'min cholestrol'
       problem += lpSum([cholestrol[i] * amountVars[i] for i in foods]) <= diet.</pre>
        →iloc[66, 4], 'max cholestrol'
       problem += lpSum([fat[i] * amountVars[i] for i in foods]) >= diet.iloc[65, 5],
        →'min fat'
       problem += lpSum([fat[i] * amountVars[i] for i in foods]) <= diet.iloc[66, 5],
        →'max fat'
       problem += lpSum([sodium[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
        \hookrightarrow6], 'min sodium'
       problem += lpSum([sodium[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
        \hookrightarrow6], 'max sodium'
```

```
problem += lpSum([carbs[i] * amountVars[i] for i in foods]) >= diet.iloc[65, u
\hookrightarrow7], 'min carbs'
problem += lpSum([carbs[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
\hookrightarrow7], 'max carbs'
problem += lpSum([fiber[i] * amountVars[i] for i in foods]) >= diet.iloc[65, u
→8], 'min fiber'
problem += lpSum([fiber[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
→8], 'max fiber'
problem += lpSum([protein[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
\rightarrow 9], 'min protein'
problem += lpSum([protein[i] * amountVars[i] for i in foods]) <= diet.iloc[66, __
 →9], 'max protein'
problem += lpSum([Vit_A[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
\hookrightarrow10], 'min Vit_A'
problem += lpSum([Vit_A[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
\hookrightarrow10], 'max Vit_A'
problem += lpSum([Vit_C[i] * amountVars[i] for i in foods]) >= diet.iloc[65, u
→11], 'min Vit_C'
problem += lpSum([Vit_C[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
\hookrightarrow11], 'max Vit_C'
problem += lpSum([Calcium[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
\hookrightarrow12], 'min Calcium'
problem += lpSum([Calcium[i] * amountVars[i] for i in foods]) <= diet.iloc[66, __
→12], 'max Calcium'
problem += lpSum([Iron[i] * amountVars[i] for i in foods]) >= diet.iloc[65, u
\hookrightarrow13], 'min Iron'
problem += lpSum([Iron[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
 \hookrightarrow13], 'max Iron'
```

C:\Users\ujjaw\anaconda3\lib\site-packages\pulp\pulp.py:1114: UserWarning:
Spaces are not permitted in the name. Converted to '_'
warnings.warn("Spaces are not permitted in the name. Converted to '_'")

Solving the Problem

```
[131]: problem.solve()
   varsDictionary = {}
   for v in problem.variables():
      varsDictionary[v.name] = v.varValue
      if v.varValue >0:
            print ("{} = {}".format(v.name, v.varValue))
```

```
Amounts_Celery,_Raw = 52.64371

Amounts_Frozen_Broccoli = 0.25960653

Amounts_Lettuce,Iceberg,Raw = 63.988506

Amounts_Oranges = 2.2929389

Amounts_Poached_Eggs = 0.14184397

Amounts_Popcorn,Air_Popped = 13.869322
```

Results As we can see, we have a solution with the only constraints (other than minimimum serving size being 0) is that the diet is above and below the minimum and maximum nutrional requirements. Doesn't look to be a good diet though... I certainly wouldn't want to eat it.

0.1.2 Question 2

Please add to your model the following constraints (which might require adding more variables) and solve the new model: a. If a food is selected, then a minimum of 1/10 serving must be chosen. (Hint: now you will need two variables for each food i: whether it is chosen, and how much is part of the diet. You'll also need to write a constraint to link them.) b. Many people dislike celery and frozen broccoli. So at most one, but not both, can be selected. c. To get day-to-day variety in protein, at least 3 kinds of meat/poultry/fish/eggs must be selected. [If something is ambiguous (e.g., should bean-and-bacon soup be considered

Writing out the Optimization Problem

```
[121]: problem = LpProblem('Diet Problem', LpMinimize)
       selectVars = LpVariable.dicts('Picked', foods, 0, 1, cat = 'Integer')
       amountVars = LpVariable.dicts('Amounts', foods, 0)
       problem += lpSum([cost[i] * amountVars[i] for i in foods]), 'total cost'
       problem += lpSum([cals[i] * amountVars[i] for i in foods]) >= diet.iloc[65, 3],__
        \hookrightarrow 'min cals'
       problem += lpSum([cals[i] * amountVars[i] for i in foods]) <= diet.iloc[66, 3],__</pre>
        →'max cals'
       problem += lpSum([cholestrol[i] * amountVars[i] for i in foods]) >= diet.

→iloc[65, 4], 'min cholestrol'
       problem += lpSum([cholestrol[i] * amountVars[i] for i in foods]) <= diet.</pre>
        →iloc[66, 4], 'max cholestrol'
       problem += lpSum([fat[i] * amountVars[i] for i in foods]) >= diet.iloc[65, 5],
       problem += lpSum([fat[i] * amountVars[i] for i in foods]) <= diet.iloc[66, 5],
        \hookrightarrow 'max fat'
       problem += lpSum([sodium[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
        \hookrightarrow6], 'min sodium'
```

```
problem += lpSum([sodium[i] * amountVars[i] for i in foods]) <= diet.iloc[66, u
\rightarrow 6], 'max sodium'
problem += lpSum([carbs[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
\hookrightarrow7], 'min carbs'
problem += lpSum([carbs[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
\hookrightarrow7], 'max carbs'
problem += lpSum([fiber[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
→8], 'min fiber'
problem += lpSum([fiber[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
\rightarrow 8], 'max fiber'
problem += lpSum([protein[i] * amountVars[i] for i in foods]) >= diet.iloc[65, __
\rightarrow 9], 'min protein'
problem += lpSum([protein[i] * amountVars[i] for i in foods]) <= diet.iloc[66, u
\hookrightarrow9], 'max protein'
problem += lpSum([Vit_A[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
\hookrightarrow10], 'min Vit_A'
problem += lpSum([Vit_A[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
→10], 'max Vit_A'
problem += lpSum([Vit_C[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
\hookrightarrow11], 'min Vit_C'
problem += lpSum([Vit_C[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
\hookrightarrow11], 'max Vit_C'
problem += lpSum([Calcium[i] * amountVars[i] for i in foods]) >= diet.iloc[65, __
→12], 'min Calcium'
problem += lpSum([Calcium[i] * amountVars[i] for i in foods]) <= diet.iloc[66, u
→12], 'max Calcium'
problem += lpSum([Iron[i] * amountVars[i] for i in foods]) >= diet.iloc[65,__
\hookrightarrow13], 'min Iron'
problem += lpSum([Iron[i] * amountVars[i] for i in foods]) <= diet.iloc[66,__
\hookrightarrow13], 'max Iron'
#Minimum 1/10 Serving Size
for i in foods:
    problem += amountVars[i] >= selectVars[i]*0.1
    problem += amountVars[i] <= selectVars[i]*100000</pre>
#Poultry Requirement
```

```
problem += lpSum([Poultry[i] * selectVars[i] for i in foods]) >= 3, 'poultry
    →requirement'

#Frozen brocolli and celery requirement
problem += selectVars['Celery, Raw'] + selectVars['Frozen Broccoli'] <= 1</pre>
```

Solve Optimization Problem

```
[127]: problem.solve()
  varsDictionary = {}
  for v in problem.variables():
    varsDictionary[v.name] = v.varValue
    if v.varValue >0:
        print ("{} = {}".format(v.name, v.varValue))
```

```
Amounts_Celery,_Raw = 42.399358
Amounts_Kielbasa, Prk = 0.1
Amounts_Lettuce, Iceberg, Raw = 82.802586
Amounts_Oranges = 3.0771841
Amounts_Peanut_Butter = 1.9429716
Amounts_Poached_Eggs = 0.1
Amounts_Popcorn, Air_Popped = 13.223294
Amounts_Scrambled_Eggs = 0.1
Picked_Celery, Raw = 1.0
Picked_Kielbasa,Prk = 1.0
Picked_Lettuce, Iceberg, Raw = 1.0
Picked_Oranges = 1.0
Picked_Peanut_Butter = 1.0
Picked_Poached_Eggs = 1.0
Picked Popcorn, Air Popped = 1.0
Picked_Scrambled_Eggs = 1.0
```

Results We also have a solution now with the following constraints: - Minimum of 1/10 serving is chosen - Celery and Frozen Brocolli are not both chosen at the same time. - 3 kinds of meat/poultry etc. are chosen.

Still does not look appetizing but the program has done it's job as the solution is both feasible and is the optimal solution.